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Wind Tunnel Tests at Mach Numbers
between 0.6 and 1.4 of a 60° Swept
Wing having an Aerofoil Section
Designed for Subcritical Flow at
a Mach Number of 1.2

Part I: 9% Thick Section with "Triangular"

Pressure Distribution

by

E. F. Lawlor

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SUMMARY

Pressures have been measured at Mach numbers between 0.6 and 1.4 around one streamwise station on a 9% thick, 60° swept wing, cambered to have a subcritical type of upper surface pressure distribution of triangular shape at a Mach number of 1.2 and a lift coefficient of 0.153. In spite of boundary layer effects which caused some loss of lift coefficient, subcritical flow conditions were achieved at the design Mach number of 1.2 with the design suction values over the forward part of the section. At all Mach numbers, the flow development was closely analogous to that over two dimensional aerofoils at subsonic speeds.

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One possible solution to the aerodynamic problem of designing a supersonic long-range aircraft involves the use of a highly swept, high aspect-ratio wing, on the assumption that infinite-swept-wing flow conditions can be maintained all over the wing at the cruising lift coefficient. It has been predicted theoretically¹ that for a sufficiently thin and highly swept wing of infinite aspect ratio a subcritical type of flow can persist up to a supersonic free-stream Mach number, so long as the component of velocity normal to the peak suction line is less than sonic. Under these conditions the wing wave drag remains zero. By extending this concept to swept wings of finite aspect ratio, the aerodynamic outline of a supersonic transport aircraft can be determined as in Ref.2, where the design cruising Mach number is 1.2, although the actual value does not affect the design philosophy in principle.

The first stage in developing a suitable wing for this type of aircraft configuration is to choose a basic wing section shape, together with an angle of sweep, to give an essentially subcritical type of flow at the chosen cruising speed and lift coefficient on a swept wing of infinite span. Theoretical methods have been devised^{3,4} for determining the geometry of aerofoil sections having a specified pressure distribution in an inviscid, incompressible flow. Methods applicable to two-dimensional wings are extended to swept wings of infinite span by the addition of a flow component parallel to the wing leading edge. There are also methods^{5,6} for determining the sonic range ($M = 1$) pressure distribution from a specified two-dimensional aerofoil shape and one of these has been extended⁷ to cover the Mach number range between critical and sonic. The relationship between wing sweep, thickness-chord ratio and lift coefficient for various types of upper surface pressure distribution is discussed in Ref.8.

These methods can be used in the project or early layout stages of an aircraft design to provide estimates of the inter-relation between aerofoil geometry and subcritical pressure distribution, and to predict also the Mach numbers at which drag rise begins or at which separation effects such as buffeting might be expected to appear. In general, good agreement can be obtained between experiment and theory for both moderately swept and unswept wings at low speeds, providing the characteristics of the boundary layer are determined and taken into account (see for example Refs.9 and 10).

The present series of tests is aimed at extending the comparison between experiment and theory to higher angles of sweep and higher Mach numbers, and in particular to cover the case where the free-stream Mach number is supersonic but the flow over the wing is still expected to be subcritical. There are three main objectives:-

- (a) To demonstrate experimentally that a subcritical type of flow, without shocks, can exist at a supersonic free-stream Mach number on a lifting wing;
- (b) to determine the extent to which viscosity and compressibility modify the theoretical pressure distribution around the aerofoil section of an infinite swept wing when the flow is subcritical; and
- (c) to investigate the influence of the local supercritical region, produced by increasing Mach number or lift coefficient above the values for (a), on the drag and shock-induced boundary-layer separation characteristics of the section.

These tests are being conducted on half models (Fig.1), having untwisted and substantially untapered wings, of aspect ratio near 5 and 60° sweepback, mounted on a body. The aerofoil sections are in general designed to have

a subcritical type of flow up to a Mach number of around 1.2 using the method of Ref.4 modified to take account of compressibility effects - see Appendix 2. Measurements of pressure only are made all round a streamwise section at 71% semi-span.

For the tests reported in the present note, the wing section is of basically RAE 101 thickness distribution, 9% thickness-chord ratio, and cambered to have a "triangular" or "linear" shape of upper surface pressure distribution at a C_L of 0.153 at a Mach number of 1.2 (Figs.2 and 3). The results show that, in general terms, subcritical flow conditions can be maintained at supersonic Mach numbers, for instance at $M_0 = 1.2$ and $C_L = 0.085$, although at the design C_L of 0.153 a small supercritical region exists which is insufficient to cause an appreciable rise in drag. No attempt has been made in this test to determine the characteristics of the boundary layer quantitatively; this will be done later, however, for another model having a thinner section.

The tests form part of the programme of the Cruising Aerodynamics Group of the Supersonic Transport Aircraft Committee (S.T.A.C.). They were planned initially for the 8 ft x 8 ft supersonic tunnel at R.A.E. (Bedford). However, as the scope of the activities of the S.T.A.C. widened, it became desirable to transfer the actual testing to the 9 ft x 8 ft transonic tunnel of the Aircraft Research Association, Ltd., Bedford. This tunnel has a perforated-wall working section, and a flexible nozzle which together with auxiliary suction from the plenum chamber surrounding the working section enables Mach numbers of up to 1.4 to be achieved. A description of the tunnel is contained in Ref.11. The tests were made in May, 1958.

Section 2 of this note describes the design of the model and some of the problems which were encountered. The test procedure is outlined in section 3, and some comments on the accuracy of the results are given in section 4. The results are presented and discussed in section 5, which also includes a review of the expected development of the flow over an infinite sheared wing. Finally, section 6 contains the conclusions and considers certain further tests which are desirable.

2 MODEL DESIGN

2.1 Experimental approach to achieving sheared-wing conditions

Sheared-wing conditions demand that the pressures experienced by the section should be constant along lines parallel to the edges of the wing. In general these conditions are not achieved near the root of a swept wing, so that, unless the root of the wing is carefully shaped, the isobars in this region are less highly swept than the wing and unswept altogether at the root itself. Similarly, near the tip of the wing the isobars may again be insufficiently swept unless a careful choice of tip planform and camber is made. On many low aspect ratio wings these root and tip effects overlap so much that nowhere does the flow closely resemble yawed wing conditions.

In the tests reported here, the aim has been to measure the pressures at a spanwise station as far away from the root as possible while maintaining sufficient span outboard to ensure that at all supersonic speeds the Mach cone from the tip passes well downstream of this station. It was considered that sheared-wing flow was unlikely to be achieved, even approximately, inboard of the spanwise station at which the wing root trailing edge disturbance (the "rear shock" in Fig.4(a)) had passed forward of the leading edge. (This assumes it spread along a Mach wave.) It was therefore decided to design an untapered wing of the required sweepback on which measurements

of pressure would be made at a single streamwise section lying aft of the root disturbance and ahead of the tip disturbance. Nevertheless, it was realised that there must be significant viscous effects since these considerations were leading to a combination of high sweep with high aspect ratio which in turn demanded a relatively thick section if model strength, and hence Reynolds number, were not to be unduly sacrificed.

Although it would have been desirable to reduce the magnitude of the wing root disturbance by having a body in which a cylindrical shape could be replaced by a "waisted" shape, it was hoped that this would not be necessary in this experiment. Provision was nevertheless made for fitting alternative body shapes, although only the cylindrical shape was used. Later tests of similar models have included "waisted" configurations.

2.2 Model layout

The basic model is sketched in Fig.1. It is a half-wing-body combination on which pressure measurements are made at 49 points on a single streamwise section on the untapered part of the wing. This configuration was preferred to a complete sting-mounted model because of the larger scale which was possible for a half model. The basic shape of the wing section to give the pressure distribution shown in Fig.2 has been determined by Weber's method given in Appendix 2.

Ordinates of the wing section at 32 pivotal points, which are relevant to the methods of Ref.4 and Appendix 2, have been determined from inspection of the model and are given in Table 1. The wing was found to be thin (8.94% instead of 9%) and to have a twist of -0.06° at the pressure measuring station; after making allowance for these considerations all ordinates were correct to within ± 0.002 ". The ordinates of the pressure holes as determined from the inspection report are listed in Table 2.

The design of the model was arranged to ensure that the shock pattern from the wing root would not be reflected from the walls of an 8 ft x 8 ft tunnel in such a way as to strike the model in the region of the pressure plotting station above $M_0 = 1.1$. This condition set limits to model size, sweepback and spanwise position of the pressure plotting station. The design was also arranged to ensure that disturbances originating at the wing root trailing edge passed (assuming they spread along a Mach wave) in front of the pressure plotting station at Mach numbers up to 1.5. This condition also set limits to the sweepback and spanwise position of the pressure plotting station. A compromise between these conflicting factors resulted in a wing of 12 ins root chord, sweepback 60° , and with a pressure measuring station 1.825 chords (21.9 inches) outboard of the effective model centreline. This in turn influenced the choice of thickness-chord ratio towards a fairly high value (9% along wind) in order to ensure adequate model strength. Since a condition of the design of wing section² is that nowhere over the surface of the wing should the Mach number, resolved in a direction normal to the leading edge, appreciably exceed unity ($C_p \frac{1}{2} C_p^*$), a limit was set to the lift coefficient which could be achieved at the design Mach number. The values finally chosen were a C_L of 0.153 at $M_0 = 1.2$ with almost wholly subcritical inviscid flow. The upper surface pressure distribution (Fig.2) is of a "triangular" shape, and was obtained by adding a suitable camber line (Fig.3) to a basically RAE 101 thickness distribution. The curvature in the camber line towards the trailing edge produced a concavity in the lower surface of the section, which was "filled in" to provide a plane surface to ease manufacture. The change in camber produced by this modification was less than 0.1% at the maximum, and the effect on the upper surface pressures was not significant.

This particular combination of sweep, thickness and lift coefficient is of course only relevant in so far as it is intended to produce the desired flow conditions for the tunnel model. Further tests are being made on thinner wings which may be more relevant as a choice for an aircraft configuration.

The extent of the wing outboard of the pressure measuring station is determined by the condition that the Mach cone from the tip region should pass wholly downstream of this station when the Mach number exceeds 1.10. The actual tip shape has been chosen so as to inhibit a loss of sweep of the isobars with consequent possible spread of the disturbances inboard. The overall semispan of the model is 30.9 ins (2.575 chords) and the pressure plotting station is at 0.71 semispan.

The basic body is of 0.4 chords (4.8 ins) diameter and consists of a nose of length 4 chords (length-diameter ratio 10) plus a parallel portion which extends from 0.5 chord in front to nearly 4 chords behind the wing root leading edge, terminating in a bluff base (Fig.5). The body cross-section is D-shaped; where the body is parallel the section consists of a semicircle 2.4 ins (0.2 chord) radius displaced outwards from the wall by the addition of a 2 in. thick parallel slab, in order to minimise any effects of the tunnel boundary layer. Further forward, along the length of the nose, the body section shape is similar but decreases smoothly in area to zero at the nose; this variation is given, in units of body maximum radius, by

$$y = \left(\frac{x}{20} - 1 \right)^3 + 1$$

where x = distance aft of the nose

y = local body radius.

This variation ensures that the curvature of the nose shape in plan view tends to zero at the front of the nose and again at the junction with the parallel part of the body. This type of nose was chosen to minimise the influence of the body pressure field (reflected from the walls of the tunnel) on to the pressure plotting station. The nose shock, reflected from the roof of the tunnel, clears the pressure plotting station at all Mach numbers above 1.12. Its reflection from the side walls of the tunnel, however, passes along the pressure plotting chord line between Mach numbers of 1.28 and 1.34. At the design Mach number of 1.2, the pressure plotting station is subjected to the reflected field from a region about half way along the length of the nose. This region produces a weak expansion field, which in the A.R.A. tunnel is reflected weakly as a shock; it is believed that this "second-order" disturbance does not appreciably influence the measured pressures.

The wing was made of S96 steel, heat-treated to give an ultimate tensile strength of over 70 tons/sq in. Grooves were cut in the wing to allow 0.080 in. o/d (0.053 in. i/d) copper-nickel tubes to be laid in the wing from each pressure hole (1/32 in. dia.), the pressure tubes being faired over afterwards with araldite. The body was largely constructed in light alloy.

The model was mounted on the floor of the A.R.A. 9 ft x 8 ft tunnel. Bracing wires attached to the model near the wing tip passed out through perforations in the tunnel walls and were secured at each incidence to restrain the wing from deflecting under load. The wires and attachments at the model did not exceed 0.25 in. dia. and were situated at 30% chord 6 ins. outboard (measured normal to body axis) of the pressure measuring station,

this location being chosen so that the disturbances from the wires should pass wholly downstream of the pressure measuring station at all supersonic Mach numbers. Some studies of oil flow patterns at $M_0 = 1.25$ and 1.4 (Figs. 27 and 28) would seem to indicate that the flow at the pressure plotting station was not significantly influenced by the wires.

3 TEST PROCEDURE AND RANGE OF TESTS

The procedure adopted was to fix the model incidence and tunnel pressure, and then vary the Mach number from 0.6 to 1.4, taking care as far as possible that the intervals of Mach number were close enough in the neighbourhood of the drag rise and separation Mach numbers to enable values of M_D and M_{SE} to be obtained. The bracing wires from the wing tip had to be re-rigged at each change of incidence, and therefore the tunnel was shut down between incidence runs.

The theoretical design incidence α_T for the wing of infinite span was 1.83° ; in order to investigate the flow over a wide range of conditions, tests were made at a range of incidences from 0° to 5° . A carborundum strip (particles 0.002 to 0.003" high) was applied around the leading edge and extending back to 5% chord on both surfaces but with a small gap in the immediate proximity of the pressure holes) in order to fix transition. Figs. 27 and 28 show that there is a striated flow pattern behind the carborundum strip which is consistent with turbulent flow; whereas at the extreme wing tip, outboard of the carborundum strip, the pattern is not striated so strongly forward of the turbulent "wedge" springing from the end of the strip. On this evidence it would appear that turbulent flow was successfully achieved over most of the wing.

At each Mach number, complete pressure readings of the section were recorded by photographing a multi-tube mercury manometer. Most of the tests were made at atmospheric stagnation pressure, so that the Reynolds number (based on wing chord) varied from 3.8×10^6 at $M = 0.6$ to 5×10^6 at $M = 1.0$, remaining close to 5×10^6 at all supersonic speeds. In addition, however, one run was carried out at an incidence of 2.6° at a stagnation pressure of 36" mercury. For this run the Reynolds number varied from 4.5×10^6 to 6×10^6 . The variation of Reynolds number with Mach number and stagnation pressure is shown in Fig. 19.

4 ACCURACY

The mercury manometer readings were recorded on film which was subsequently projected on to a screen from which the readings were recorded manually. It was possible to read the height of the mercury columns to ± 0.02 in. and this results in an error of ± 0.002 in p/H_{eff} (see para. 5.1).

When integrating pressures around the section to determine force coefficients, the trapezium rule has been used for simplicity and convenience, thus enabling coefficients to be compared on a consistent basis, even though there is some loss of absolute accuracy. Because of the large number of pressure holes and their close spacing (approx. 0.0050) around the nose, the force coefficients are always correct to within $\pm 2\%$, and in all but a few cases to within $\pm 1\%$.

For Fig. 12 to 15 the values of pressure coefficient (C_p) have been obtained by a process of "smoothing" the experimental results, as described in para. 5.3. It is therefore necessary to take into account the accuracy of the smoothing process in assessing the accuracy of the data plotted on these figures.

5 RESULTS AND DISCUSSION

5.1 Presentation of results

It is convenient to present the pressures measured at each pressure plotting hole in the form of p/H_{eff} , where p is the local pressure and H_{eff} is a "reduced" form of the total head which effectively corresponds to the two-dimensional value at a free stream Mach number of $M_0 \cos \Lambda$ (Λ = sweepback angle). The value of H_{eff} is determined from the actual total head H_0 by the following relation:-

$$\frac{H_{\text{eff}}}{H_0} = \left(\frac{1 + \frac{\gamma - 1}{2} M_0^2 \cos^2 \Lambda}{1 + \frac{\gamma - 1}{2} M_0^2} \right)^{\frac{\gamma}{\gamma - 1}}$$

A derivation of this relation is given in Appendix 1.

Provided that yawed wing conditions have been achieved these values of p/H_{eff} are directly comparable with the values of p/H_0 in two-dimensional flow at $M_0 \cos \Lambda$.

5.1.1 Pressure distributions

The pressure distributions measured at various Mach numbers are plotted in the form of p/H_{eff} for each incidence in Figs.6 to 11. The pressures are shown in carpet form plotted against x/c (chordwise position) and Mach number. The values of p/H_{eff} at each pressure hole, and the position of each hole as determined by inspection of the model after manufacture, are given in Table 3. Figs.12 to 15 show comparisons of theoretical and experimental pressure distributions at Mach numbers near 0.6 and 1.2 - the pressures in this case being in the form of C_p since the theoretical distributions determined by the method of Appendix 2 are in this form. In Figs. 12 to 15 only, however, some adjustments have been made to the measured pressures which have the effect of smoothing the variation of pressure at any pressure hole with variation of Mach number. This procedure is discussed in greater detail in para.5.3.

5.1.2 Integrated loads

The pressure distributions around the section have been integrated normal to and along the chord at each Mach number and incidence, and the results are tabulated in coefficient form as $\overline{C_z}$ and $\overline{C_x}$ in Table 4. The coefficients are plotted against Mach number for various incidences in Figs.16 and 17, while $\overline{C_z}$ is plotted against incidence for a Mach number near 1.2 and compared with theory for inviscid flow and infinite aspect ratio in Fig.18.

5.2 Effect of Reynolds number

An additional run at an incidence of 2.6° only was made at a stagnation pressure of 36 ins. mercury, the Reynolds number varying from 4.5×10^6 at $M_0 = 0.6$ to about 6×10^6 at supersonic speeds (Fig.19). The corresponding

run at the lower Reynolds number (30 ins. mercury) was only made at Mach numbers from 0.98 upwards. It was found that nowhere did this admittedly small variation in Reynolds number cause any significant variation in either upper or lower surface pressure distributions (Table 3). The curves of Fig. 6, 7, 9, 10 and 11 are all for 30 ins. mercury stagnation pressure. However, the curves of Fig. 8 ($\alpha_E = 2.6^\circ$) are for 36 ins. mercury, except for $M_0 = 1.405$ which is for 30 ins.

5.3 Disturbances in flow development

5.3.1 Disturbances affecting pressure distribution

Figs. 6 to 11 show that the development of pressure distribution with Mach number is not entirely regular. In general, the pressures around 40% chord seem to be slightly greater (less suction) than expected. Inspection of the model revealed nothing likely to account for this, but it is possible that a leak may have developed during the test in the appropriate pressure tube.

More significantly, there are areas over which the rate of decrease of pressure with Mach number is temporarily reduced, as for example near $M_0 = 0.98$ over the rearmost 20% of the chord. Because of the high sweep and aspect ratio of the model, the trailing edge of the pressure plotting station was located 14 inches further downstream in the tunnel working section than would have been recommended¹¹ for a complete model. However, any deterioration of the flow near this region is mainly associated with the complete-model support strut, which of course was not present for these tests. It seems more probable that the local high pressure region near the trailing edge at $M_0 = 0.98$ is due to a simple blockage effect.

Over the most forward 30% of the chord a similar local high pressure region occurs at all incidences near $M_0 = 1.02$. Application of a blockage correction does not account satisfactorily for this effect. Some tests at close intervals of Mach number on a later wing in the series have shown that a similar region moves rearwards over the section as M_0 is increased from 1.02 to 1.04. The rate of movement suggests a disturbance originating from the forward part of the model and being reflected from the tunnel sidewalls. The source of this disturbance is probably the suction region expected to occur at this Mach number over the rear part of the section at the wing root. At the sidewalls this suction would be reflected as a compression¹². A properly waisted body would thus be expected to improve matters. Some disturbance would also be expected from the bow shock associated with the bracing wire near the tip, but the chordwise extent of the disturbance (about 0.3 c) seems rather large for it to be accounted for entirely by the wire.

Another region of relatively high pressure occurs over the upper surface of the wing between 25% and 50% chord at $M_0 = 1.19$. The cause in this case appears to be a disturbance originating from the saw-tooth junction in the tunnel floor and being reflected from the roof. Moreover, the analysis in the next section (5.3.2) reveals that on the lower surface there is a low pressure region further aft (45% to 70% chord) which could arise from a different part of the same disturbance (Fig. 25). Other deviations in pressure between 50% and 80% chord near $M_0 = 1.35$ on the lower surface have probably arisen from the disturbance due to the other saw-tooth junction in the roof being reflected from the floor.

At low incidences (0° and 2°) the suction at 6% chord seems to be slightly low over most of the Mach number range; at 2.6° this "trough" has moved back to 8% and is more noticeable. Also, at high incidences (up to 4°) the pressure distributions near the nose are rather "wavy", especially between Mach numbers of 0.9 and 1.0, and there appears to be a "double peak suction" at 3% and 10% chord at $M_o = 0.9$ and 0.94 . On a later model in the series, similar effects have been found to arise from the discontinuity in the transition strip near the pressure plotting station, suggesting that the boundary layer may be laminar within a limited region between the transition strips. This may be giving rise to a local laminar bubble separation, with subsequent reattachment as a turbulent layer, at the higher incidences.

5.3.2 Disturbances affecting integrated loads

The variation of \overline{C}_X with Mach number for various incidences (Fig.17) shows that a sudden change in \overline{C}_X is observable near $M_o = 1.02$ followed by some deviations at higher Mach numbers. The similarity of the curves for various incidences suggests that the source of these deviations is probably external to the wing section, and may arise from disturbances spreading out from the root, or from the tunnel flow itself. These disturbances need only be very localised; for instance, if only the first 10% of the chord is affected on both surfaces, there may be a substantial effect on \overline{C}_X and yet not on \overline{C}_Z .

The curves of p/H_{eff} against M_o and x/c (Figs.6 to 11) show that the pressure over the front 30% of the chord is relatively high at $M_o = 1.02$ which accounts for much of the high value of \overline{C}_X . Also, at $M_o = 1.19$ there is a further band of high pressure between 25% and 50% chord; however, in this region it does not significantly affect \overline{C}_X . On the other hand, the region of high pressure aft of 55% chord at $M_o = 1.10$ contributes to a reduction in \overline{C}_X at that Mach number. Since the results are believed to be affected in this way, it has been thought worthwhile to attempt to correct them. To do this, the experimental pressures for one incidence ($\alpha_E = 2.6^\circ$) for both upper and lower surfaces have been plotted as a ratio of tunnel stagnation pressure (i.e. in the form p/H_o) in Figs.20 and 21 in carpet form against chordwise position and Mach number, together with the curve of p_o/H_o for free stream conditions. An attempt is made on these figures to draw "smooth" curves through the pressures measured at each pressure hole. The deviation of each value of p/H_o from its appropriate "smooth" curve has been integrated around the chord in the same manner as the pressures themselves and used to provide a deviation in \overline{C}_X , plotted as ΔC_X in Fig.22. For Mach numbers above 1.2 this method could not be used for the upper surface due to the onset of supercritical flow with shock waves. In this region, therefore, ΔC_X has been taken as twice the value appropriate to the lower surface. The curves of Fig.22 show that below $M = 1.2$ this procedure would in general give a reasonable estimate of ΔC_X . The values of ΔC_X so obtained have been taken to apply at all incidences. When applied to \overline{C}_X , and resolved together with \overline{C}_Z to provide C_D , a fairly plausible variation of

* Smooth - defined here as being of the same general shape as the curve of p_o/H_o against M_o .

C_D with Mach number and incidence is obtained (Fig.23). These values of C_D also include an allowance for skin friction drag under tunnel conditions. This has been estimated by the method of Refs. 17a and 21 and is shown in Fig.19. Comparison of the values of total C_D with those of ΔC_X help to put into better perspective the scatter in the experimental results.

The assumed corrections to the flow, in terms of the deviations in p/H_0 used for the construction of Fig.23, are shown as a plot of local Mach number in Figs.24 and 25. The reduction of Mach number near the nose at $M_0 = 1.02$ occurs on both surfaces. The low Mach number aft of 55% at $M_0 = 1.10$ is seen to be more marked on the upper than the lower surface. The reduction in Mach number at about 40% chord at $M_0 = 1.19$ seems to be confined to the upper surface, while there is an increase in Mach number (and hence suction) around 50% to 70% chord on the lower surface which will also be contributing to the increase in $\overline{C_X}$ observed at this M_0 ; these deviations are unfortunate in so far as they occur near the design Mach number. On the other hand the deviation near the nose is not considered to be a spurious effect but is associated with the imminent development of a local supersonic region.

5.4 Predicted flow pattern over sheared wing

Before discussing the results in detail, it may be worth briefly reviewing the physical principles underlying the concepts of subcritical and supercritical flow over an infinite sheared wing.

In considering the inviscid flow pattern expected to develop over the wing, it is suggested that only the component of flow normal to the wing leading edge is significant. Thus the onset of critical flow conditions, with the associated drag rise and separation effects, is governed solely by the magnitude of the Mach number component normal to the wing and is independent of the component parallel to the wing, irrespective of magnitude. The parallel component serves merely to influence the resultant (i.e. free-stream) Mach number and the absolute magnitude of the pressures. On simple assumptions such as these, there is no theoretical limit to the magnitude of this parallel component, and no significance is necessarily attached, therefore, to a free-stream Mach number of unity or greater.

Defining now the critical Mach number M_{CR} as the Mach number at which the flow component normal to the isobars first reaches a sonic value somewhere over the section, it is found that above M_{CR} the flow expands rapidly from the attachment line (equivalent to the stagnation line on a two dimensional wing) so that the component normal to the isobars is supersonic over an appreciable part of the section. Behind this region, the pressure recovers to a value which differs little from that given by the appropriate subcritical distribution. The manner of recovery is at first almost isentropic but, at supercritical Mach numbers, soon develops into a shock which in plan view will be fully swept, if sheared wing conditions are being maintained. With further increase of Mach number, the shock moves back along the section and increases in strength, producing in due course an increase in section drag. Eventually, as Mach number is increased still further the pressure rise across the shock becomes sufficient to cause the boundary layer to separate forward of the trailing edge, producing non-linear changes in lift and drag. If the drag rise Mach number is defined as M_D , and the Mach number at which separation effects become noticeable is defined as M_{SE} , the

significance of these Mach numbers is broadly that M_D sets a limit to the aerodynamic efficiency of the wing section and hence to the cruising economy of the aircraft, and M_{SE} sets a limit to the usable speed of the aircraft, due to effects such as buffeting and possibly loss of control effectiveness.

The problem is therefore to achieve as high a Mach number as possible for the onset of drag rise while retaining an adequate margin between this Mach number and the Mach number for the onset of separation effects.

As in the two-dimensional case, several basically different types of pressure distribution suggest themselves, for example:-

(a) a distribution which at lift has a peak suction well forward (i.e., ahead of, say, 0.2 chord) followed by approximately linearly increasing pressure to the trailing edge. The shape of this distribution is thus roughly "triangular",

(b) a distribution which, after an initial rapid fall near the leading edge, has approximately constant pressure over part of the chord (back to 0.5 chord, say), followed by a more rapid increase in pressure to the trailing edge, i.e. of "rooftop" shape at its design lift coefficient.

For a given lift and thickness the peak suction for the "triangular" type will in general be greater than for the "rooftop" type, so that M_{CR} will be lower. However, as Mach number is increased above M_{CR} the supersonic region for the triangular type will initially be confined to forward-facing parts of the section, i.e. ahead of the crest (defined as the chordwise station where the upper surface slope is parallel to the undisturbed stream), whereas for the rooftop type the supersonic region will quickly extend to the back of the rooftop, i.e., well behind the crest. Tests by Nitzberg and Crandall¹³ suggest that M_D is closely associated with the Mach number at which the shock moves aft of the crest, so that for the triangular type the margin $M_D - M_{CR}$ may be greater than for the rooftop. It is not, therefore, immediately apparent which type will have the greater value of M_D . Moreover, with the triangular type there is a less severe adverse pressure gradient aft of the maximum suction so that the margin $M_{SE} - M_D$ may also be greater for this type, since the corresponding strength of shock needed to cause the boundary layer to separate will also be greater. Thus the value of M_{CR} alone is not necessarily a reliable guide to the merits of different wing sections from the viewpoint of drag rise and separation effects.

In the tests reported here, the upper surface pressure distribution is of the "triangular" type. Further tests on other sections of "rooftop" type are in progress and will be reported in due course.

5.4.1 Three dimensional effects

Departures from infinite sheared wing flow occur in general on finite wings in the neighbourhood of the tips and of any abrupt changes in sweep, as for instance at the root of a wing of V planform. In this experiment the influence of the tip is confined at supersonic speeds to a conical region which always passes well downstream of the pressure measuring station. However, the compressions which arise near the wing root leading edge and the wing root trailing edge may give rise to shocks spreading outboard along the wing at sufficiently high Mach numbers (Fig.4b). These shocks, which are sometimes called the forward and rear shocks, tend to approach and coalesce

somewhere along the span, thereafter forming a single shock called the outboard shock. By placing the pressure plotting station well outboard these root effects are minimised but may not be entirely negligible; later tests of other section shapes incorporate shaping of the body at the root in order to try to reduce these effects still further.

5.5 Compressibility and viscosity effects

The theoretical estimates of pressure distribution given in Refs.3 and 4 do not include compressibility or viscosity effects. In Appendix 2, however, an extension of these methods is given which allows the effect of compressibility to be estimated; this extension has been used to provide the theoretical estimates for these tests. The experimental results include both compressibility and viscosity effects, and differ (as might be expected) from the inviscid theoretical estimates.

It has been shown (in Refs.9 and 10 for example) that the incompressible inviscid theory can be used to give good estimates of pressure distributions at low speeds on both unswept and swept wings of symmetrical section, providing that allowance is made for the displacement thickness of the boundary layer. For example, Ref.10 gives the loss in loading, due to boundary layer effects, along a chord at 0.41 semispan on a 12% thick RAE 101 section wing of 45° sweep. In this case, measurements of the boundary layer profile were made just behind the trailing edge, and the displacement thickness estimated. The theoretical pressure distribution was then re-calculated for the aerofoil profile as modified by the addition of the displacement thickness, and it was found to agree well with the experimental results.

In the tests reported here, the wing section is no longer symmetrical, compressibility effects are present, and the high sweepback and aspect ratio would be expected to produce a substantial boundary-layer displacement thickness. No measurements have been made, however, of the boundary layer profile in this test and hence no allowance for it appears in the theoretical estimates. It is therefore not possible to devise a wholly satisfactory criterion for comparing theory and experiment. The provisional criterion chosen has been the simple one of equal level of peak suction. This at least shows to some extent the differences between the general shapes of the theoretical and the experimental upper surface pressure distributions without significantly affecting the Mach number for the onset of critical flow conditions.

For later tests in the series, boundary layer profiles are being measured at the trailing edge of the pressure plotting station, and it is hoped that this will enable comparisons to be made in future between the theory for inviscid flow and experiment so that the viscosity effects can be shown up and studied in more detail.

In much of the discussion which follows, the conditions of subcritical flow and supercritical flow have been treated separately. However, in those figures in which parameters are plotted against Mach number, the whole Mach number range has been covered. It follows, therefore, that the reader may be referred to different parts of the same figure on different occasions.

5.6 Subcritical flow conditions

5.6.1 Comparison with theory

At the lowest subsonic Mach number of 0.6, the theoretical (inviscid, compressible, and for infinite aspect ratio) and experimental pressure distributions are shown in Fig.12, which is a carpet plot of C_p against x/c and incidence. By comparing the distributions for equal levels of peak

suction it has been found possible to relate the theoretical and experimental wing incidences (α_T and α_E) by an empirical equation of the form

$$\alpha_E = N \alpha_T + K$$

and for this Mach number the best agreement is obtained by putting $N = 1.2$ and $K = 0.7$ (degrees). The value of N of 1.2 is partly accounted for by the finite aspect ratio. Extrapolation from the results of Ref.14 for wings of somewhat similar planform suggests a value of 1.1 for incompressible flow. No tunnel constraint corrections have been applied to the results. The normal Glauert correction would not be significant but there is some uncertainty as to the precise nature of the boundary condition at the wing root. Experience at A.R.A. suggests that a small part (perhaps 10%) of the deficiency in lift curve slope might be attributed to root effects. Much of the remaining discrepancy may be due to the influence of viscosity.

The reason for the additional shift of 0.7° is not understood; it appears at other Mach numbers and at zero lift (as noted in para.5.6.3) but does not seem to be accounted for by deviations in the tunnel flow or twist of the wing. Since it occurs at zero lift, where the pressure gradient on the lower surface is more adverse than that on the upper surface, it does not seem likely that its origin is due solely to viscous effects, although on a later model the addition of vortex generators to the upper surface only has been found to decrease the zero lift angle by up to 0.3° .

In Fig.13 the theoretical and experimental pressure distributions on both surfaces at $M_0 = 0.6$ are compared at closely corresponding levels of peak suction, and shows satisfactory agreement over the forward 30% of the chord. Further aft, where the pressure gradients are unfavourable, there is some loss of loading so that C_L is about 17% less experimentally (0.100 as compared with 0.120), possibly because of viscous effects. In addition, the predicted positive pressure coefficient near the trailing edge is not achieved, as is commonly observed.

Turning now to the design Mach number of 1.2, the theoretical and experimental pressure distributions (Fig.14 and 15) show that, for equal levels of peak suction, there is a greater loss of loading over the rear of the section than at a Mach number of 0.6. Fig.14 shows that the theoretical (again inviscid, compressible, and for infinite aspect ratio) and experimental wing incidences are now related by the equation

$$\alpha_E = \alpha_T + 0.7$$

and in this case α_E is varying at the same rate as α_T ($N = 1.00$), instead of 20% more rapidly as at $M_0 = 0.6$. Some calculations of the spanwise variation of twist at $M_0 = 1$ in Ref.15 suggest that for wings having triangular (linear) chordwise loadings the incidence at the pressure measuring station would only be about 6% greater than the infinite sheared wing value ($N = 1.06$). The discrepancy in N is probably partly due to the fact that near locally critical conditions the peak suction pressure coefficients in practice tend to change more rapidly with incidence than the subcritical theory predicts. It is however noteworthy that the other discrepancy of 0.7° persists. In Fig.15 the pressure distributions on both surfaces are compared at closely corresponding levels of peak suction near to the design

value. Although agreement is still good in the regions of favourable pressure gradient, these are confined to the forward 10% of the upper surface and the forward 30% of the lower surface, and behind these regions both surfaces, but particularly the upper, contribute to a considerable loss of loading.

It appears that, although the level of peak suction has risen rapidly with Mach number, the suction well aft of the peak (for instance at 60% chord) actually falls, in terms of C_p , so that overall there is also a fall in C_L (from 0.100 at $M_0 = 0.6$ to 0.085 at $M_0 = 1.2$) instead of a gain as predicted for inviscid flow (from 0.120 at $M_0 = 0.6$ to 0.153 at $M_0 = 1.2$). Thus at $M_0 = 1.2$ the experimental lift coefficient is 44% less than the theoretical value; some of this effect may be attributable to the low value of N as discussed above, but even if the value of N were taken to be 1.2 (as at $M_0 = 0.6$) the loss in C_L would still be 34% ($C_L = 0.100$). For equal C_L the value of N would have to be 1.8. It is not clear how a discrepancy of this magnitude arises, unless it is due to much more severe viscous effects than those encountered at $M_0 = 0.6$. The increase in M_0 , in spite of (or perhaps even together with) the increase in Reynolds number from 3.8 to 5.0×10^6 may possibly be producing a more rapid and non-linear thickening of the boundary layer on the upper surface. It was found in Ref. 10 that even at low speed and a lower sweep (45°), at a station 0.41 semi-span outboard from the root of an aspect ratio 3 wing, that the flow direction was parallel to the trailing edge (i.e. "spanwise") at the trailing edge and for a height of nearly 0.01 chord above it at a C_L of 0.57. The resultant loss in C_L compared with an inviscid estimate neglecting boundary layer thickness was 14%. However, by determining and adding the displacement thicknesses on both surfaces of the aerofoil, and treating the resultant "modified" aerofoil by the inviscid theory, it was found that the loss in C_L could be accounted for fully. It was also found¹⁰ that this loss of lift increases with angle of sweep. Later tests in the present series will include measurements of boundary layer profiles at the trailing edge, as well as the addition of vortex generators, in an endeavour to assess quantitatively the nature and magnitude of viscous effects.

5.6.2 Normal force and drag

The variation of \overline{C}_Z with M_0 for various incidences (Fig. 16) shows that very little change in \overline{C}_Z occurs with Mach number, except at high incidence and Mach number where a flow separation behind a shock becomes established. The nature of this separation is discussed in more detail in para. 5.7.3. Its effect on the pressure distribution is to increase the suction over the rear part of the upper surface (Fig. 11 shows this happening at 5° incidence at all Mach numbers above 1.15) and hence to increase both \overline{C}_Z and \overline{C}_X .

The comparison of theoretical and experimental values of \overline{C}_Z as a function of incidence show (Fig. 18) that at zero lift the experimental angle of incidence α_E is about 0.8° greater than the theoretical value α_T , corresponding closely to the discrepancy of 0.7° found when comparing theoretical and experimental pressure distributions (para. 5.6.1). The loss of loading discussed in para. 5.6.1 appears in Fig. 19 as a reduction in the slope of the experimental curve.

The drag coefficient, corrected by the method of paragraph 5.3.2, is plotted against Mach number for various incidences in Fig.23. As predicted by the yawed wing analogy, there is no significance in a Mach number of unity. Thus, in spite of the shortcomings of the experimental pressure distributions, the flow conditions predicted in Ref.1 have been achieved - i.e., an effectively shock free flow has been obtained - with lift - at a supersonic Mach number, without incurring any penalty in wave drag.

No detailed comparison between theory and experiment has been made at the design lift coefficient ($C_L = 0.153$) and Mach number (1.2), since the experimental pressure distribution includes an appreciable supercritical region well forward, and an incipient separation near the trailing edge. Instead, the approach preferred here has been to make comparisons for similar values of pressure coefficient over regions of favourable pressure gradient, and to look for possible reasons to account for the loss in loading over the remaining regions. However, it is worth noting that at the design lift coefficient there is no great increase in drag over the subcritical value, so that although the flow is no longer shock free the design conditions of Mach number and lift have been achieved without appreciable penalty (except that the margin $M_{SE} - M_D$ is virtually zero, since both M_{SE} and M_D are close to 1.2 at this incidence).

5.6.3 Trailing edge pressure recovery

In Fig.26 the pressure coefficient (C_p) has been plotted for the upper surface at 95% chord. This figure shows that, except for Mach numbers between 0.9 and 1.0, the pressure coefficient at this position was never greater than 0.032. This is rather less than, for example, the pressure coefficients measured at 90% chord on a tapered wing of 59° sweepback¹⁶ in which the value of C_p , everywhere outboard of 40% semispan, was around 0.06, at low speed and at a Reynolds number of 1.6×10^6 (the Reynolds number for the tests reported here was at least 3.8×10^6). At 5° incidence, C_p at 95% chord is negative at all Mach numbers. Figs.6 to 11 also show that the pressure distribution is somewhat uneven between 80% and 95% on the upper surface at most incidences and Mach numbers for which the flow has not separated farther upstream. This suggests that the thickness of the boundary layer may be great enough to affect the comparison between theoretical and experimental pressure distributions.

5.7 Supercritical flow conditions

The analogy with two-dimensional flow would suggest that above a certain Mach number which depends on incidence, a shock would form near the nose of the aerofoil. Further increase of Mach number and incidence would cause the shock to move aft and strengthen, followed by an increase in the drag of the section, and leading ultimately to separation of the flow everywhere aft of the shock.

5.7.1 Pressure distribution

The pressure distributions shown in Fig.6 to 11 suggest that in general a recognizable shock (shown by the dotted part of the lines) first appears soon after the value of p/H_{eff} falls below about 0.52 anywhere on the surface. This corresponds to the onset of a region of locally supersonic flow over a two-dimensional section. As Mach number is increased, the position of the shock corresponds approximately to the more aft of the two chordwise positions at which the local value of p/H_{eff} would have been 0.52 if the pressure distribution had remained of subcritical shape. Further aft the distribution

follows the subcritical shape, while in front of the shock the pressure distribution becomes of a typically supersonic form, and in particular the local value of p/H_{eff} no longer decreases with increase of free stream Mach number.

(Near the nose p/H_{eff} actually increases somewhat.) There is thus a strong "Mach-number-component freeze", analogous to the corresponding Mach number freeze observed in many experiments on two dimensional wings, and discussed by Sinnott⁶ and predicted by Randall's theory⁵.

Oil flow patterns observed at an incidence of 2.6° and a Mach number of 1.25 are illustrated in Fig.27. The upper part of the figure shows the outboard two-thirds of the span and the shock wave can be seen crossing the pressure measuring station near 20% chord. In this region it is some 5° less swept than the wing, and further inboard it is tending towards the wing root trailing edge, as well as becoming less sharply defined. It appears therefore that the root is still exerting some influence on the flow conditions at the pressure measuring station. To this extent then the experiment has not succeeded in creating yawed wing flow in the required region, although the correlations with two dimensional flow discussed above suggest that at this station the root effects may not be very significant. Shaping the body at the root would be expected to lessen these effects.

If the Mach number and incidence are further increased the pressure distributions of Figs.8 to 11 suggest that flow separation begins to occur aft of the shock which then ceases to move rearwards and may even move forwards again. The flow pattern was therefore observed at an incidence of 2.6° and a Mach number of 1.40, and is shown in Fig.28. The shock is now passing over the pressure measuring station near the 30% chord position. Behind the shock the oil pattern indicates a large region of separated flow. Inboard of the pressure measuring station the shock moves back and becomes less clearly defined, again suggesting that its origin lies near the wing root trailing edge (compare the "rear shock" of Fig.4(b)). There is another disturbance, however, which is visible well inboard in front of the main shock, and which is more highly swept than the wing; this appears to be the forward shock (Fig.4(b)) which coalesces with the rear shock to form the outboard shock at a point on the span roughly half a chord inboard of the pressure measuring station.

It has been suggested¹⁸ that for flows with a high supersonic leading edge suction peak the bulk of the subsequent pressure recovery may take place isentropically rather than through a shock, under the influence of the reflection of the leading edge supersonic expansion waves as compression waves from the sonic line. The nearest approach to a high supersonic leading edge suction in this experiment occurs at an incidence α_E of 5° (Fig.11). Subcritically the pressure distribution is peaky near the nose, while supercritical values of p/H_{eff} (i.e. less than 0.528) occur down to a Mach number of as little as 0.9. However, up to Mach numbers of at least 1.2 the shape of the pressure distributions suggests a less abrupt pressure recovery than one would expect from a shock, even though the flow has completely separated further aft along the section. This effect is illustrated in Fig.29 where the Mach number for which p/H_{eff} first falls below 0.515 anywhere on the upper surface, and the Mach number for which a recognizable shock appears, are plotted against incidence. It will be noted that at the higher incidences these Mach numbers diverge by an amount which may bear some relation to the extent to which the pressure recovery takes place isentropically.

5.7.2 Comparison with theory

The theoretical prediction of the transonic characteristics of two-dimensional round nosed aerofoils in a sonic stream has been considered by Sinnott⁶ and Randall⁵. Sinnott's method is semi-empirical and applies over the region behind the crest of the aerofoil. Randall's treatment is purely theoretical (inviscid) but deals also with the region forward of the crest almost up to the nose of the aerofoil. Sinnott has also extended his method^{7,18,20} to deal with Mach numbers below unity for which a shock wave is present on the wing surface aft of the crest. He further suggests that this method may be used to estimate drag rise and separation Mach number (M_D , M_{SE}), at any rate for comparative purposes.

Some calculations of pressure distributions have been made using both Sinnott's and Randall's methods. These estimates are compared with the experimental results in Fig.30. Some caution is necessary in interpreting this comparison, however. First of all, estimates for two dimensional wings are being compared with experimental results on a three dimensional wing. Secondly, Sinnott's method is intended for use on fairly thin sections having a value of the parameter χ not greater than 0.9. The parameter χ , introduced in Ref. 6, is defined as

$$\chi = \frac{\left(\frac{z}{c}\right) \text{ at } \frac{x}{c} = 0.02}{\Delta \left(\frac{x}{c}\right) \text{ for } \theta = 2^\circ \text{ to } \theta = 4^\circ}$$

(where θ is the surface slope of the wing section, in the region forward of the wing crest). For this wing $\chi = 1.01$ at $\alpha_T = 1.9^\circ$ (corresponding to $\alpha_E = 2.6^\circ$) so that extrapolation beyond Sinnott's recommended limits is necessary. Thirdly, Randall's sonic range theory cannot strictly be used to treat sections whose shape is defined by a polynomial in $\frac{x}{c}$ which contains terms in both $\left(\frac{x}{c}\right)^{\frac{1}{2}}$ and $\left(\frac{x}{c}\right)$. In the case considered here, a polynomial expansion in $\left(\frac{x}{c}\right)^{\frac{1}{2}}$ was derived from the inspection report* of the aerofoil shape, and the coefficient of $\left(\frac{x}{c}\right)$ was found to be small, although not zero. In any case, the effect of incidence appears as a change in the coefficient of $\frac{x}{c}$. Randall has suggested an approximation for overcoming this difficulty for small incidences; in this experiment the incidence normal to the leading edge (3.8°) is possibly large enough to introduce significant errors.

Using Sinnott's method¹⁸, the pressure distributions downstream of the shock have been derived from the experimental distribution at the highest shock-free Mach number (in this case 1.20) by application of the Prandtl-Glauert rule. In this way, the effects of compressibility and viscosity can be included approximately. The shock position along the chord is then given by the intercept of this pressure distribution for the appropriate Mach

* To avoid any possible differences due to deviations between the nominal (design) and the achieved aerofoil shape.

number with the locus of $\frac{P_{2G}}{H}$ (the subcritical pressure just downstream of the shock position). $\frac{P_{2G}}{H}$ is a function of $\frac{P_1}{H}$ (pressure just upstream of the shock) but varies very slowly - in this case it always lies between 0.52 and 0.53. The value of $\frac{P_1}{H_0}$ is obtained for the appropriate Mach number and shock position. The pressure at the crest (which must be forward of the shock) and the variation of pressure from crest to shock is then estimated. The pressure distribution at sonic conditions has also been calculated by both Sinnott's and Randall's methods; the latter method is of interest here since it deals with the forward part of the aerofoil ahead of the crest.

In Fig.30 the various estimated pressure distributions described above are plotted as full lines. For comparison, experimental values of

$\frac{P}{H_{eff}}$ are also shown as symbols, joined by dotted lines. The experimental value for $M_0 = 1.26$ (where the shock is theoretically at the crest) has, however, been obtained by interpolation between experimental results at nearby Mach numbers.

It is interesting to observe that, downstream of the shock, agreement is reasonably good at all Mach numbers except 1.40 where in any case the flow had separated completely behind the shock. Further, the predictions of shock wave position are in fair agreement in that the shock always lies between the same pressure holes as found experimentally (except again at $M_0 = 1.40$), although it is clear from oil flow pictures (Figs.27 and 28) that the flow field was to some extent influenced by conditions at the wing root.

Just upstream of the shock however, the experimental value of $\frac{P_1}{H_{eff}}$ is sometimes up to 0.02 greater than predicted, while at the crest this discrepancy increases to 0.04 to 0.05 at the highest Mach number. This effect has also been observed in recent unpublished N.P.L. tests; the cause is at present unresolved.

5.7.3 Drag rise and separation effects

The curves of Fig.23 show that a rapid rise in drag coefficient begins when the Mach number and incidence is sufficiently high. Considering initially the case where no flow separation occurs downstream of the shock, the pressure distributions of Figs.6 to 11 show how the shock forms initially well forward on the aerofoil; and gains in strength as it moves back with increase of Mach number and incidence. Initially it is ahead of the aerofoil crest, but as it passes behind the crest the drag of the section starts to rise rapidly. For incidences of 2° or less the shock does not pass significantly behind the crest at Mach numbers up to 1.4, but at $\alpha_E = 2.6^\circ$ the crest is close to 22% chord and the shock passes over this position at just over $M_0 = 1.25$. From Fig.23 the drag rise is seen to begin at around $M_c = 1.25$ at this incidence. This correlation between Mach numbers for shock-on-crest and for drag-rise has been observed in two dimensions by Nitzberg and Grandall¹³ while Sinnott¹⁸ suggests that the Mach number for shock on crest will be given by the condition that $\frac{P_{2G}}{H}$ (for a two dimensional wing) at the

crest is 0.515, a value obtained by analysis of experimental results with a fairly weak shock⁷. For the shock strengths observed in this case a more appropriate value of $\frac{P_2G}{H}$ might be 0.52 to 0.53 but this does not introduce significant errors. The experimentally observed values of Mach number for shock-on-crest and for drag rise are compared in Fig.31 with estimates using the above criterion*. It will be seen that good agreement is obtained between the estimates and the experimental values, except at $\alpha_E = 0^\circ$ where the experimental value has been derived by taking into account a single rather high drag value at $M = 1.408$ (Fig.23), and at $\alpha_E = 4^\circ$ and 5° where some of the drag rise is due to flow separation.

Further increase of Mach number causes the shock to increase in strength until the flow downstream of it separates completely. The condition of practical interest is the onset of the effects of this separation, such as buffeting. Pearcey¹⁹ has suggested that for two-dimensional aerofoils this condition is observed to correspond to the stage at which the separation bubble behind the shock fails to reattach upstream of the trailing edge. When this happens the pressure at the trailing edge decreases abruptly. In the experiment described in this note, the pressures observed at 95% chord have been plotted against Mach number for various incidences in Fig.26, and it will be seen that above $\alpha_E = 2^\circ$ the trailing edge pressure decreases, fairly rapidly, above a certain Mach number which varies with incidence. Thus again an analogous behaviour with two-dimensional wings has been observed. Sinnott¹⁸ suggests a relation between the pressure immediately ahead of the shock at the separation Mach number and the parameter χ which depends on leading edge geometry. This parameter, as pointed out in para. 5.7.2, has a value of 1.01 for this section at $\alpha_E = 2.6^\circ$, which is higher than the upper limit (0.9) recommended by Sinnott; however, by extrapolation from Fig.12 of Ref.18 a value of $\frac{P_1}{H}$ (pressure just upstream of the shock) of 0.31 has been estimated. Experimentally, the value of $\frac{P_1}{H_{eff}}$ is between 0.33 and 0.34 at $\alpha_E = 2.6^\circ$ when the trailing edge pressure diverges, which is at a Mach number between 1.35 and 1.40.

At higher incidences (higher values of χ) Fig.12 of Ref.18 suggests that the value of $\frac{P_1}{H}$ should remain nearly constant at around 0.31; the experimental value of $\frac{P_1}{H_{eff}}$ is in fact found to remain constant near 0.33. The discrepancy of 0.02 in $\frac{P_1}{H_{eff}}$ is probably partly due to the addition of a spanwise component of flow which causes a thicker boundary layer to form so that separation begins slightly earlier. However, with this adjustment the analysis of Sinnott offers a reasonable guide to the separation Mach number of a yawed wing, and in Fig.31 the actual values of M_{SE} for various incidences are plotted together with the curve for $\frac{P_1}{H_{eff}} = 0.33$.

From Fig.31 the margin of Mach number between drag rise and the onset of separation effects ($M_{SE} - M_D$) has been derived and is plotted in Fig.32. This shows that above an incidence of about 3.7 degrees the margin is zero or negative, and that even at the design incidence ($\alpha_E = 2.6^\circ$), the margin is

* M_D has been taken here as the Mach number for which the actual drag coefficient exceeds the subcritical value (extrapolated to the same Mach number) by 0.0015.

only 0.07. This margin is smaller than would be expected on inviscid considerations; some form of boundary layer control may be required if these viscous effects persist at full scale Reynolds numbers.

6 CONCLUSIONS

Pressure distributions have been measured around the section of a 60° swept wing at Mach numbers from 0.6 to 1.4. The section was basically a 9% thick RAE 101 thickness distribution, cambered to provide an approximately triangular upper surface pressure distribution, which was subcritical almost everywhere, at a Mach number of 1.2 and a lift coefficient of 0.153 in inviscid flow. The wing was substantially untapered and had an aspect ratio near 5. Pressures were measured all round one streamwise station at 0.71 semi-span.

It is concluded that:-

- (1) A subcritical type of flow, without shocks, has been achieved at a supersonic free stream Mach number on a lifting wing, as predicted theoretically in Ref.1, without incurring any significant wave drag.
- (2) At the design Mach number of 1.2, the theoretical (inviscid) and experimental pressure distributions, compared on a basis of equal peak suction, are in good agreement wherever the pressure gradient is favourable. Elsewhere, agreement is less good, both upper and lower surfaces contributing to a loss in loading sufficient to reduce lift curve slope by around 40%. Substantial boundary layer outflow is observed which would be expected to account for much of this effect. At the design lift coefficient, a region of supercritical flow, terminated by a shock, develops well forward on the aerofoil, without causing any great increase in drag. However, the boundary layer is at this stage on the point of separating completely over the rear of the section.
- (3) As Mach number or lift coefficient is increased above the design value, there appears on the upper surface a shock which in plan view is nearly as highly swept as the wing itself. No drag penalty is evident until the shock moves aft of the crest of the aerofoil. Eventually the flow separates everywhere behind the shock. Rather small margins between the Mach numbers for drag rise and for the onset of separation effects were found but the relatively thick boundary layer may be largely responsible for this.
- (4) Some estimates of supercritical pressure distributions for two-dimensional wings have been extended to the swept wing case and compared with the experimental results. In general quite good agreement is found. The Mach number for which the shock first appears, the subsequent movement of the shock, the drag-rise Mach number and the Mach number for the onset of separation effects can all be predicted with reasonable accuracy from knowledge of the just-subcritical pressure distribution. Ahead of the shock the component of local Mach number normal to the leading edge "freezes" in an analogous manner to the two-dimensional case.
- (5) No significant variations in pressure distributions were found due to increasing Reynolds number from 5×10^6 to 6×10^6 at supersonic speeds.

Future testing will include models having design pressure distributions of roof-top shape, a thinner (6%) section, body shaping to help reduce root effects still further, and devices which are intended to reduce the effective boundary layer thickness, as well as measurements of total head distributions in the region of the trailing edge.

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LIST OF SYMBOLS

C_Z	normal force coefficient
C_X	chord force coefficient
ΔC_X	error in C_X due to tunnel flow (para.5.3)
C_L	lift coefficient
C_D	drag coefficient
C_f	skin friction drag coefficient
C_p	pressure coefficient $\frac{p - p_o}{0.7 p_o M_o^2}$
C_p^*	pressure coefficient when local Mach number component normal to leading edge is equal to unity
c	local wing chord
H	stagnation pressure
H_{eff}	stagnation pressure for equivalent unswept wing (see para.5.1)
M	Mach number
N	$\frac{\partial a_E}{\partial a_T}$ (para.5.6.1)
p	local static pressure
x, y, z	orthogonal co-ordinates defining wing surface
α	angle of incidence
γ	ratio of specific heats (taken as 1.4)
θ	surface slope of aerofoil measured forward from crest
Λ	angle of sweepback
χ	$\left(\left(\frac{z}{o} \right)_{x=0.02\alpha} \right) / \left(\Delta \frac{x}{o} \text{ between } \theta = 2^\circ \text{ and } \theta = 4^\circ \right)$ (a function of aerofoil geometry near leading edge)

LIST OF SYMBOLS (Contd)

Suffices

o	free stream conditions
1	immediately upstream of shock
2	immediately downstream of shock
2_G	used in p_{2G} to denote value of p_2 given by appropriate sub-critical pressure distribution at position of shock
CR	critical value
D	value at onset of drag rise
E	experimental value
SE	value at onset of separation effects
T	theoretical value

LIST OF REFERENCES

<u>No.</u>	<u>Author</u>	<u>Title, etc.</u>
1	Küchemann, D. Weber, J.	The subsonic flow past swept wings of zero lift without and with body. A.R.C. R. & M.2908. March, 1953.
2	Bagley, J.A.	An aerodynamic outline of a transonic transport aeroplane. A.R.C. 19,205. October, 1956.
3	Weber, J.	The calculation of the pressure distribution over the surface of two-dimensional and swept wings with symmetrical aerofoil sections. A.R.C. R. & M.2918. July, 1953.
4	Weber, J.	The calculation of the pressure distribution on the surface of thick cambered wings and the design of wings with given pressure distribution. A.R.C. R. & M.3026. June, 1955.
5	Randall, D.G.	Transonic flow over two-dimensional round-nosed aerofoils. A.R.C. C.P.456. September, 1958.
6	Sinnott, C.S.	On the flow of a sonic stream past an aerofoil surface. Journal Aero/Space Sciences, Vol.26, No.3. March, 1959.
7	Sinnott, C.S.	On the prediction of mixed, subsonic/supersonic pressure distributions. Journal Aero/Space Sciences, Vol.27, No.10. October, 1960.
8	Bagley, J.A.	Wing section design for a transonic aeroplane. Unpublished M.O.A. Report.

LIST OF REFERENCES (Contd)

<u>No.</u>	<u>Author</u>	<u>Title, etc.</u>
9	Brebner, G.G. Bagley, J.A.	Pressure and boundary layer measurements on a two dimensional wing at low speed. A.R.C. R. & M.2886. February, 1952.
10	Küchemann, D.	Boundary layers on swept wings - their effects and their measurements. AGARD Paper No. AG 19/P9. April, 1955.
11	Haines, A.B. Jones, J.C.M.	The centre line Mach number distributions and auxiliary suction requirements for the ARA 9 ft x 8 ft transonic wind tunnel. A.R.C. R. & M.3140. April, 1958.
12	O'Hara, F. Squire, L.C. Haines, A.B.	An investigation of interference effects on similar models of different size in various transonic tunnels in the U.K. A.R.C. 21,094. February, 1959.
13	Nitzberg, G.E. Crandall, S.	A study of flow changes associated with air-foil section drag rise at supercritical speeds. N.A.C.A. Tech. Note No. 1813. February, 1949.
14	Blake, M.	Results of some calculations on camber and twist distributions for swept wings at $M = 0$. Vickers Armstrongs (Aircraft) Ltd. Report No. A.570.2. September, 1959.
15	Bagley, J.A. Beasley, J.A.	The shapes and lift-dependent drags of some sweptback wings designed for $M_0 = 1.2$. A.R.C. C.P.512. June, 1959.
16	Tunnel Staff of Aero Dept.	Pressure and boundary layer measurements on a 59° sweptback wing at low speed and comparison with high speed results on a 45° swept wing. A.R.C. C.P.86. August, 1950.
17	Monaghan, R.J.	A review and assessment of various formulae for turbulent skin friction in compressible flow. A.R.C. C.P.142. August, 1952.
18	Sinnott, C.S.	Theoretical prediction of the transonic characteristics of aerofoils. Report No. NPL/Aero/369. January, 1959.
19	Pearcey, H.H.	Some effects of shock induced separation of turbulent boundary layers in transonic flow past aerofoils. Proc. Symposium on boundary layer effects in aerodynamics. A.R.C. R. & M.3108. June, 1955.
20	Sinnott, C.S.	The design of two dimensional cambered aero-foil sections for the supersonic transport project. Report No. NPL/Aero/332. July, 1957.
21	Monaghan, R.J.	Formulae and approximations for aerodynamic heating rates in high speed flight. A.R.C. C.P.360. October, 1955.

APPENDIX 1

RELATION BETWEEN PRESSURE AND MACH NUMBER COMPONENT NORMAL
TO THE LEADING EDGE OF A SWEEPED WING

In the case of two-dimensional wings, it is sometimes convenient to express pressures around the wing section in the form p/H_o , where H_o is the stagnation pressure. For swept wings of infinite span, there is an analogous expression for pressure which may be written p/H_{eff} , where H_{eff} is defined as the pressure at the attachment line, i.e., the line where the local component of flow normal to the leading edge is zero. Thus the value of p/H_o for an unswept wing will be the same as the value of p/H_{eff} for the same wing yawed through an angle Λ , if the free stream Mach number is increased by a factor equal to the secant of the angle of yaw.

Let V = velocity
 a = velocity of sound
 M = Mach number $\left(\frac{V}{a}\right)$
 Λ = sweepback angle
 γ = ratio of specific heats for air
 p = static pressure
 H = stagnation pressure

Suffix o = free stream conditions
 n = normal to wing leading edge
 t = parallel to wing leading edge.

We assume that the velocity component parallel to the leading edge is constant, i.e.

$$V_t = V_o \sin \Lambda = \text{constant} .$$

We express the value of p/H_o in the two following ways:-

$$\frac{p}{H_o} = \left(1 + \frac{\gamma - 1}{2} M^2\right)^{\frac{\gamma}{1-\gamma}} \quad (1)$$

$$\frac{p}{H_o} = \left(1 + \frac{\gamma - 1}{2} \left(\frac{V}{a_o}\right)^2\right)^{\frac{\gamma}{\gamma-1}} . \quad (2)$$

Now

$$\left(\frac{V_o}{a_o}\right)^2 = \frac{M_o^2}{1 + \frac{\gamma-1}{2} M_o^2}, \quad \text{so that, when } V_n = 0$$

$$\begin{aligned} \frac{p}{H_o} &= \frac{H_{\text{eff}}}{H_o} \\ &= \left\{ 1 - \frac{\gamma-1}{2} \left(\frac{V_t}{a_o}\right)^2 \right\}^{\frac{\gamma}{\gamma-1}}. \end{aligned}$$

But

$$\begin{aligned} \left(\frac{V_t}{a_o}\right)^2 &= \frac{M_o^2 \sin^2 \Lambda}{1 + \frac{\gamma-1}{2} M_o^2}, \quad \text{whence} \\ \frac{H_{\text{eff}}}{H_o} &= \left\{ \frac{1 + \frac{\gamma-1}{2} M_o^2 \cos^2 \Lambda}{1 + \frac{\gamma-1}{2} M_o^2} \right\}^{\frac{\gamma}{\gamma-1}}. \end{aligned} \quad (3)$$

$$\frac{p}{H_{\text{eff}}} = \frac{p}{H_o} \cdot \frac{H_o}{H_{\text{eff}}}$$

so that, from (1) and (3)

$$\frac{p}{H_{\text{eff}}} = \left(1 + \frac{\gamma-1}{2} M^2 \cos^2 \Lambda \right)^{\frac{\gamma}{1-\gamma}} \quad (4)$$

which is the isentropic relation with an "effective" stagnation pressure.

APPENDIX 2

DESIGN OF AEROFOIL SECTIONS WITH LINEARLY VARYING PRESSURE DISTRIBUTION ON THE UPPER SURFACE

by

J. Weber, Dr.rer.nat.

The task is to design for infinite sheared wings with given thickness distribution a camber line such that the wing has at the design incidence a given lift coefficient and on its upper surface a pressure distribution which varies nearly linearly along the chord (no requirement is made for the lower surface). It is required that these conditions are satisfied at a given Mach number for which the flow is subcritical. The latter condition imposes certain limits on the thickness of the wing and on the design lift coefficient.

In designing the wing which has been the subject of these tests, we have relaxed these conditions somewhat by allowing the velocity to be slightly supersonic forward of the crest but have performed the calculations as if the flow were subcritical throughout.

The symbols are defined as follows:-

A	see equation (2)
C_{p_i}	pressure coefficient as defined in equation (3)
h	see equation (6)
M	Mach number
$S^{(n)}(x)$	functions given in Refs.2 and 3
V	velocity
x	distance aft of leading edge (in units of wing chord)
z	distance above chord line (in units of wing chord)
z_o	ordinate of camber line of section
z_t	ordinate of thickness distribution of section
α	angle of incidence
$\Gamma(x)$	load distribution
γ	ratio of specific heats (taken as 1.4)
Λ	angle of sweep

Suffices:-

o	free stream conditions
D	design
n	component normal to leading edge
us	upper surface
μ, ν	as defined in Ref.3

The pressure distribution on an infinite sheared wing in subcritical flow can be calculated from the following equation:-

$$\left(\frac{V}{V_0}\right)^2 = \cos^2 \alpha \sin^2 \Lambda + \frac{1}{1 + \left[\frac{S^{(2)}(x) \pm S^{(5)}(x)}{A \cos \Lambda}\right]^2}$$

$$\times \left\{ \cos \alpha \left[\cos \Lambda + \frac{S^{(1)}(x)}{A} \pm \frac{S^{(4)}(x)}{\sqrt{1 - M_0^2 \cos^2 \Lambda}} \right] \right.$$

$$\left. \pm \frac{\sin \alpha}{\sqrt{1 - M_0^2 \cos^2 \Lambda}} \sqrt{\frac{1-x}{x}} \left[1 + \frac{S^{(3)}(x)}{A \cos \Lambda} \right] \right\}^2 \quad (1)$$

where

$$A = \sqrt{1 - M_0^2 (\cos^2 \Lambda - C_{pi})} \quad (2)$$

and

$$C_{pi} = \cos^2 \Lambda - \frac{\{\cos \Lambda + S^{(1)}(x)\}^2}{1 + \left[\frac{S^{(2)}(x)}{\cos \Lambda}\right]^2} \quad (3)$$

$S^{(1)}(x)$, $S^{(2)}(x)$ and $S^{(3)}(x)$ are functions of the ordinates $z_t(x)$ of the thickness distribution and $S^{(4)}(x)$ and $S^{(5)}(x)$ are functions of the ordinates $z_o(x)$ of the camber line. The relations between $S^{(v)}(x)$ and $z_t(x)$ and $z_o(x)$ are given in Refs. 2 and 3.

The pressure coefficient is determined from the velocity distribution by the relation:-

$$C_p = \frac{2}{\gamma M_0^2} \left(\left(1 + \frac{\gamma-1}{2} M_0^2 \left[1 - \left(\frac{V}{V_0}\right)^2 \right] \right)^{\frac{\gamma}{\gamma-1}} - 1 \right) \quad (4)$$

The local Mach number M_n of the velocity component normal to the isobars is related to the pressure coefficient by the equation:-

$$C_p(M_n, M_o, \Lambda) = \frac{2}{\gamma M_o^2} \left\{ \left[\frac{2}{2 + (\gamma - 1) M_n^2} \right]^{\frac{\gamma}{\gamma - 1}} \left[1 + \frac{\gamma - 1}{2} M_o^2 \cos^2 \Lambda \right]^{\frac{\gamma}{\gamma - 1}} - 1 \right\} \dots (5)$$

For the present test programme, aerofoil sections were required for wings of 60° sweep which had a design lift coefficient of 0.15 and which satisfied the conditions mentioned above at a free stream Mach number of 1.2. The further condition was imposed that the difference between the upper and lower surface pressures tends to zero at the trailing edge.

Thickness distributions of the type RAE 100 and RAE 101 were considered. According to linear theory, these sections have at zero incidence pressure distributions of the form

$$C_{P_t}(x) = \begin{cases} A & 0 < x < h \\ A + B(x - h) & h < x < 1 \end{cases} \dots (6)$$

($h = 0$ for RAE 100, $h = 0.3$ for RAE 101). A linear pressure distribution on the upper surface

$$C_p(x) = A + B(1 - h) + C(1 - x)$$

is obtained according to linear theory if the load distribution is

$$C_{P_{US}} - C_{P_{LS}} = \begin{cases} 2B(1 - h) + 2C(1 - x) & 0 < x < h \\ 2(B + C)(1 - x) & h < x < 1 \end{cases} \dots (7)$$

If we consider these first order terms only, then we find that a wing thickness of 9% is possible. This implies that the wing section normal to the leading edge is 18% thick and that therefore the second-order terms in equation (1) have a significant effect on the pressure distribution.

To determine the required camber-line, we need to know the linear order term of the chordwise load distribution in incompressible flow:-

$$\frac{\Gamma(x)}{2 V_o} = S^{(4)}(x) + \tan \alpha_D \sqrt{\frac{1 - x}{x}} \dots (8)$$

where α_D is the design incidence. The relation between the shape of the camber-line, z_o , and the load distribution is:-

$$\frac{dz_o(x)}{dx} - \tan \alpha_D = -\frac{1}{\pi} \int_0^1 \frac{\Gamma(x')}{2V_o} \frac{dx'}{x-x'}$$

This relation can be approximated by:-

$$\frac{dz_o(x)}{dx} - \tan \alpha_D = \sum_{\mu=1}^{N-1} S_{\mu\nu}^{(22)} \frac{\Gamma_{\mu}}{2V_o} + S_{N\nu}^{(22)} \lim_{x \rightarrow 0} \frac{\Gamma(x)}{2V_o} \sqrt{x}; \quad (9)$$

the coefficients $S_{\mu\nu}^{(22)}$ are tabulated in Ref.3.

In view of the relatively large second order terms in equation (1), we have not attempted to obtain a first approximation to $\Gamma(x)$ from the linear order terms given in equations (6) and (7). Instead, we have estimated an upper surface pressure distribution and have determined an approximation to $\Gamma(x)$ from:-

$$\begin{aligned} \frac{\Gamma(x)}{2V_o} &= S^{(4)}(x) + \tan \alpha_D \sqrt{\frac{1-x}{x}} \\ &= - \left[C_{PUS} - C_P(\alpha = 0, z_o = 0) \right] \sqrt{1 - M_o^2 \cos^2 \Lambda} \frac{1 + \left[\frac{S^{(2)}(x)}{A \cos \Lambda} \right]^2}{2 \left[\cos \Lambda + \frac{S^{(1)}(x)}{A} \right]} \\ &\dots (10) \end{aligned}$$

where $C_P(\alpha = 0, z_o = 0)$ is the pressure coefficient of the uncambered section at zero lift.

With the $\Gamma(x)$ of equation (10) the slope of the skeleton line was determined by equation (9). By graphical integration of the slopes the incidence α_D and the ordinates of the camber-line were found. Then the pressure distribution can be determined from equations (1), (2) and (3), taking account of all higher order terms. If a modification to the resulting pressure distribution is then required, the procedure is to estimate the required alteration of the camber-line and of the incidence and

determine $S^{(4)}(x)$ and $S^{(5)}(x)$ and $C_p(x)$. This procedure does not, of course, lead to explicit expressions for the load distribution and the camber line.

The results of the calculations are shown in Figs.2 and 4, which show the surface pressure distributions, and the shape of the camber line respectively. The required pressure distribution has been substantially achieved, except over the first 10% of the chord.

TABLE 1

Ordinates of aerofoil at 32 pivotal points

(from inspection of model)

$\frac{x}{c}$	$\frac{z}{c}$ upper	$\frac{z}{c}$ lower
1.0000	0	0
0.9976	0	0
0.9904	0.00078	0.00085
0.9785	0.00181	0.00185
0.9619	0.00333	0.00317
0.9410	0.00521	0.00484
0.9157	0.00763	0.00689
0.8865	0.01033	0.00926
0.8536	0.01320	0.01189
0.8172	0.01621	0.01480
0.7778	0.01946	0.01799
0.7357	0.02288	0.02134
0.6913	0.02598	0.02488
0.6451	0.02915	0.02852
0.5975	0.03213	0.03231
0.5490	0.03457	0.03621
0.5000	0.03668	0.04010
0.4510	0.03789	0.04386
0.4025	0.03879	0.04712
0.3549	0.03925	0.04954
0.3087	0.03908	0.05050
0.2643	0.03852	0.04979
0.2222	0.03748	0.04766
0.1828	0.03571	0.04474
0.1464	0.03338	0.04112
0.1135	0.03058	0.03693
0.0843	0.02704	0.03226
0.0590	0.02300	0.02741
0.0381	0.01850	0.02233
0.0215	0.01402	0.01718
0.0096	0.00892	0.01190
0.0024	0.00379	0.00575
0	0	0

TABLE 2

Ordinates of pressure holes

Upper Surface		Lower Surface	
$\frac{x}{c}$	$\frac{z}{c}$	$\frac{x}{c}$	$\frac{z}{c}$
0	0	0	0
0.0044	0.00558	0.0034	0.00743
0.0101	0.00923	0.0115	0.01290
0.0197	0.01332	0.0184	0.01607
0.0300	0.01653		
0.0399	0.01904	0.0408	0.02307
0.0598	0.02333	0.0618	0.02796
0.0803	0.02625	0.0819	0.03183
0.1005	0.02900	0.1016	0.03518
0.1502	0.03367	0.1516	0.04168
0.2003	0.03650	0.2016	0.04625
0.2499	0.03818	0.2516	0.04926
0.2998	0.03896	0.3016	0.05050
0.3498	0.03925	0.3516	0.04968
0.4000	0.03896	0.4016	0.04714
0.4498	0.03803	0.4507	0.04390
0.4997	0.03673	0.5012	0.03999
0.5496	0.03454	0.5510	0.03606
0.5997	0.03191	0.6012	0.03202
0.6498	0.02887	0.6514	0.02807
0.6998	0.02541	0.7012	0.02409
0.7503	0.02182	0.7514	0.02010
0.7999	0.01779	0.8018	0.01601
0.8503	0.01358	0.8515	0.01202
0.9003	0.00895	0.9010	0.00809
0.9493	0.00457		

TABLE 4 - Values of \overline{C}_Z and \overline{C}_X

(a) Stagnation pressure 30 in. mercury

α_E	M	\overline{C}_Z	\overline{C}_X	α_E	M	\overline{C}_Z	\overline{C}_X
0.0	0.609	- 0.027	+ 0.011	2.6	0.982	+ 0.084	- 0.030
	0.803	- 0.028	+ 0.015		1.022	+ 0.085	- 0.011
	0.855	- 0.028	+ 0.015		1.064	+ 0.085	- 0.009
	0.904	- 0.030	+ 0.014		1.103	+ 0.086	- 0.024
	0.943	- 0.030	+ 0.012		1.143	+ 0.087	- 0.029
	0.983	- 0.030	+ 0.006		1.194	+ 0.086	- 0.015
	1.026	- 0.028	+ 0.040		1.216	+ 0.081	- 0.027
	1.063	- 0.030	+ 0.022		1.226	+ 0.087	- 0.020
	1.107	- 0.029	+ 0.003		1.252	+ 0.089	- 0.031
	1.145	- 0.029	+ 0.008		1.302	+ 0.085	- 0.012
	1.193	- 0.029	+ 0.016		1.355	+ 0.091	- 0.000
1.253	- 0.028	+ 0.010	1.405	+ 0.101	+ 0.034		
1.304	- 0.026	+ 0.019					
1.356	- 0.024	+ 0.011					
1.408	- 0.037	+ 0.040					
2.0	0.601	+ 0.060	- 0.002	3.0	0.600	+ 0.100	- 0.027
	0.797	+ 0.060	+ 0.000		0.803	+ 0.100	- 0.024
	0.850	+ 0.059	+ 0.003		0.848	+ 0.100	- 0.023
	0.900	+ 0.059	+ 0.001		0.901	+ 0.098	- 0.023
	0.941	+ 0.058	+ 0.003		0.942	+ 0.098	- 0.028
	0.979	+ 0.059	- 0.003		0.979	+ 0.099	- 0.034
	1.020	+ 0.060	- 0.006		1.023	+ 0.100	- 0.023
	1.062	+ 0.061	+ 0.025		1.064	+ 0.101	- 0.036
	1.101	+ 0.061	+ 0.010		1.105	+ 0.104	- 0.040
	1.142	+ 0.061	+ 0.014		1.145	+ 0.103	- 0.033
	1.190	+ 0.060	+ 0.003		1.195	+ 0.104	- 0.036
1.252	+ 0.060	+ 0.013	1.213	+ 0.101	- 0.038		
1.306	+ 0.057	+ 0.004	1.244	+ 0.104	- 0.015		
1.355	+ 0.058	+ 0.002	1.302	+ 0.105	- 0.007		
1.409	+ 0.055	+ 0.002	1.328	+ 0.106	- 0.013		
	+ 0.058	+ 0.002	1.352	+ 0.122	- 0.007		
	+ 0.055	+ 0.002	1.407	+ 0.125	+ 0.050		

TABLE 4 - Values of \overline{C}_Z and \overline{C}_X

(b) Stagnation pressure 36 in. mercury

α_E	M	\overline{C}_Z	\overline{C}_X
4.0	0.596	+ 0.139	- 0.066
	0.797	+ 0.136	- 0.062
	0.847	+ 0.139	- 0.063
	0.903	+ 0.139	- 0.065
	0.941	+ 0.138	- 0.066
	0.981	+ 0.138	- 0.075
	1.023	+ 0.138	- 0.036
	1.062	+ 0.141	- 0.061
	1.101	+ 0.145	- 0.074
	1.145	+ 0.150	- 0.078
	1.196	+ 0.166	- 0.048
1.251	+ 0.198	- 0.015	
1.301	+ 0.204	+ 0.013	
1.357	+ 0.193	+ 0.044	
1.403	+ 0.169	+ 0.066	
5.0	0.605	+ 0.166	- 0.102
	0.795	+ 0.166	- 0.102
	0.848	+ 0.167	- 0.103
	0.904	+ 0.163	- 0.105
	0.944	+ 0.164	- 0.101
	0.983	+ 0.177	- 0.112
	1.022	+ 0.177	- 0.067
	1.062	+ 0.183	- 0.086
	1.105	+ 0.182	- 0.087
	1.143	+ 0.190	- 0.063
	1.185	+ 0.216	- 0.001
1.252	+ 0.224	+ 0.008	
1.308	+ 0.225	+ 0.037	
1.357	+ 0.206	+ 0.059	
1.403	+ 0.195	+ 0.085	
2.6	0.598	+ 0.088	- 0.016
	0.797	+ 0.087	- 0.013
	0.851	+ 0.085	- 0.010
	0.896	+ 0.084	- 0.011
	0.938	+ 0.084	- 0.015
	0.976	+ 0.085	- 0.020
	1.022	+ 0.084	- 0.015
	1.063	+ 0.084	- 0.008
	1.103	+ 0.086	- 0.023
	1.144	+ 0.089	- 0.027
	1.192	+ 0.086	- 0.013
1.215	+ 0.089	- 0.022	
1.226	+ 0.087	- 0.018	
1.250	+ 0.090	- 0.028	
1.303	+ 0.087	- 0.012	
1.355	+ 0.090	- 0.000	

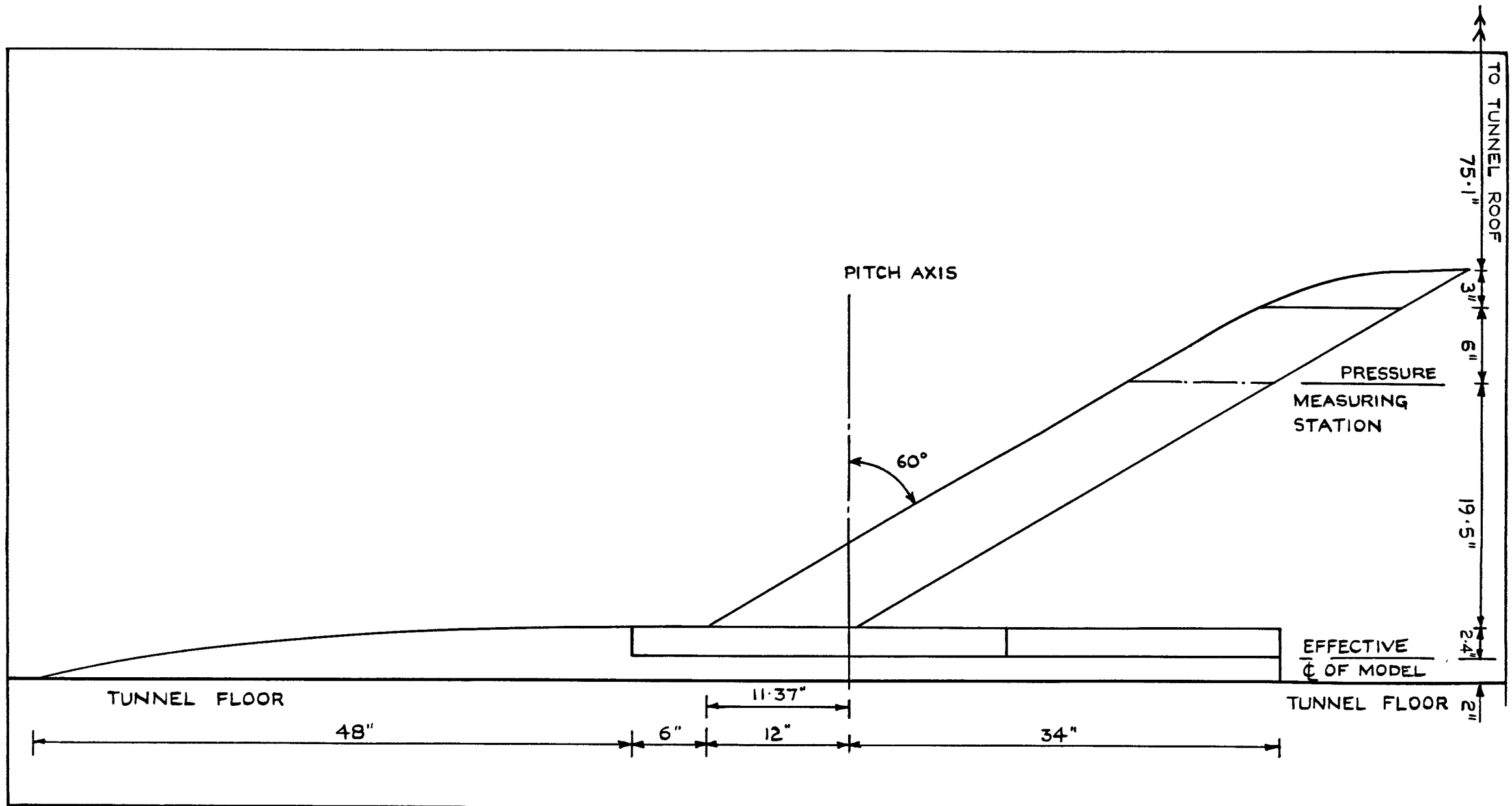


FIG.I. LAYOUT OF MODEL.

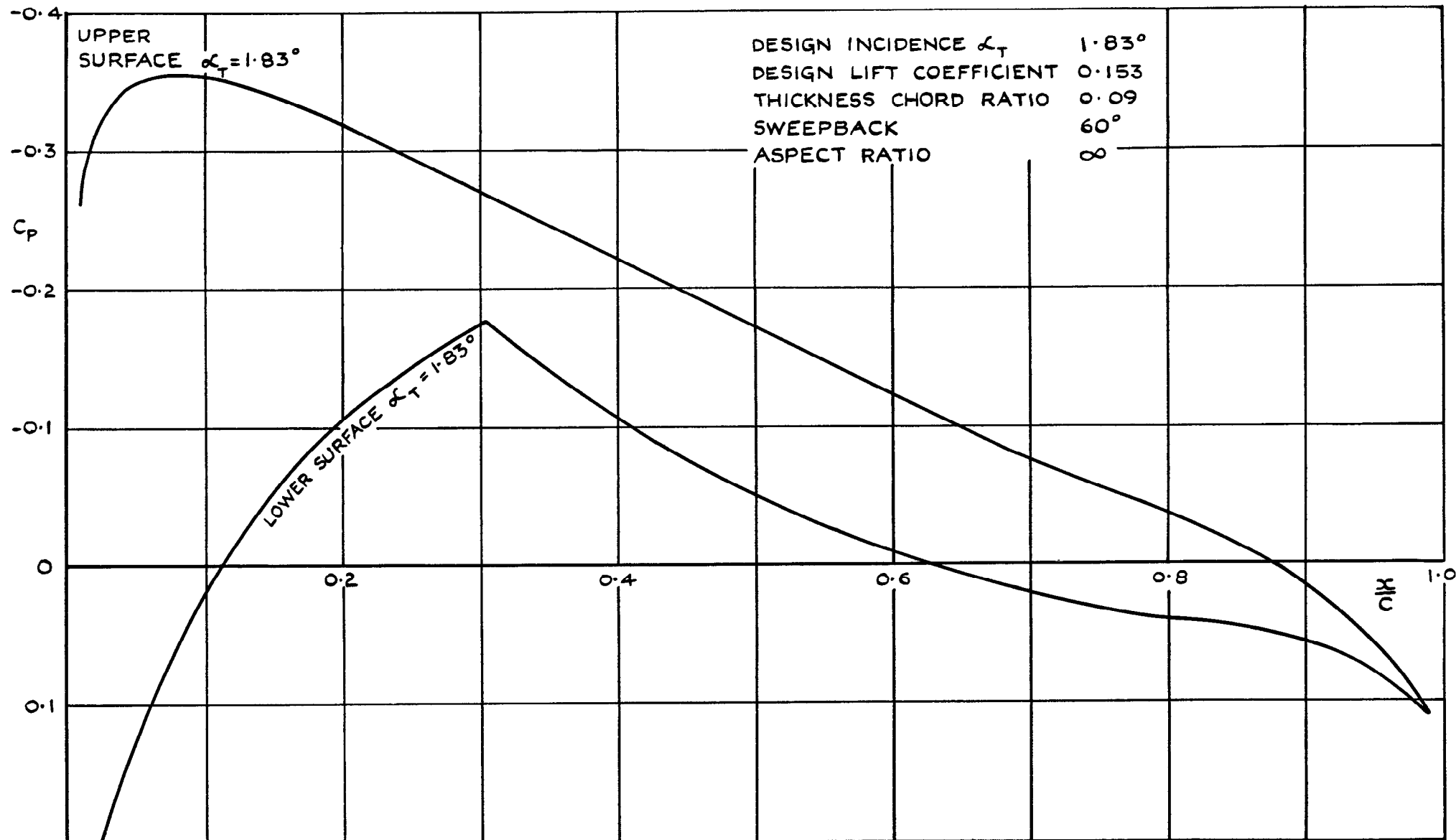


FIG.2. CALCULATED INVISCID SUBCRITICAL PRESSURE DISTRIBUTIONS AROUND AEROFOIL AT $M_0 = 1.2$.

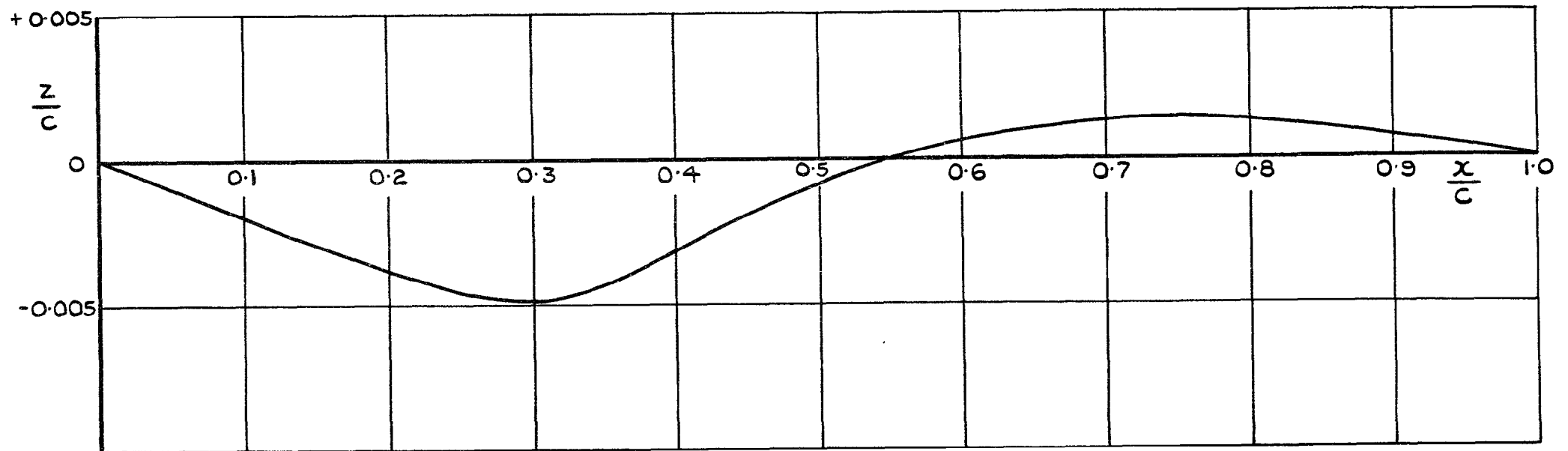


FIG. 3. CAMBER LINE (ALONG WIND) FOR AEROFOIL.

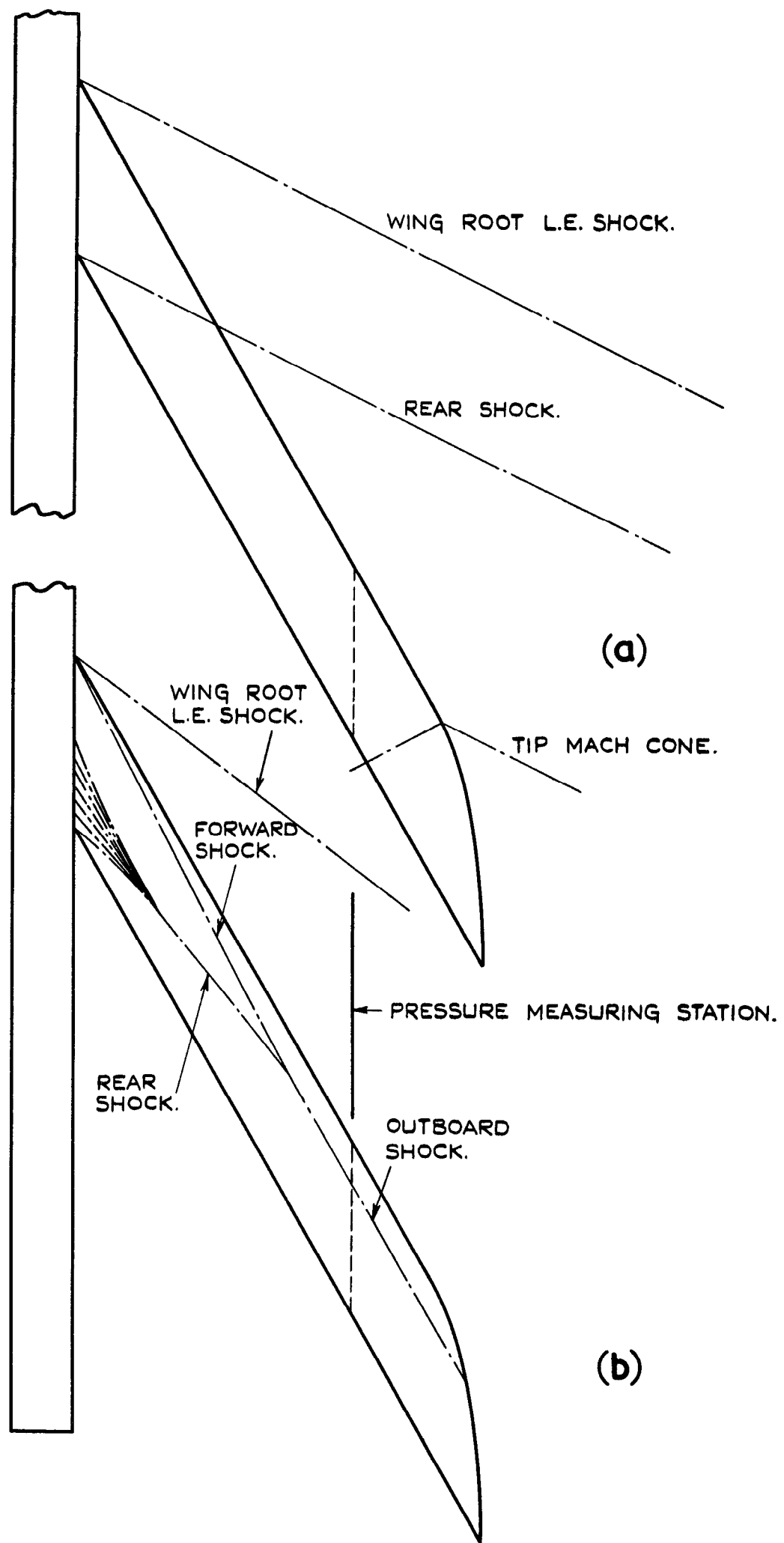


FIG. 4. SKETCH OF POSSIBLE SHOCK PATTERNS FROM ROOT WHEN FLOW AT PRESSURE MEASURING STATION IS (a) SUBCRITICAL AND (b) SUPERCRITICAL.

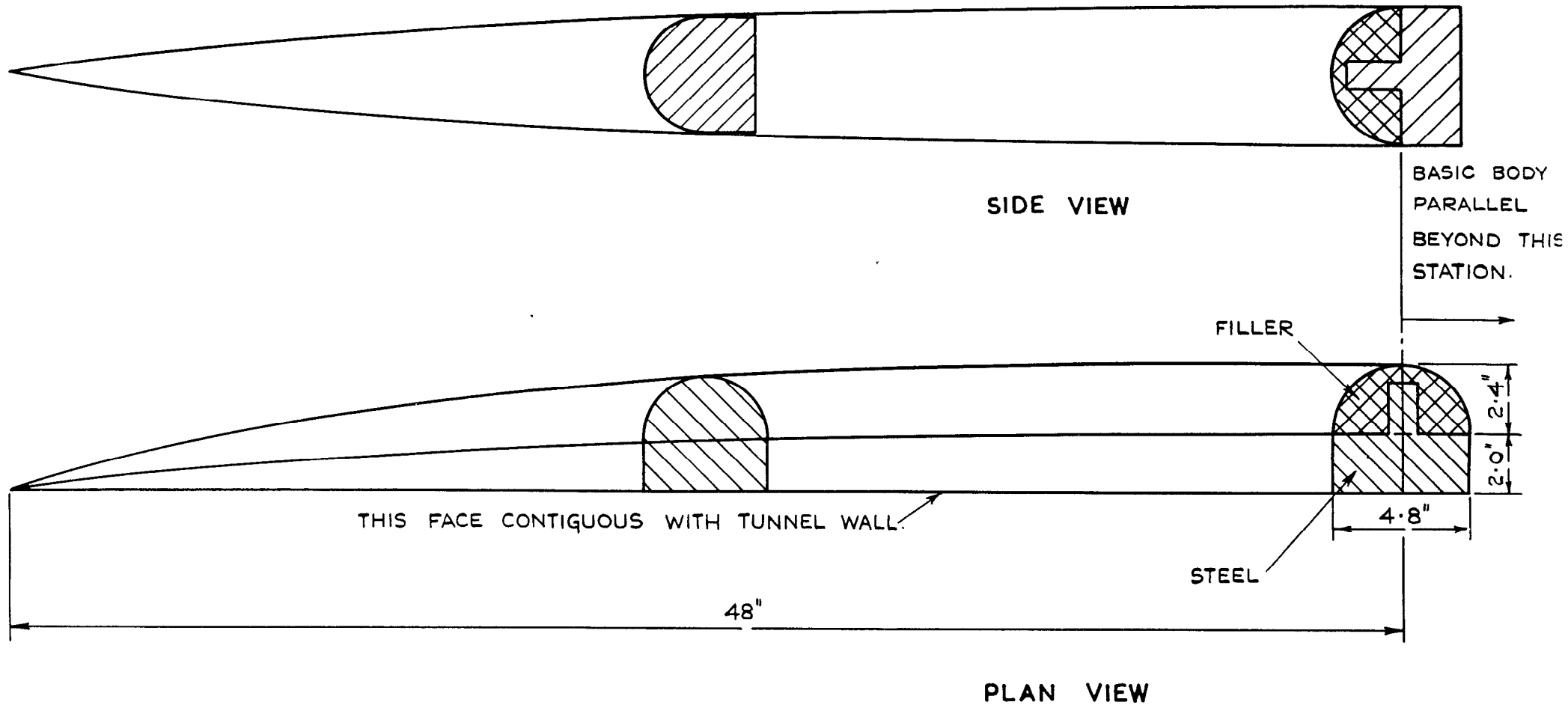


FIG. 5. VIEWS OF NOSE OF BODY SHOWING SECTION SHAPE.

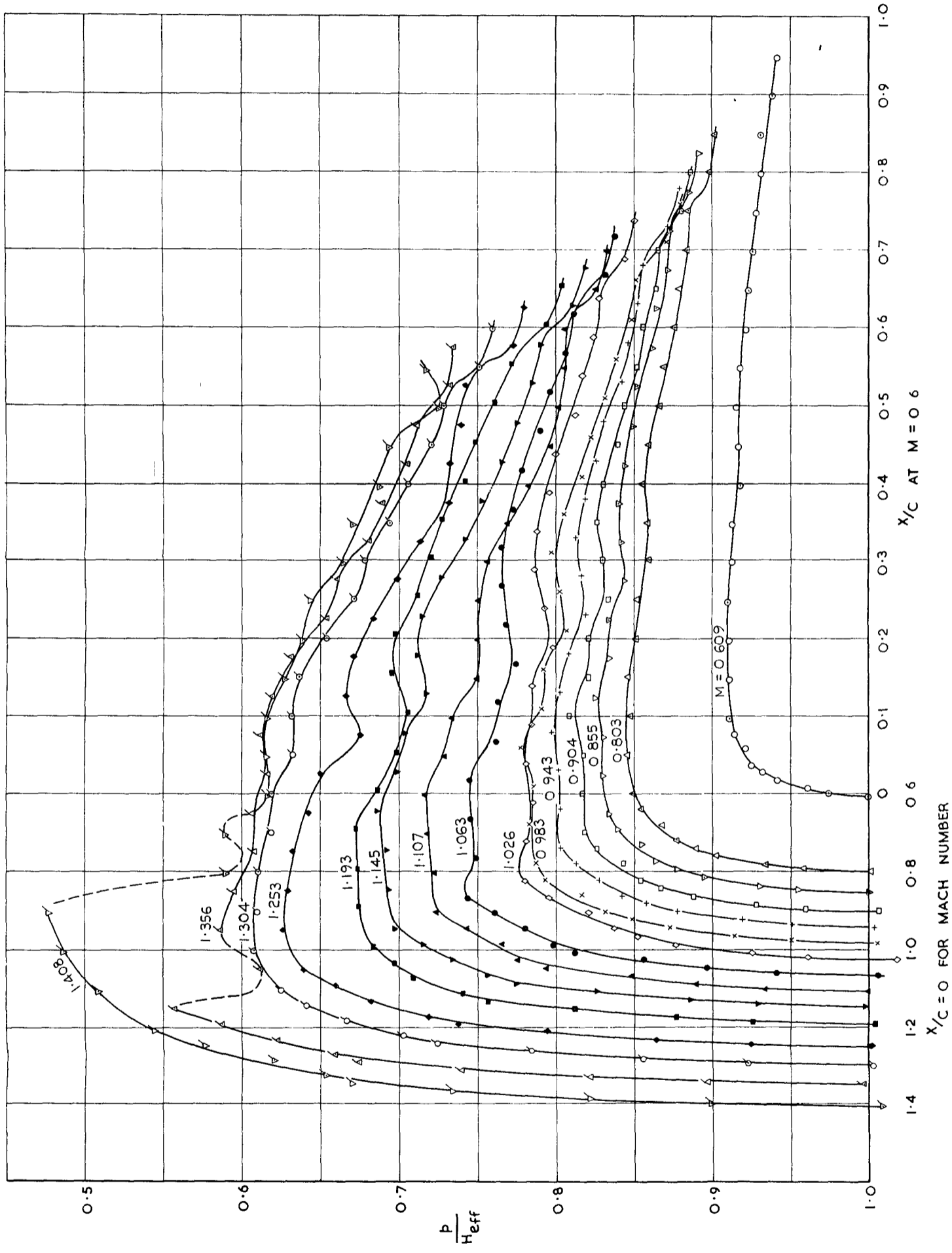


FIG. 6. UPPER SURFACE PRESSURE DISTRIBUTIONS AT VARIOUS MACH NUMBERS.
 $\alpha_E = 0^\circ$; STAGNATION PRESSURE 30 INS. MERCURY.

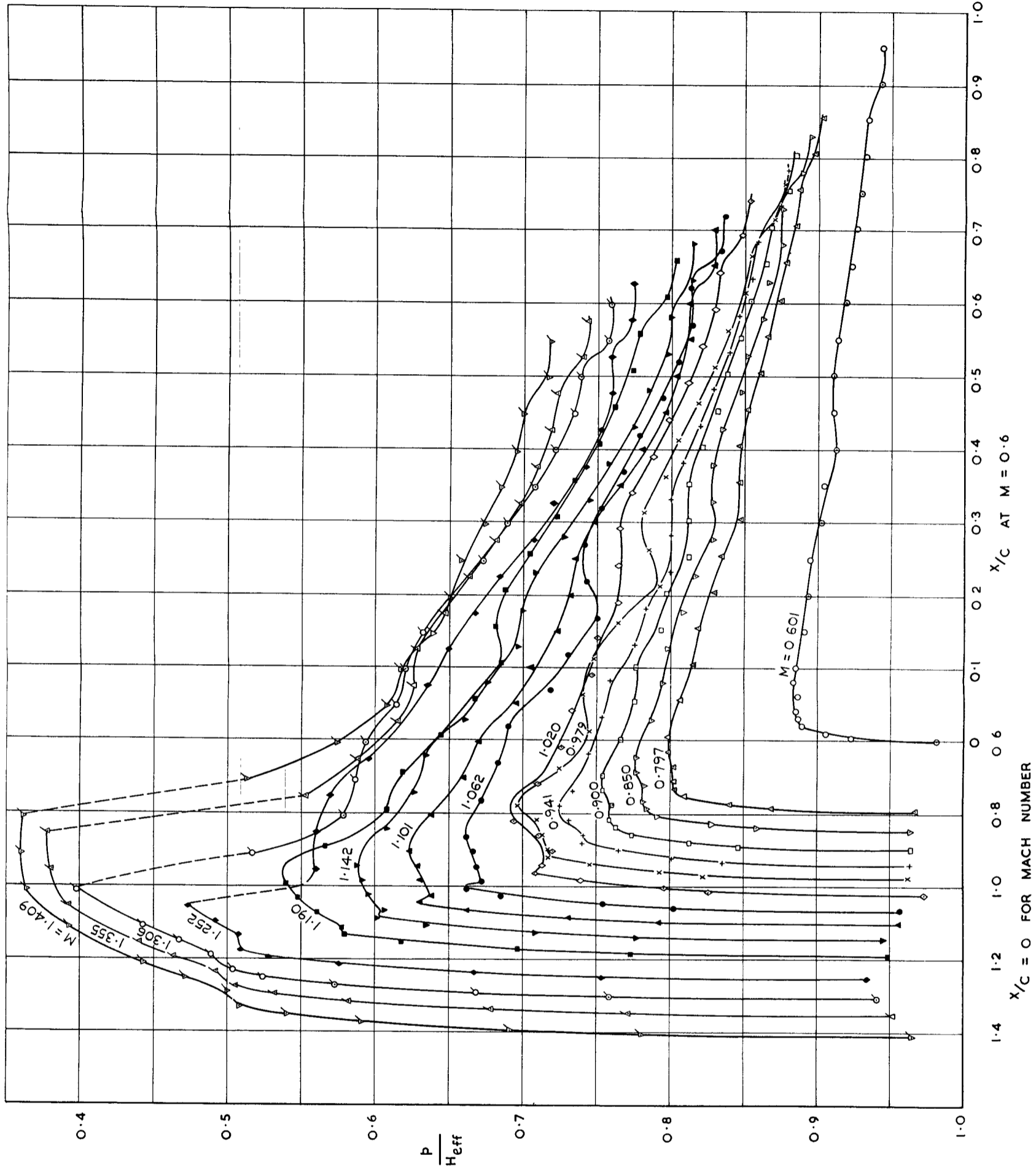


FIG. 7. UPPER SURFACE PRESSURE DISTRIBUTIONS AT VARIOUS MACH NUMBERS.
 $\alpha_E = 2.0^\circ$; STAGNATION PRESSURE 30 INS. MERCURY.

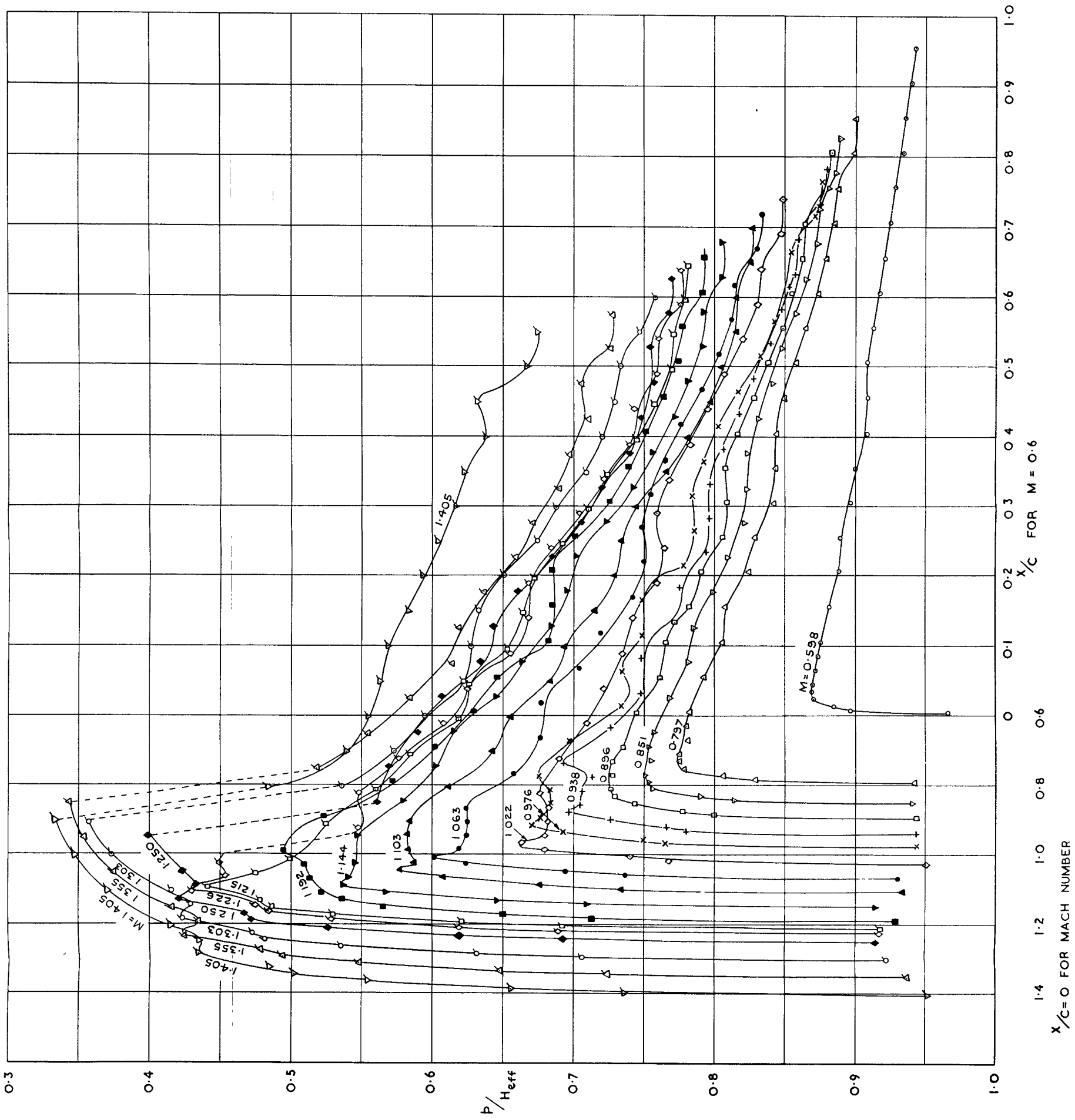


FIG. 8. UPPER SURFACE PRESSURE DISTRIBUTIONS AT VARIOUS MACH NUMBERS
 $\alpha_E = 2.6^\circ$; STAGNATION PRESSURE 36 INS. MERCURY. (30 INCS. FOR $M = 1.405$).

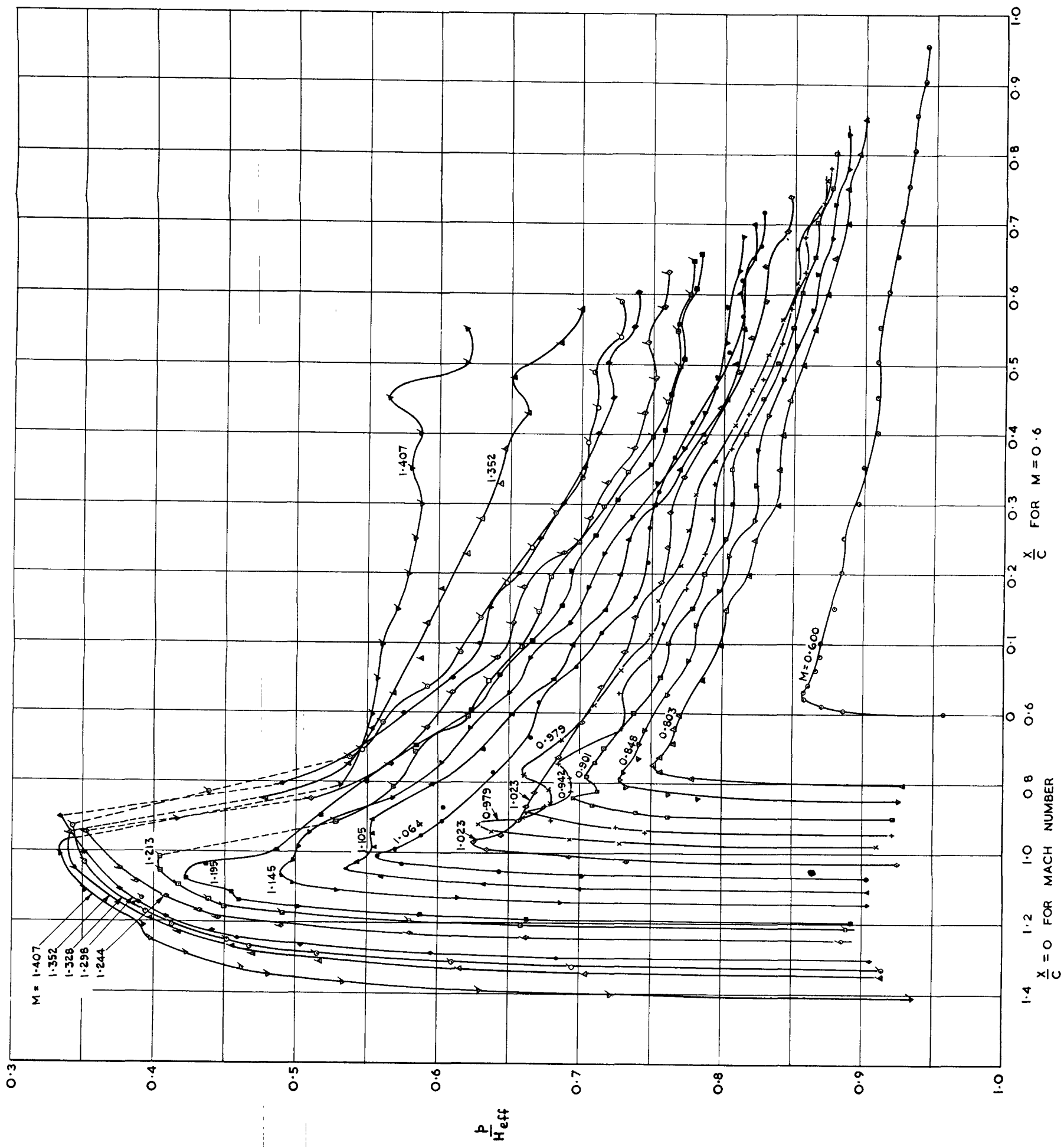


FIG. 9. UPPER SURFACE PRESSURE DISTRIBUTIONS AT VARIOUS MACH NUMBERS.
 $\alpha_E = 3.0^\circ$; STAGNATION PRESSURE 30 INS. MERCURY.

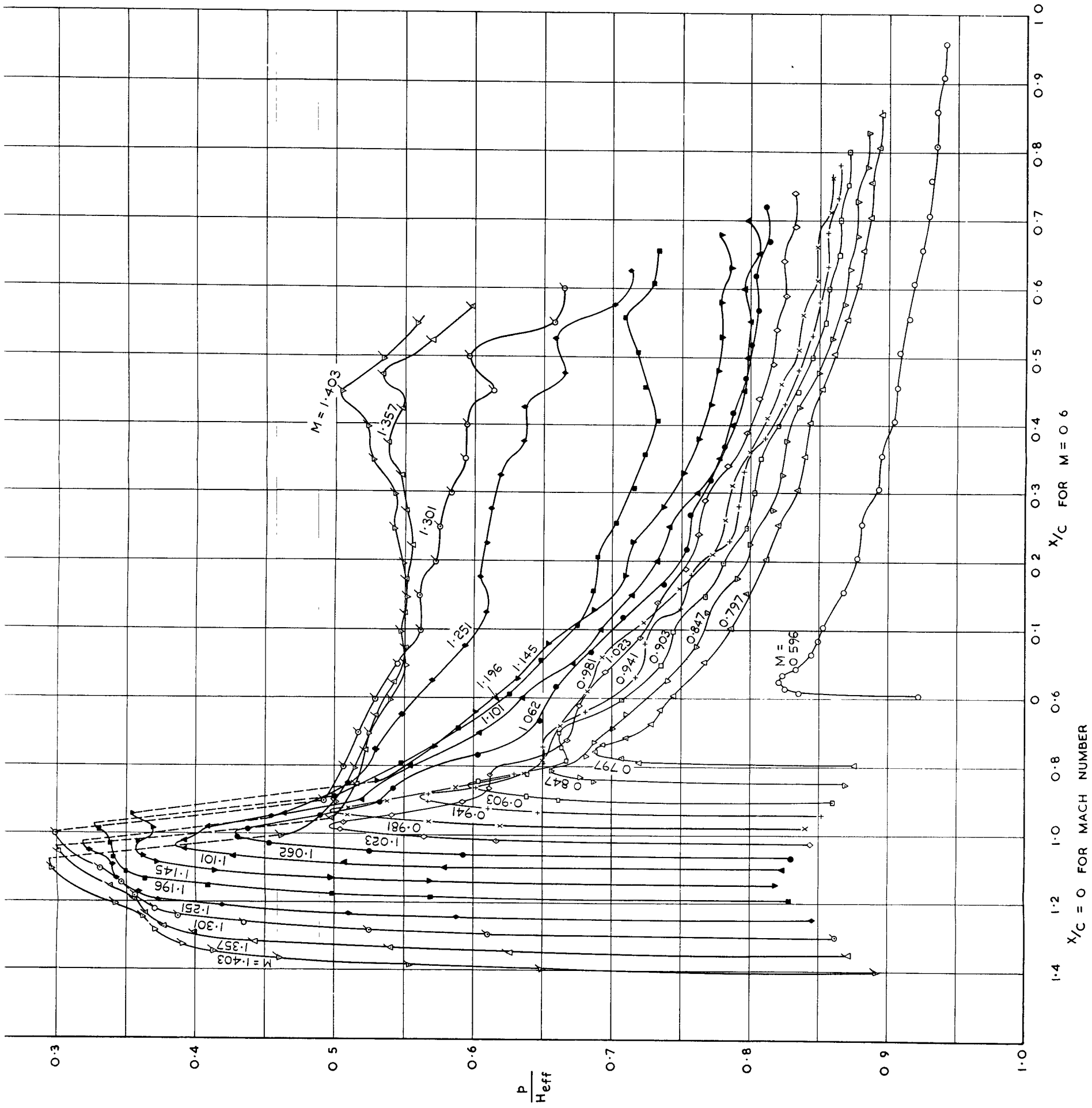


FIG. 10. UPPER SURFACE PRESSURE DISTRIBUTIONS AT VARIOUS MACH NUMBERS.
 $\alpha_E = 4.0^\circ$; STAGNATION PRESSURE 30 INS. MERCURY.

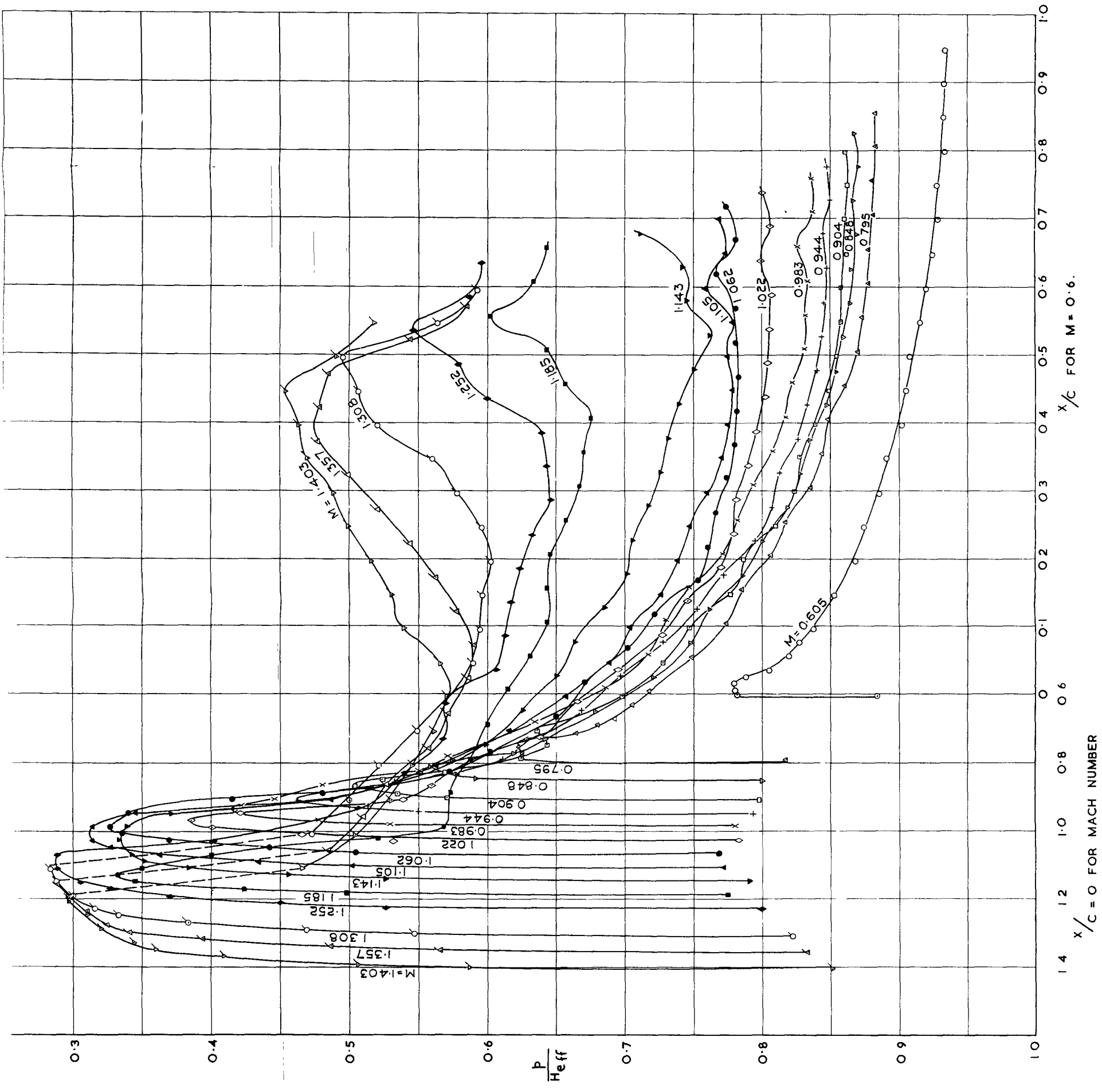


FIG. 11. UPPER SURFACE PRESSURE DISTRIBUTIONS AT VARIOUS MACH NUMBERS.
 $\alpha_E = 5.0^\circ$; STAGNATION PRESSURE 30 INS. MERCURY.

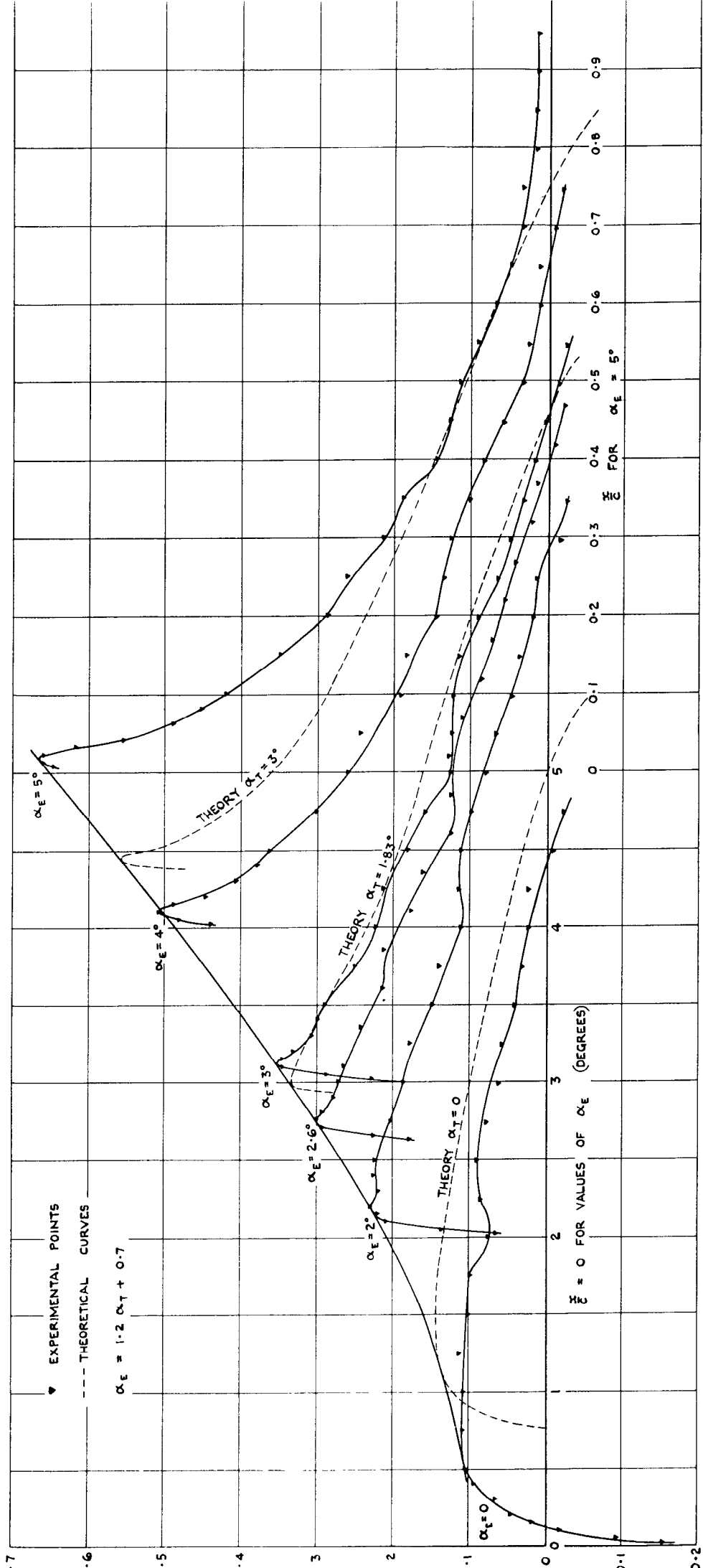


FIG.12 CARPET PLOT OF C_p vs. α_E AND α_E , UPPER SURFACE, $M_0 \doteq 0.6$

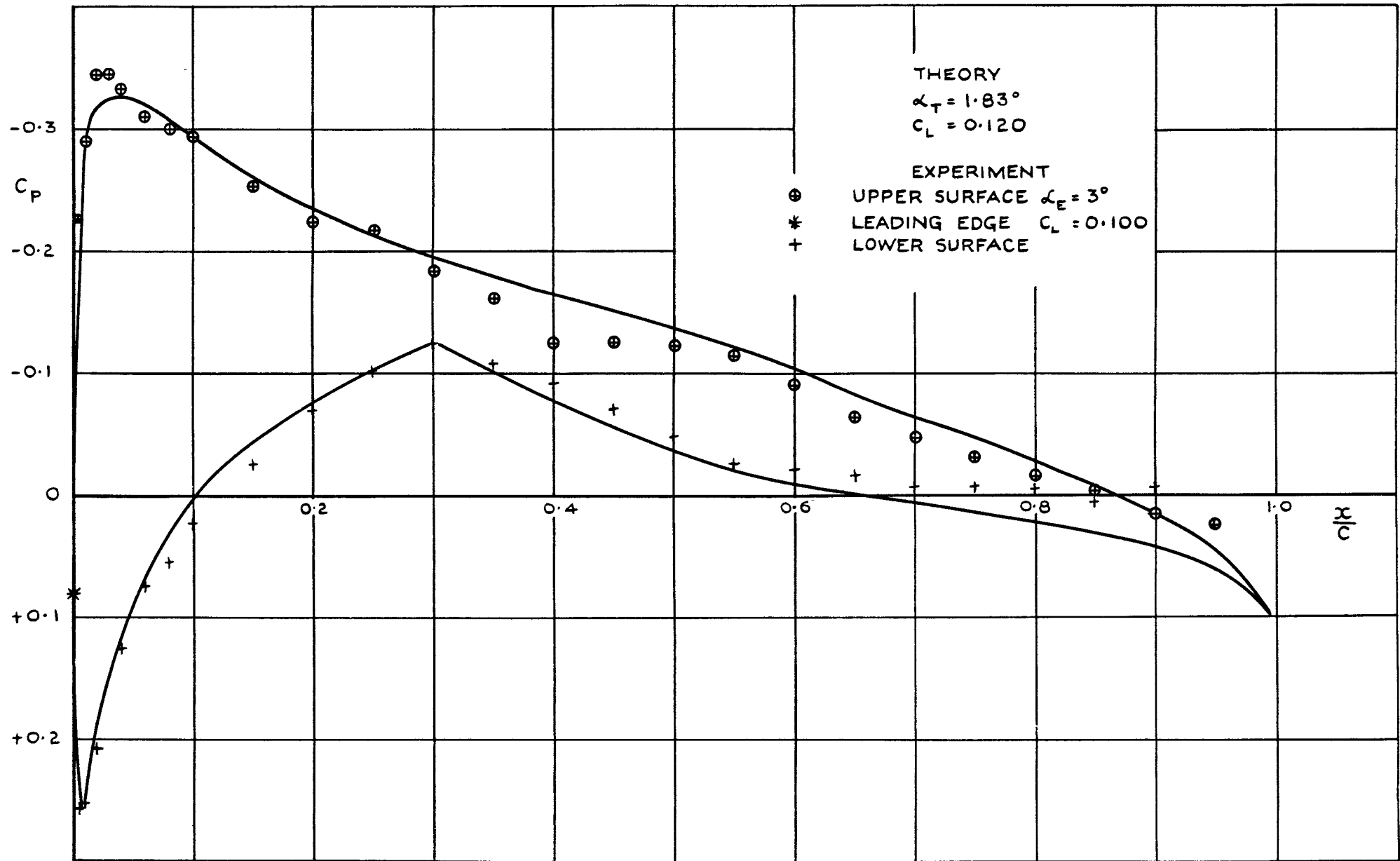


FIG. 13. COMPARISON OF THEORETICAL AND EXPERIMENTAL PRESSURE DISTRIBUTIONS AT SIMILAR VALUES OF PEAK SUCTION, $M_0 = 0.600$.

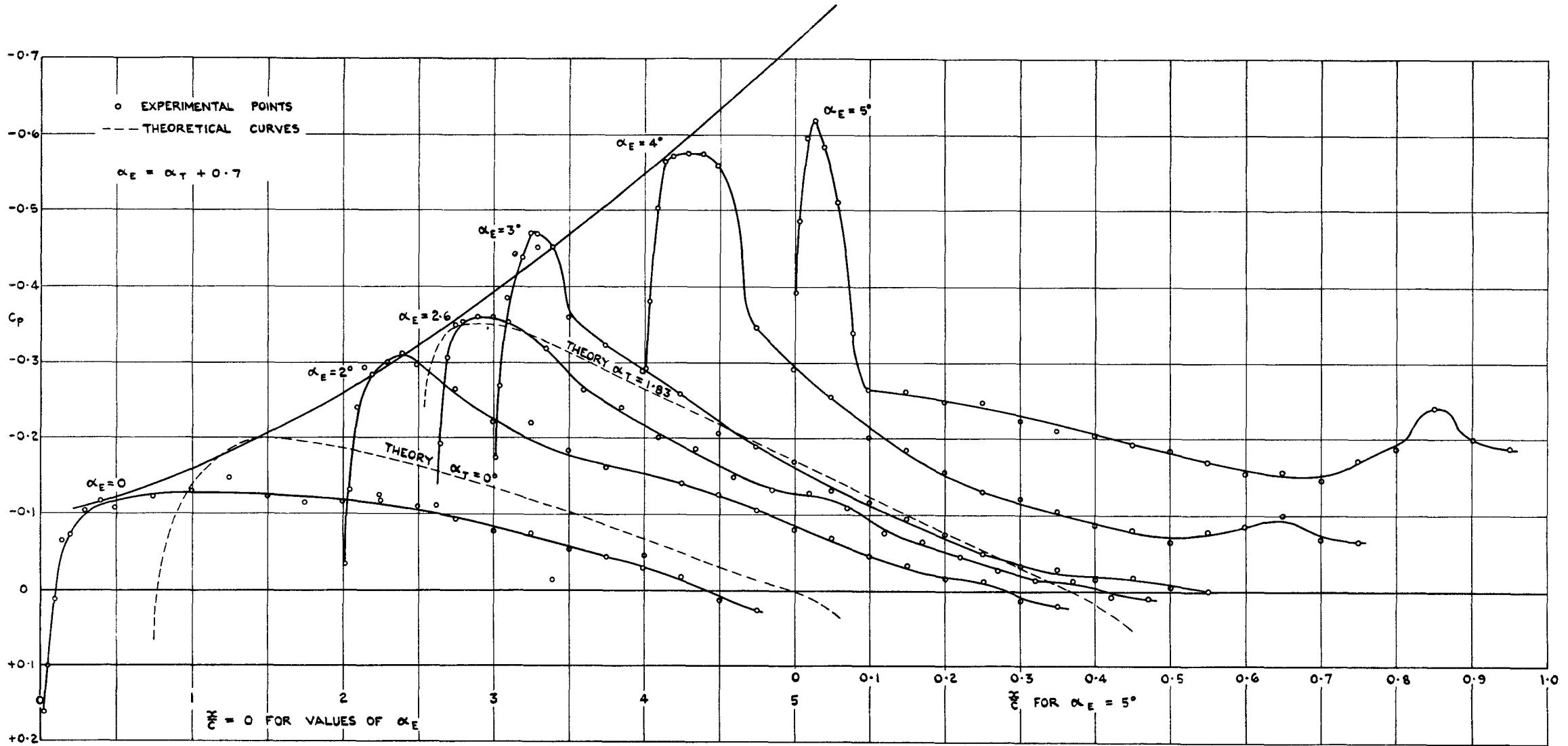


FIG.14 CARPET PLOT OF C_p vs. $\frac{x}{c}$ AND α_E , UPPER SURFACE, $M_0 \doteq 1.20$

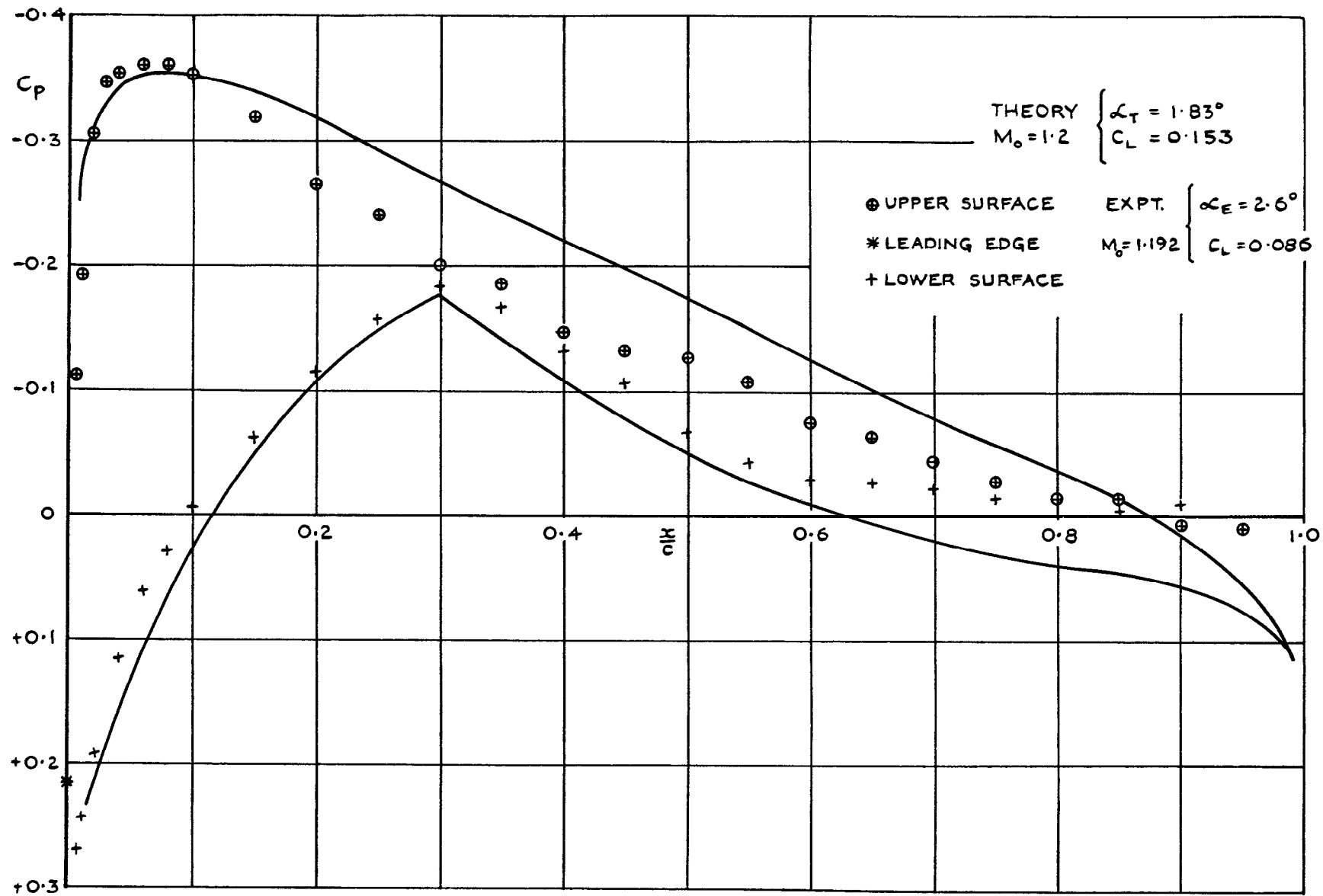


FIG.15. COMPARISON OF THEORETICAL AND EXPERIMENTAL PRESSURE DISTRIBUTIONS AT SIMILAR VALUES OF PEAK SUCTION, ($M_0 = 1.20$.)

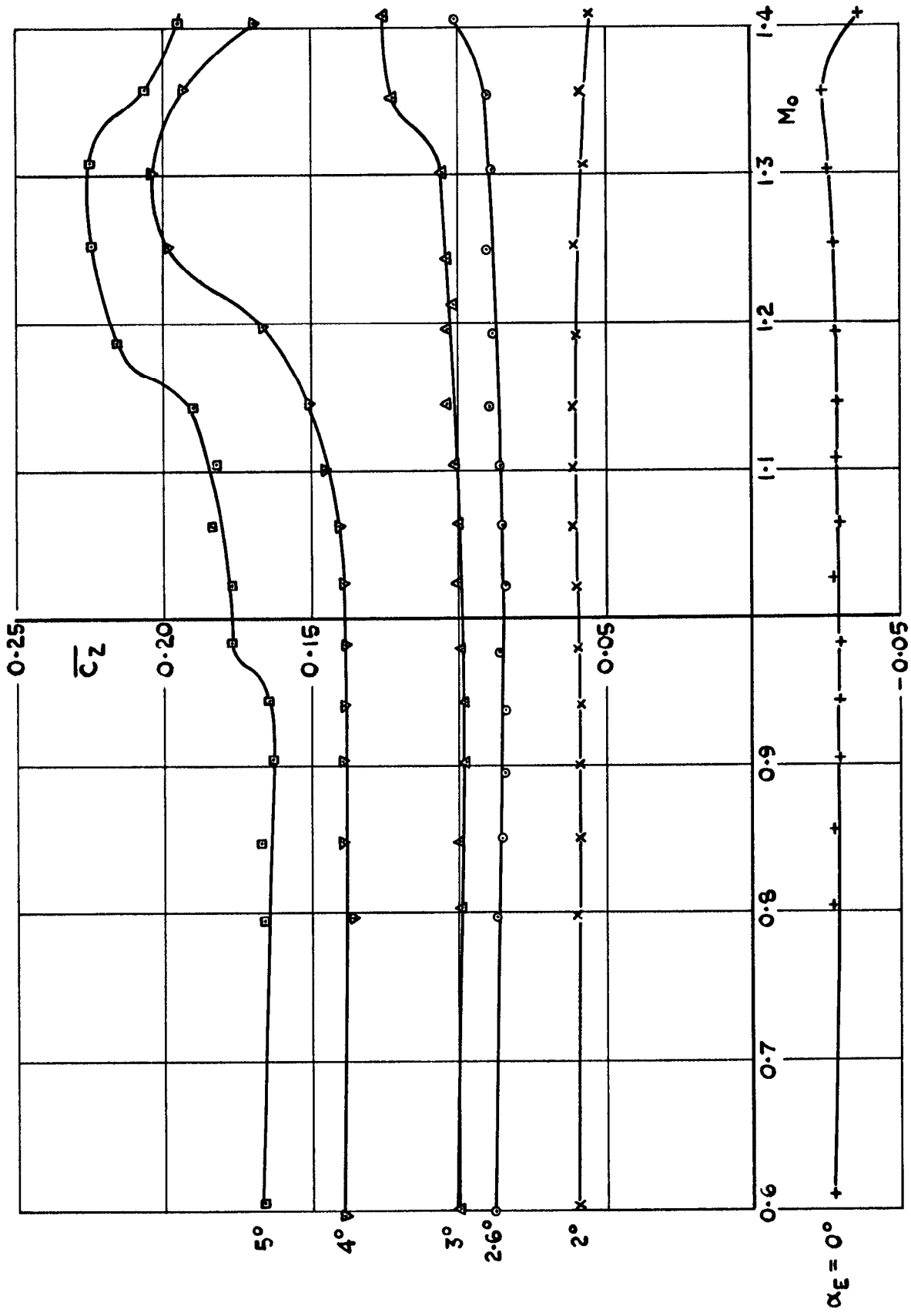


FIG.16 NORMAL FORCE COEFFICIENT vs. M_0 FOR VARYING α_E (NO "TUNNEL CORRECTIONS").

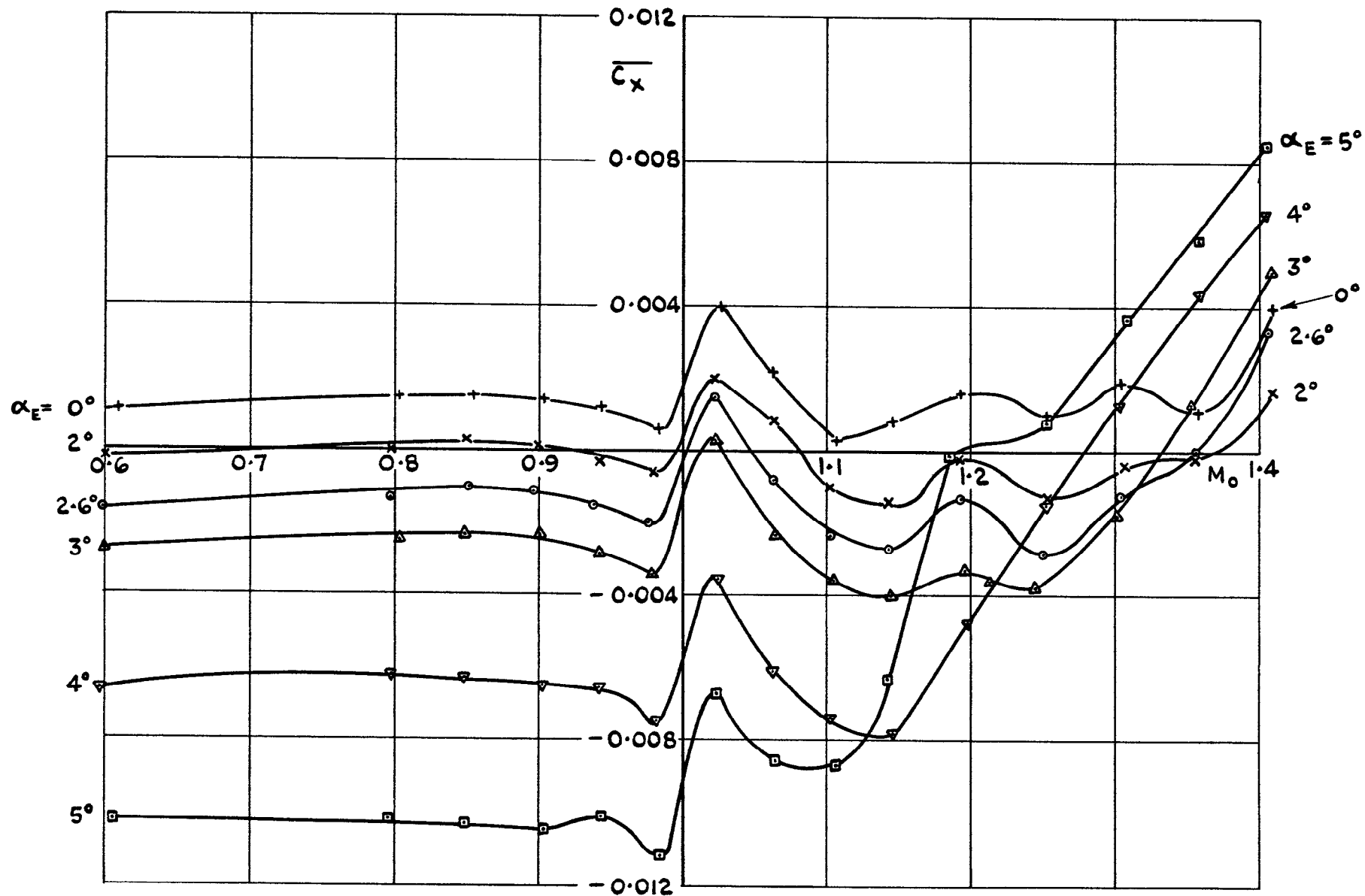


FIG.17 CHORD FORCE COEFFICIENT vs. M_0 FOR VARYING α_E
 (NO "TUNNEL CORRECTIONS").

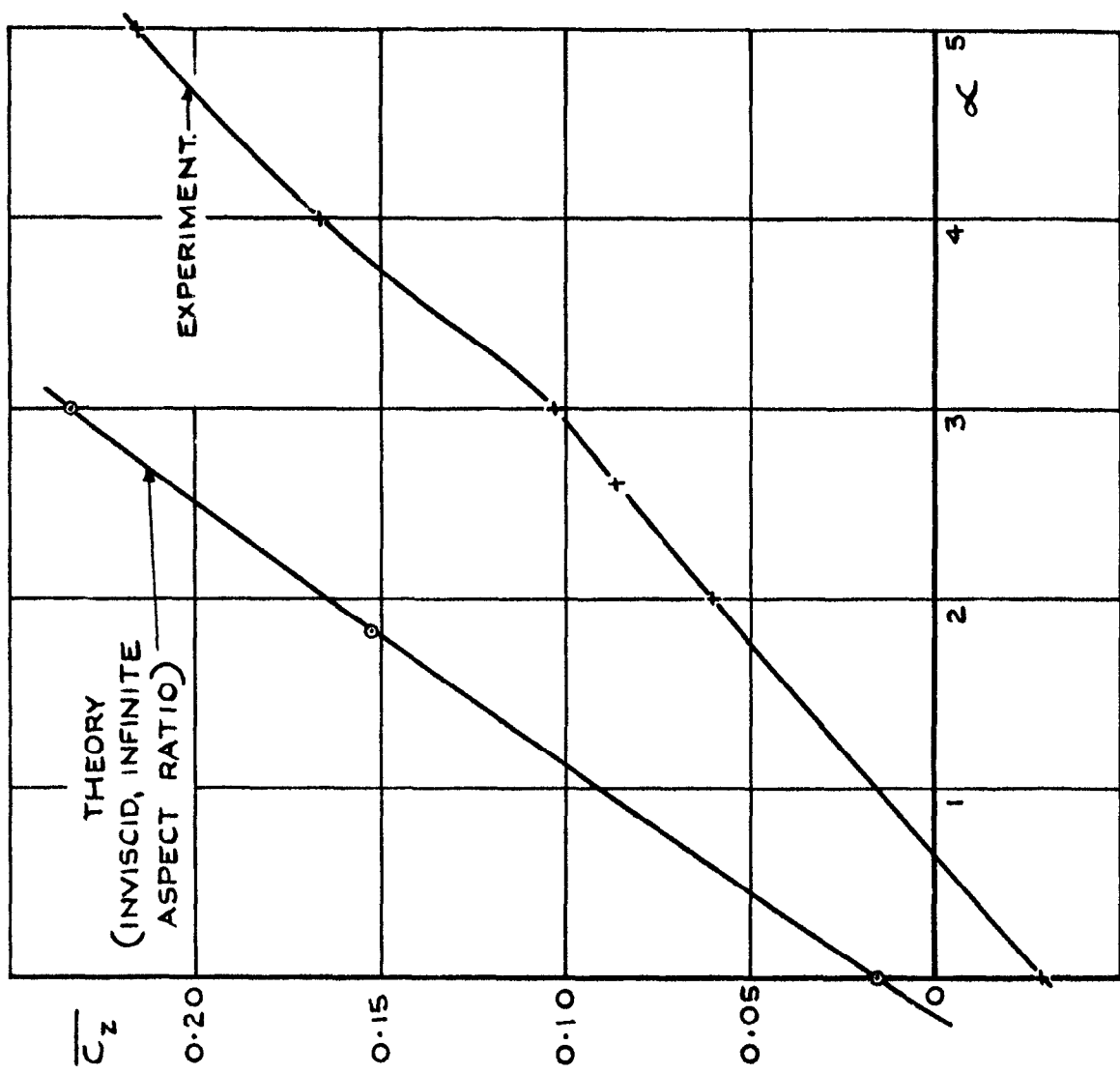


FIG.18. COMPARISON BETWEEN THEORETICAL AND EXPERIMENTAL NORMAL FORCE VS INCIDENCE CURVES AND ZERO LIFT ANGLES, $M_0 \approx 1.2$.

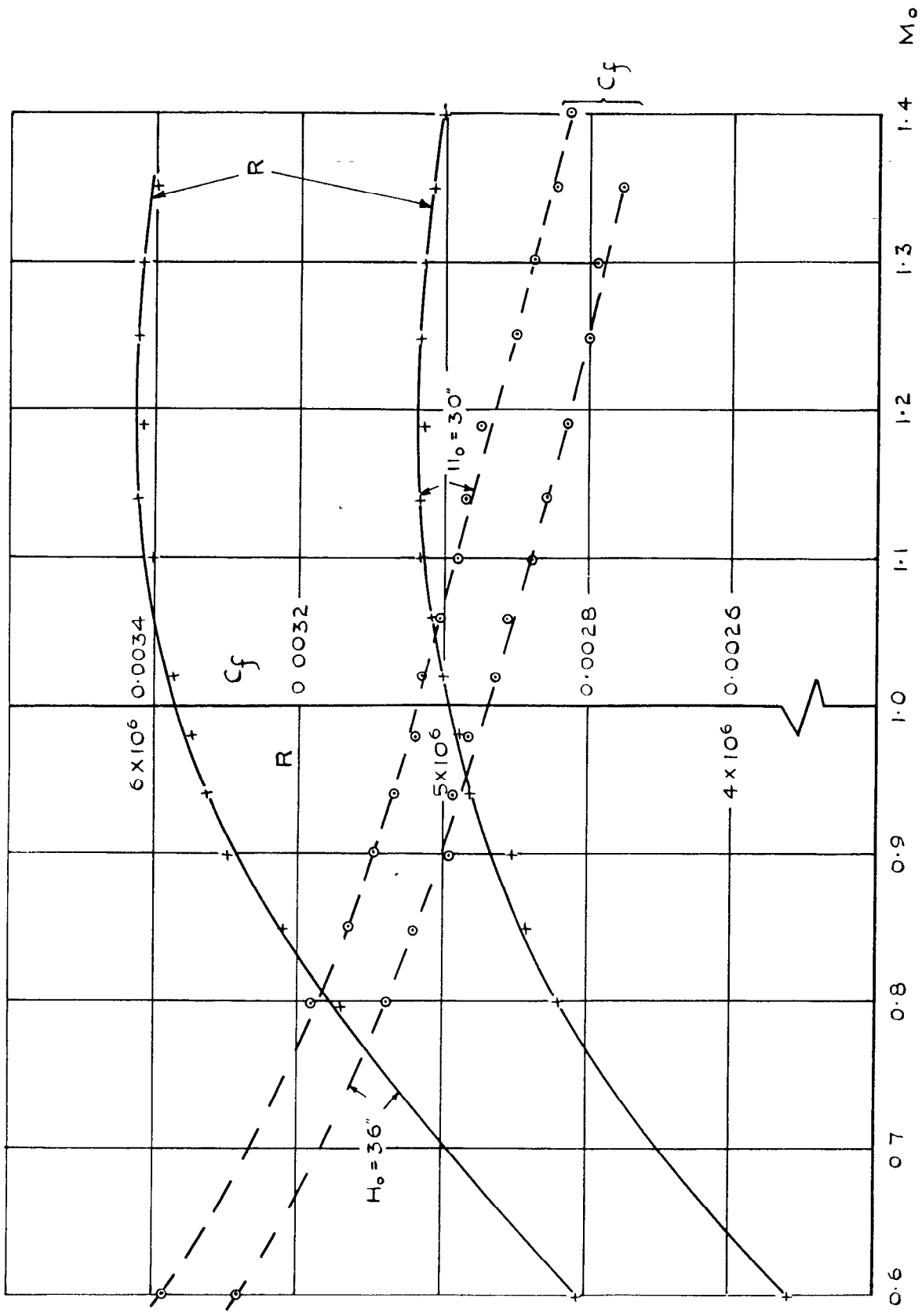


FIG .19. TEST REYNOLDS No. AND ASSUMED SKIN FRICTION COEFFICIENT vs MACH NUMBER.

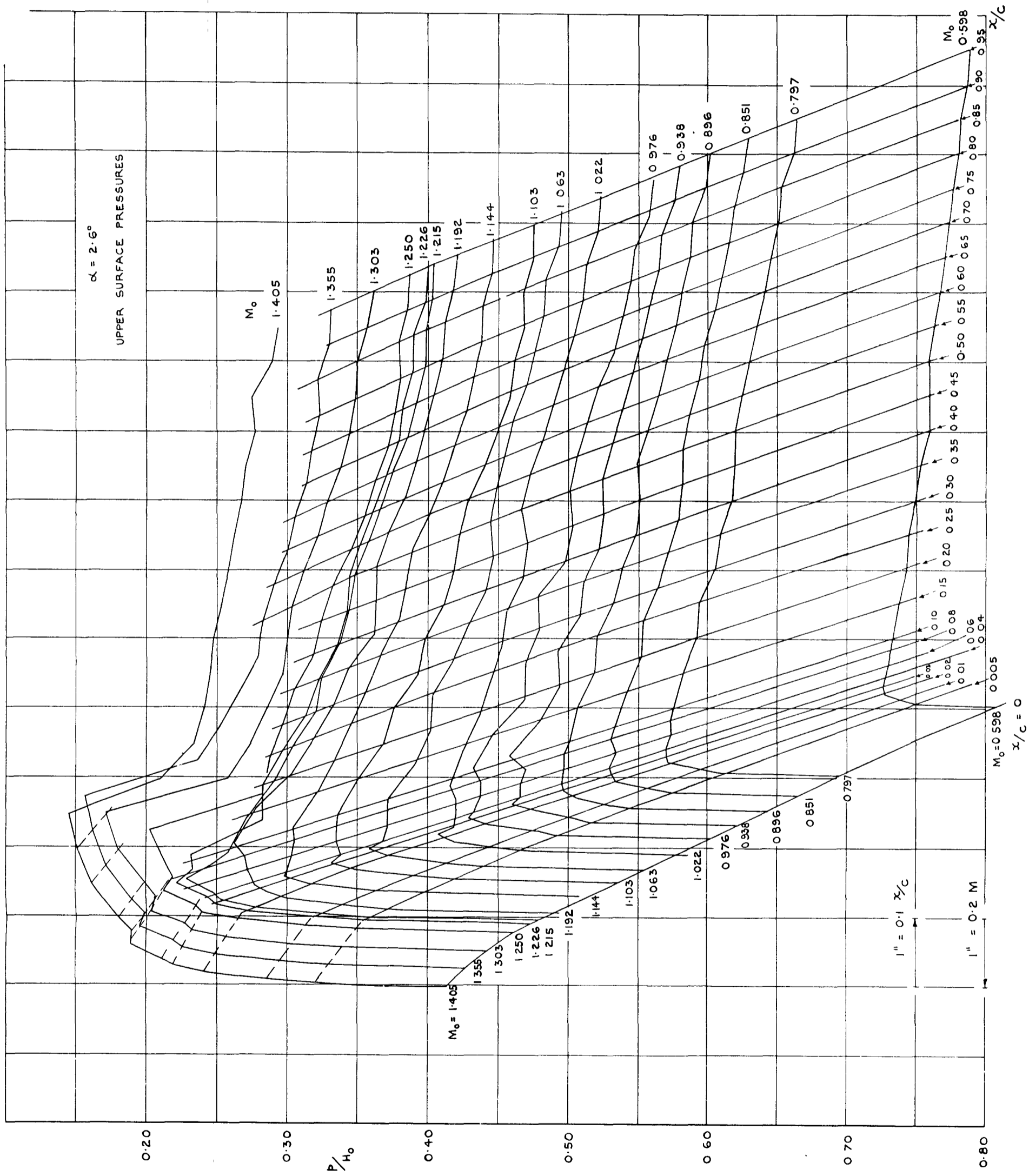


FIG. 20. CARPET PLOT OF $\frac{P}{H_0}$ VS. M_0 AND x/c , $\alpha_E = 2.6^\circ$, UPPER SURFACE.

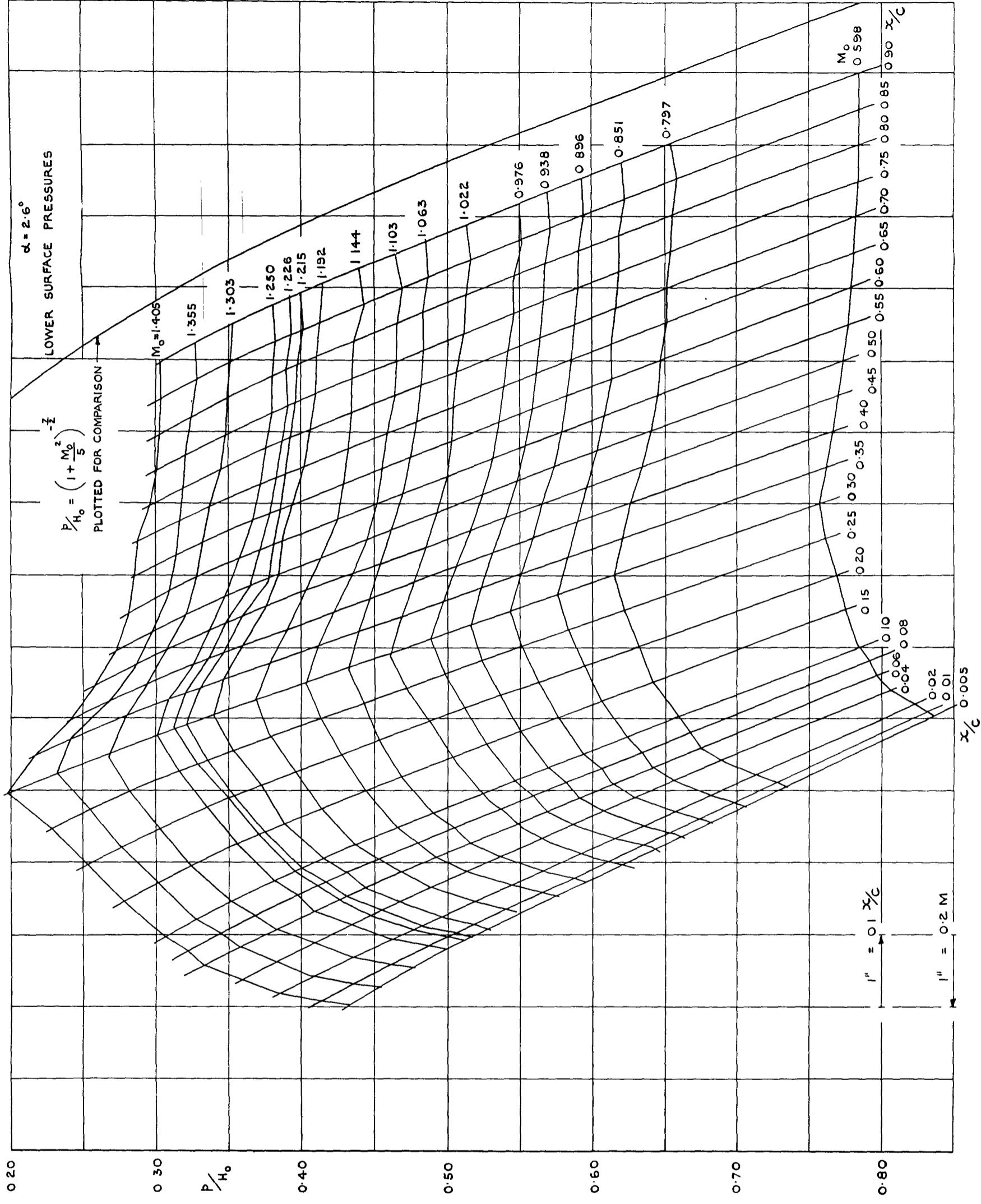


FIG.21. CARPET PLOT OF $\frac{P}{H_0}$ VS. M_0 AND x/c , $\alpha_E = 2.6^\circ$, LOWER SURFACE.

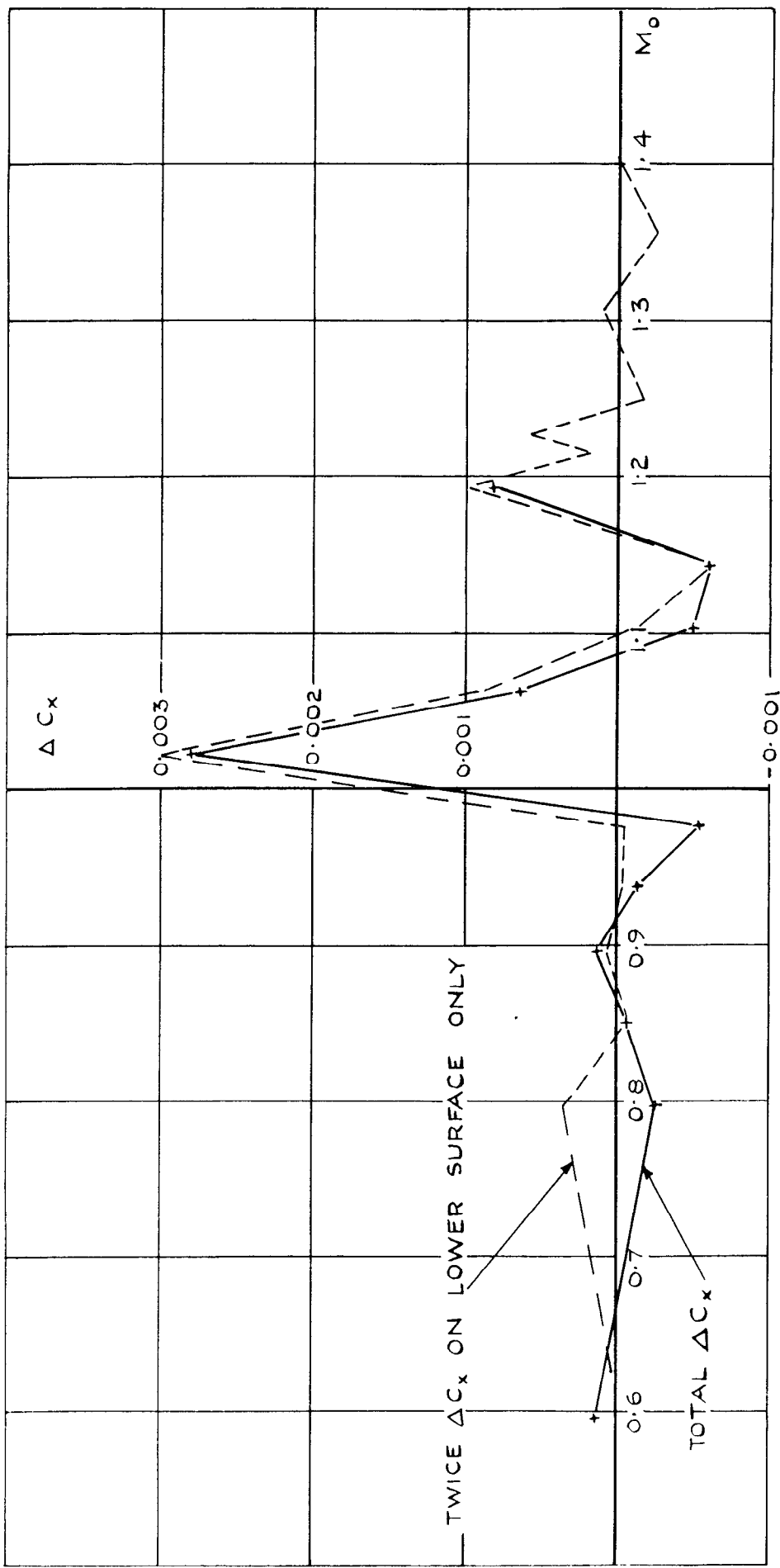


FIG. 22. CORRECTION TO CHORD FORCE COEFFICIENT VS M_0 , $\alpha_E = 2.6^\circ$.

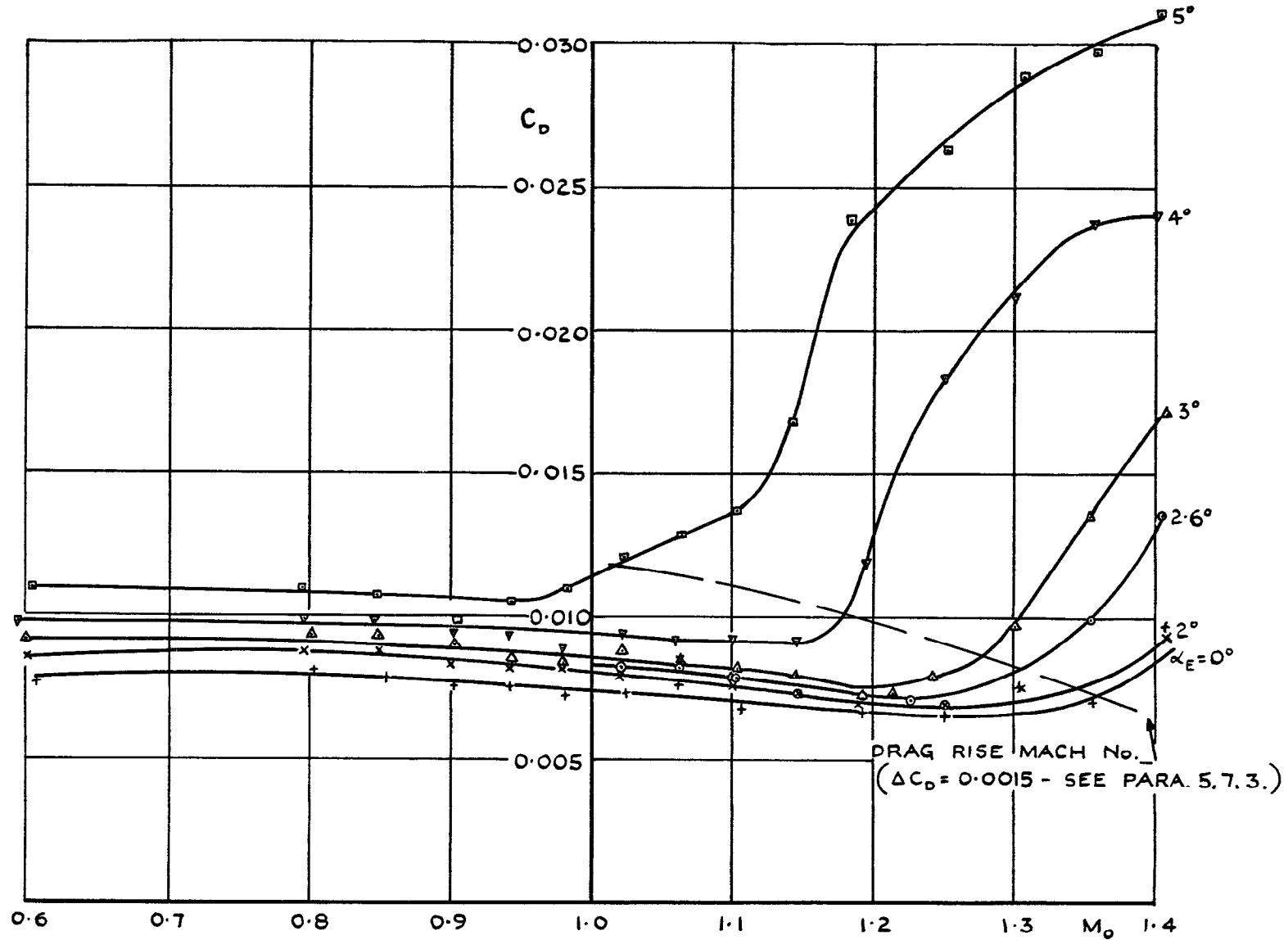


FIG. 23. SECTION DRAG COEFFICIENT vs MACH NUMBER FOR VARYING INCIDENCE (WITH "TUNNEL CORRECTIONS")

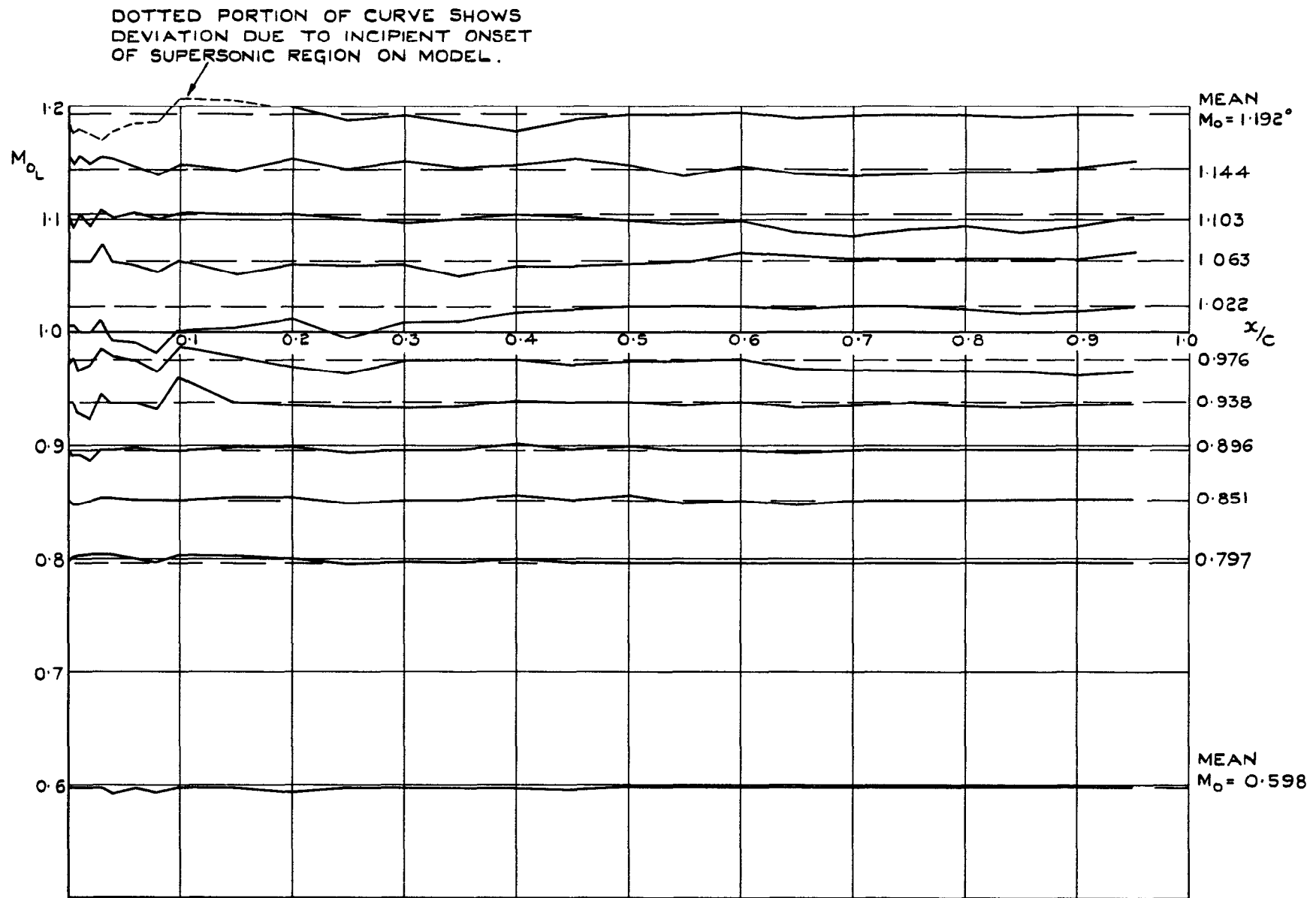


FIG. 24. TUNNEL MACH NUMBER DISTRIBUTION AT POSITION OF AEROFOIL.
(OBTAINED BY INTERPOLATION OF TEST RESULTS FROM UPPER SURFACE AT $\alpha_E = 2.6^\circ$)

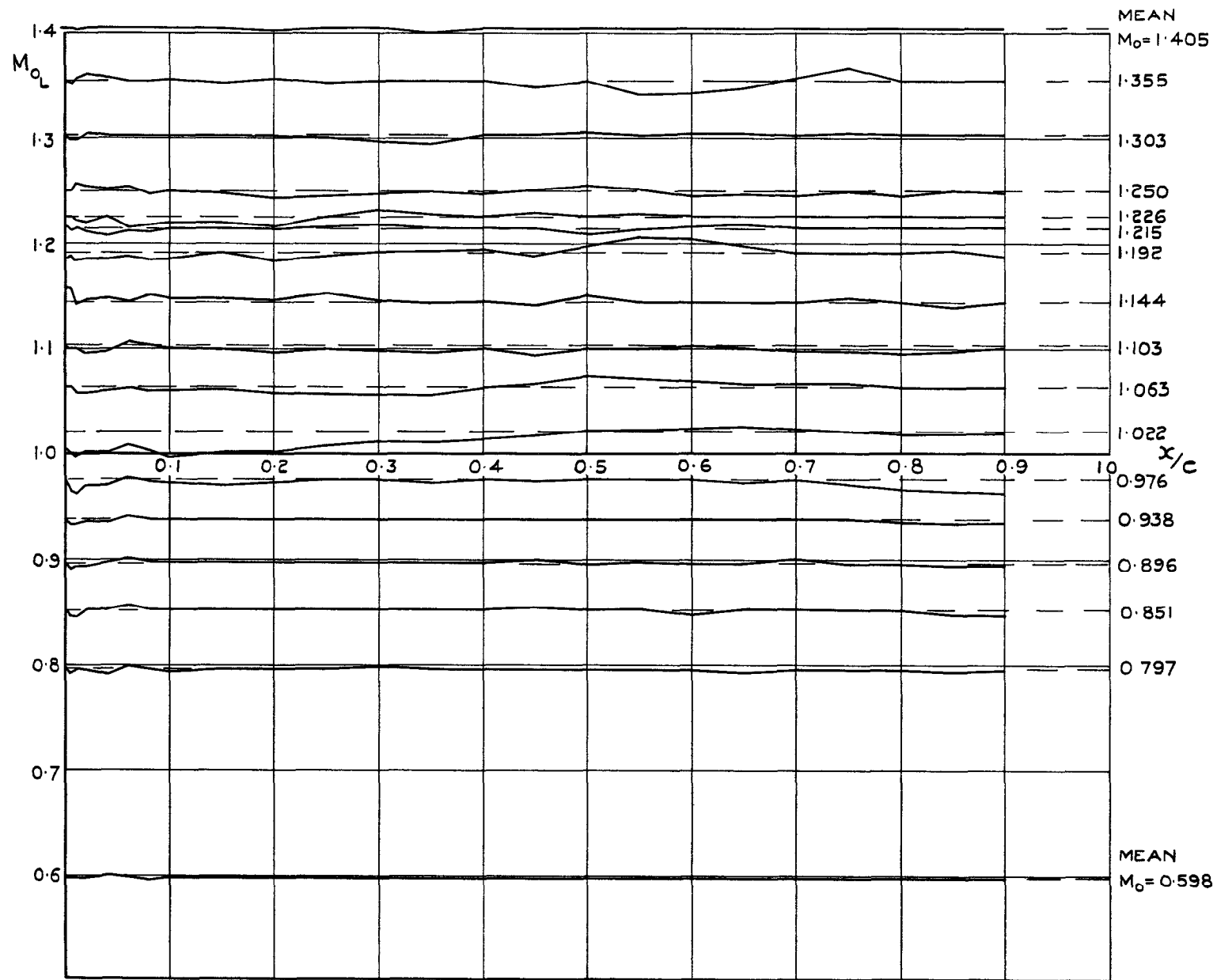


FIG. 25. TUNNEL MACH NUMBER DISTRIBUTION AT POSITION OF AEROFOIL.
 (OBTAINED BY INTERPOLATION OF TEST RESULTS FROM LOWER SURFACE AT $\alpha_E = 2.6^\circ$)

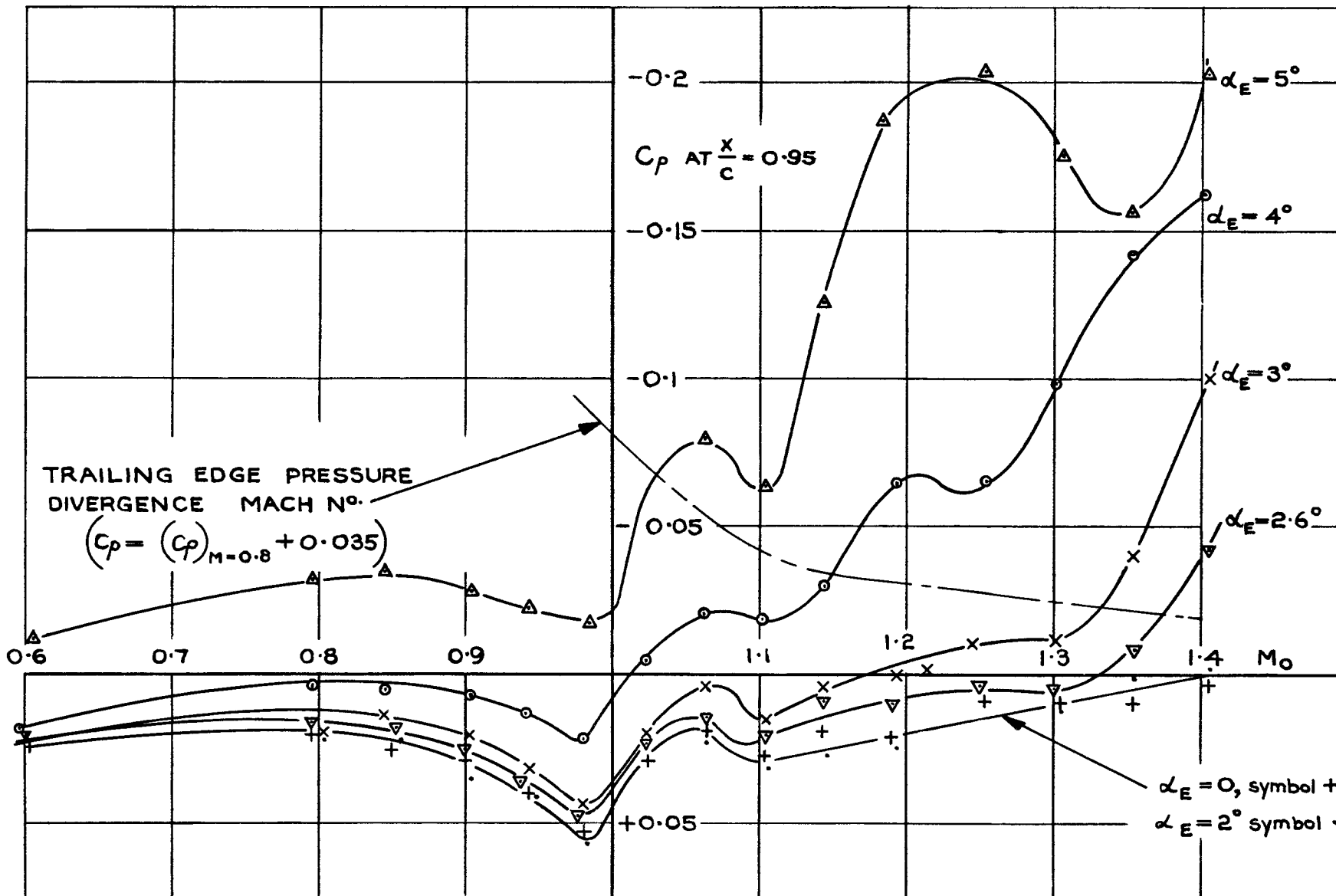
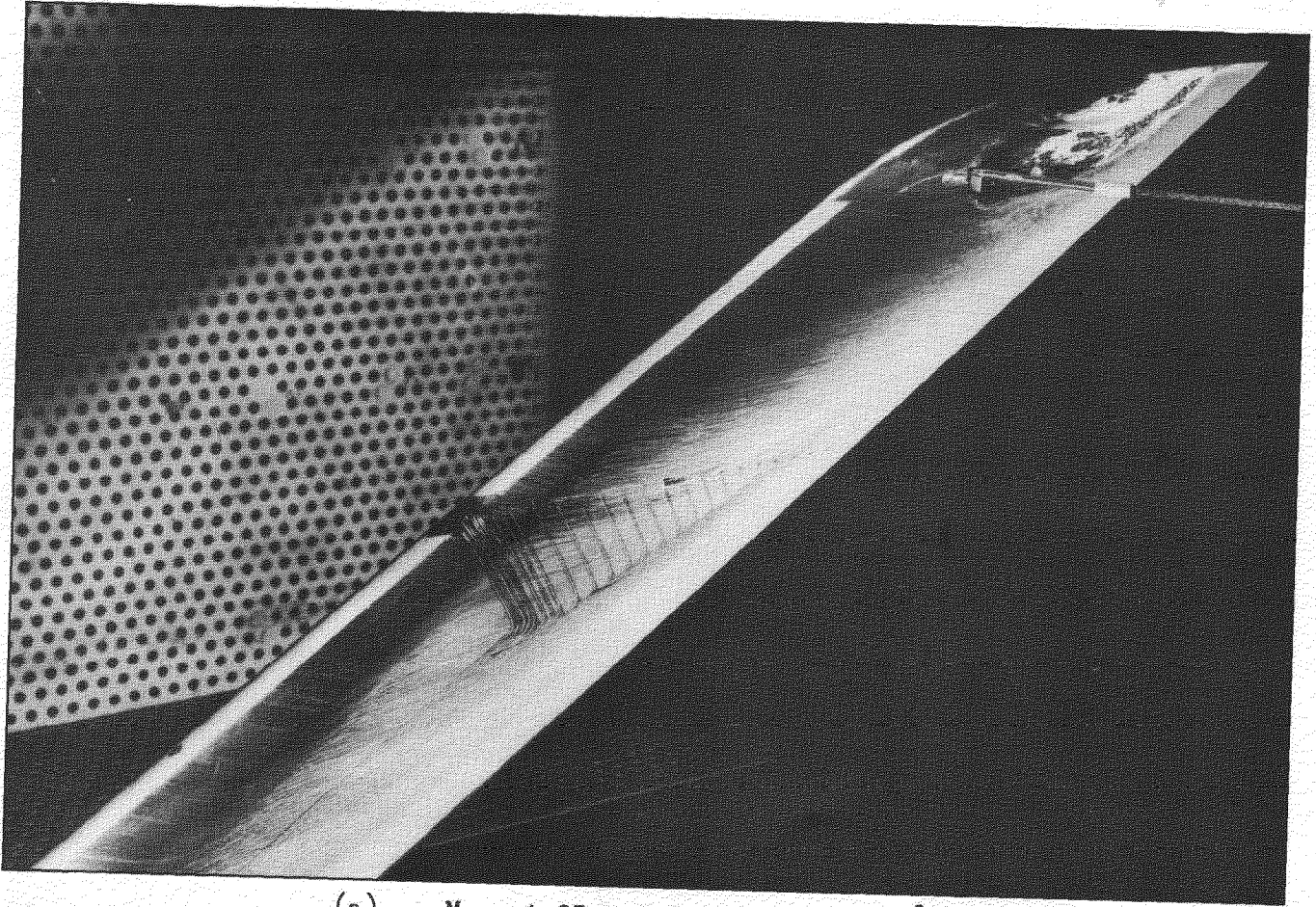
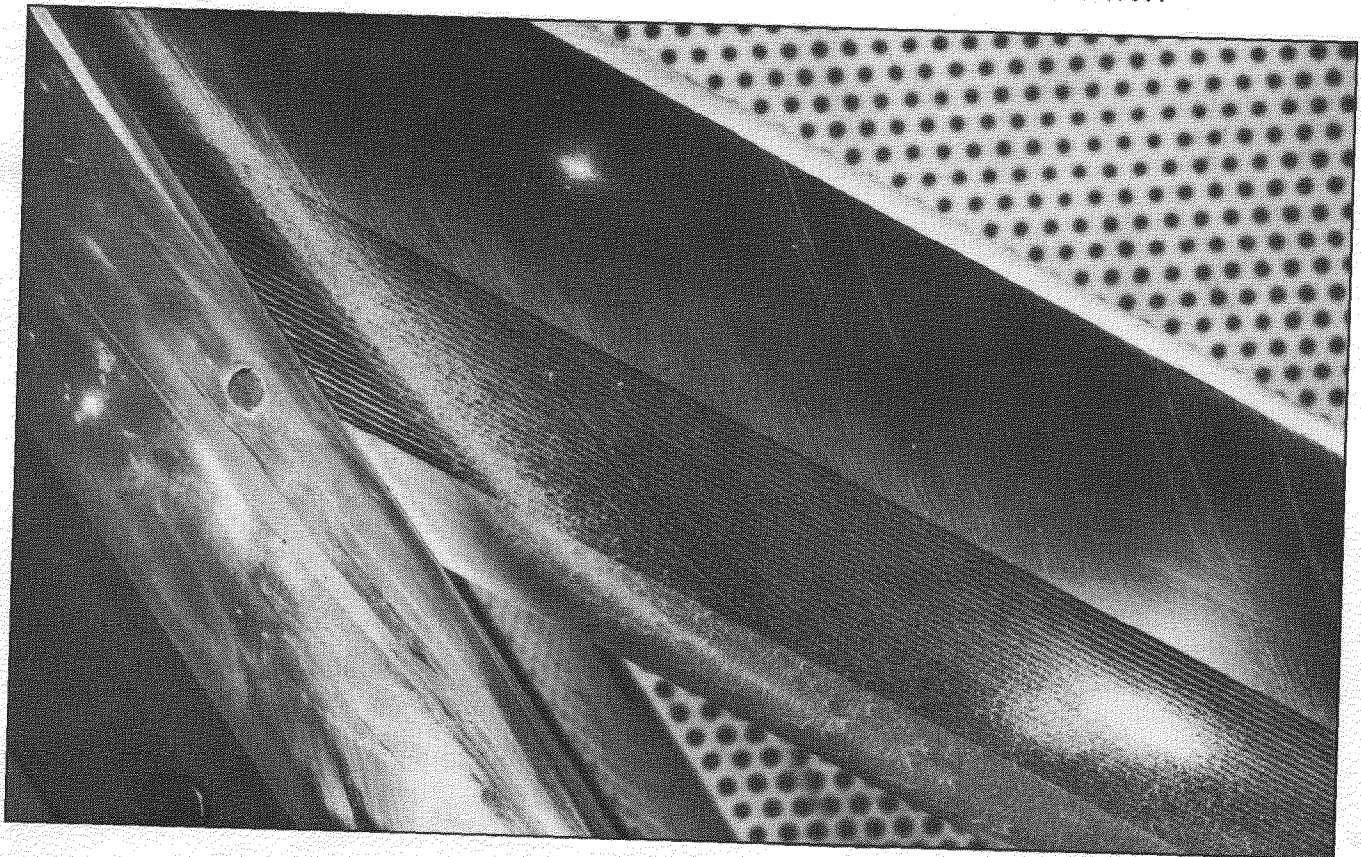


FIG. 26 PRESSURE COEFFICIENT AT 95% CHORD vs. MACH No.
FOR VARYING INCIDENCE



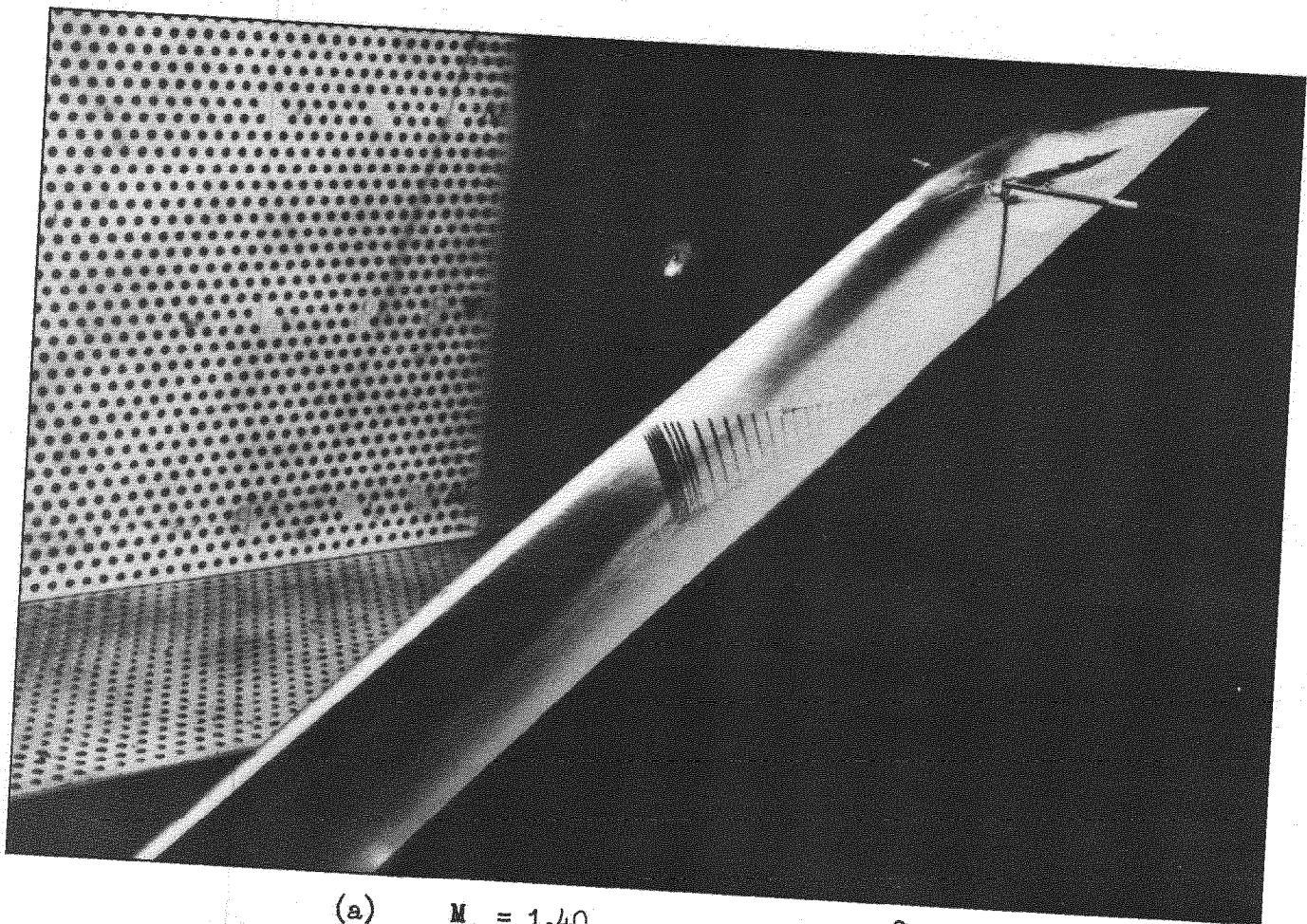
(a) $M_o = 1.25,$ $\alpha_E = 2.6^\circ$

a. OUTBOARD PART OF SPAN SHOWING PRESSURE MEASURING STATION

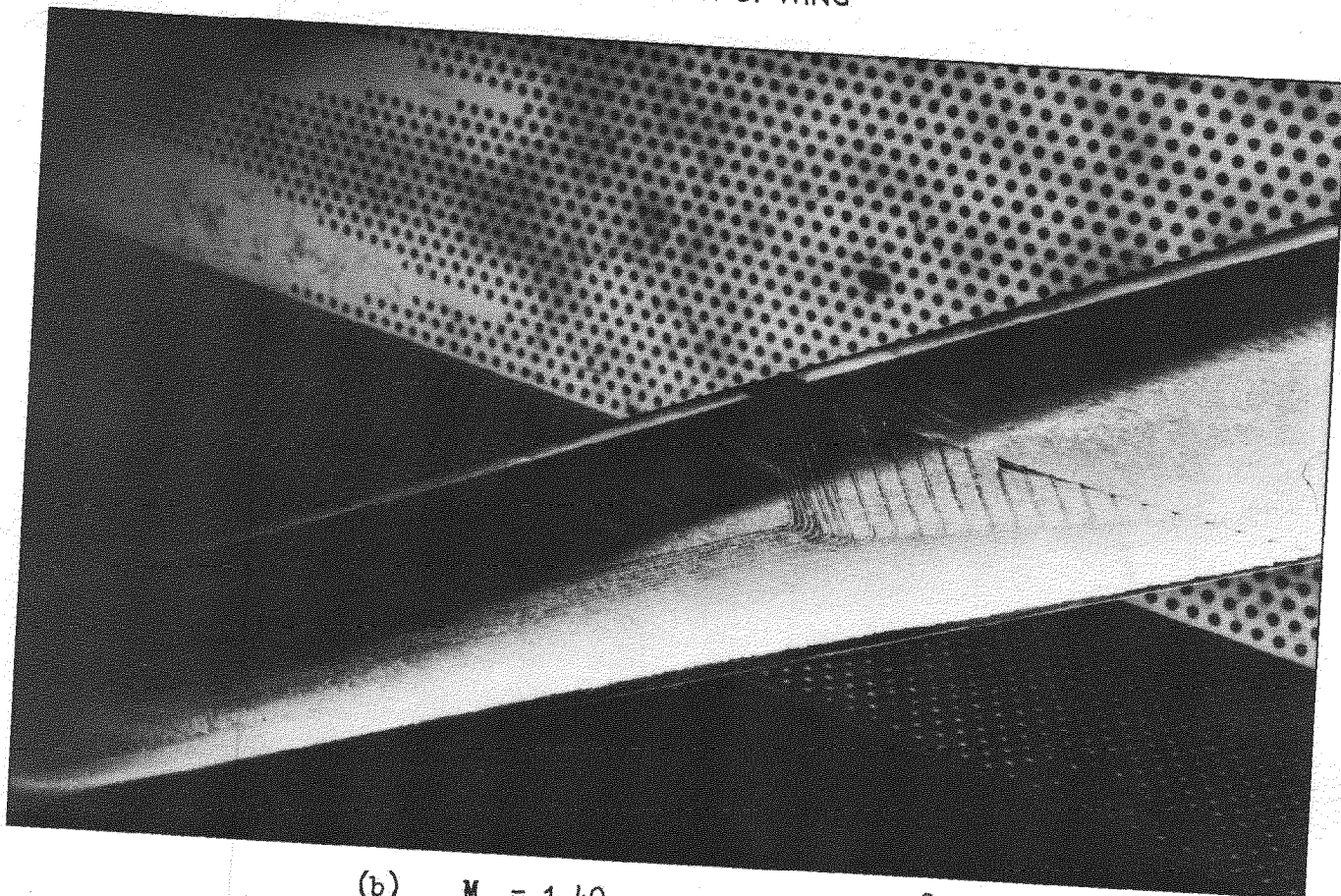


(b) $M_o = 1.25,$ $\alpha_E = 2.6^\circ$

b. WING BODY JUNCTION



(a) $M_o = 1.40,$ $\alpha_E = 2.6^\circ$
a. GENERAL VIEW OF WING



(b) $M_o = 1.40,$ $\alpha_E = 2.6^\circ$
b. REGION NEAR PRESSURE MEASURING STATION

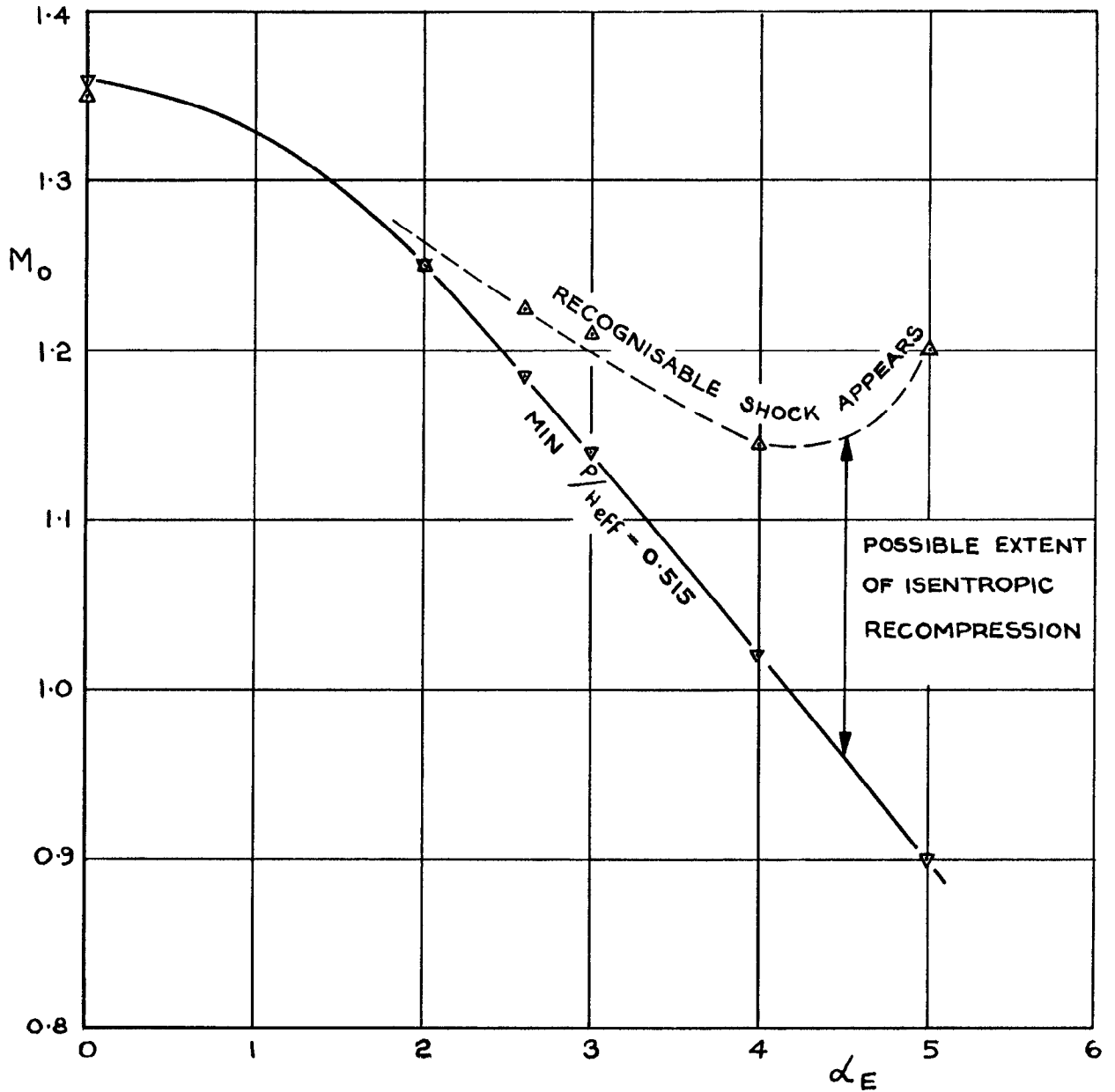


FIG. 29. MACH NUMBER FOR FIRST APPEARANCE OF SHOCK WAVE vs INCIDENCE; COMPARISON BETWEEN ESTIMATES BY METHOD OF REF. 14 AND OBSERVED VALUES (PARA. 5.7. 1.)

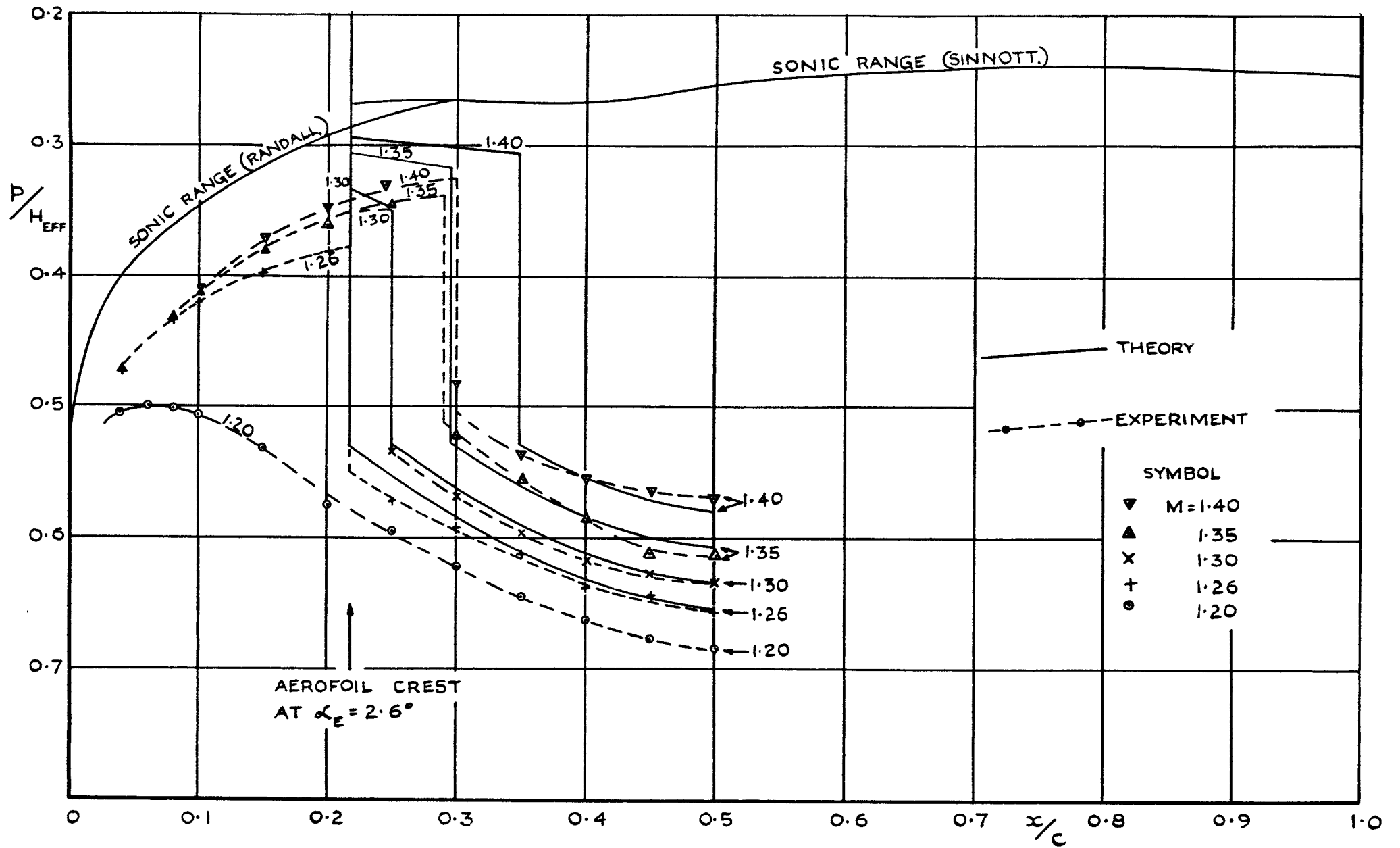


FIG. 30. COMPARISON OF THEORETICAL AND EXPERIMENTAL PRESSURE DISTRIBUTIONS WHEN THE SHOCK IS AFT OF THE AEROFOIL CREST ($\alpha_E = 2.6^\circ$)

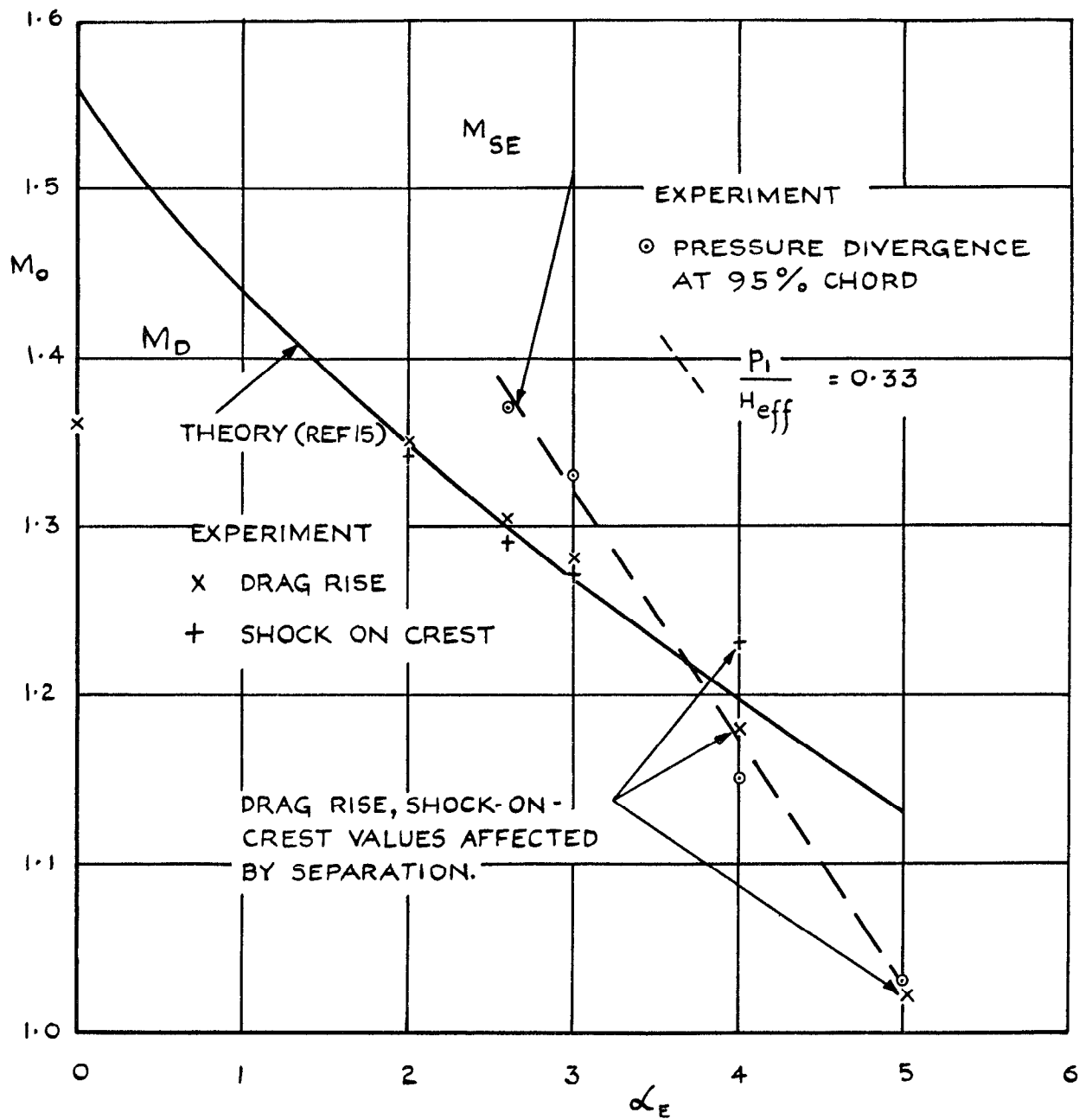


FIG. 31. MACH NUMBERS FOR DRAG RISE AND FOR ONSET OF SEPARATION EFFECTS vs INCIDENCE; COMPARISON BETWEEN THEORY AND EXPERIMENT.

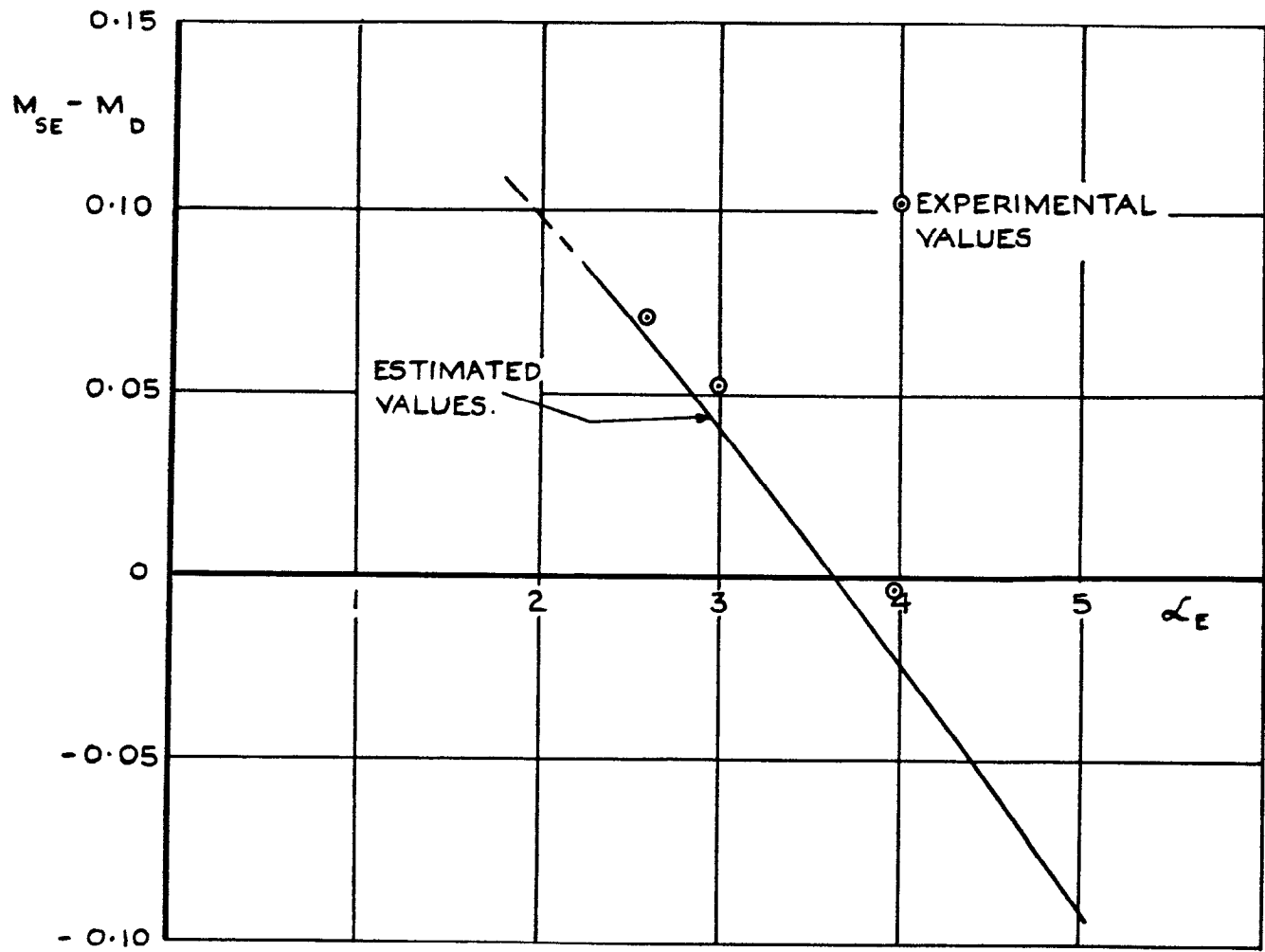


FIG. 32. VALUES OF MACH NUMBER MARGIN BETWEEN DRAG RISE AND ONSET OF SEPARATION EFFECTS vs INCIDENCE; COMPARISON BETWEEN THEORY AND EXPERIMENT.

A.R.C. C.P. No.582

533.692.1: 533.69.048.2:
533.693.1: 533.6.011.12:
533.6.011.35: 533.6.071.33
533.6.011.5:

WIND TUNNEL TESTS AT MACH NUMBERS BETWEEN 0.6 AND 1.4
OF A 60° SWEEP WING HAVING AN AEROFOIL SECTION DESIGNED
FOR SUBCRITICAL FLOW AT A MACH NUMBER OF 1.2.
PART I: 9% THICK SECTION WITH "TRIANGULAR" PRESSURE
DISTRIBUTION. Lawlor, E.F. May 1961.

Pressures have been measured at Mach numbers between 0.6 and 1.4
around one streamwise station on a 9% thick, 60° swept wing, cambered
to have a subcritical type of upper surface pressure distribution of
triangular shape at a Mach number of 1.2 and a lift coefficient of

P.T.O.

A.R.C. C.P. No.582

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P.T.O.

0.153. In spite of boundary layer effects which caused some loss of lift coefficient, subcritical flow conditions were achieved at the design Mach number of 1.2 with the design suction values over the forward part of the section. At all Mach numbers, the flow development was closely analogous to that over two dimensional aerofoils at subsonic speeds.

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