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Flight Measurements of the Drag of a
Swept-Wing Aircraft (*Hunter* Mk. 1) at Mach
Numbers up to 1.2, together with Some
Measurements of Lift-Curve Slope

By D. R. ANDREWS, B.Sc., B.Sc.(Eng.) and J. E. NETHAWAY, B.Sc.(Eng.)

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Flight Measurements of the Drag of a Swept-Wing Aircraft (*Hunter* Mk. I) at Mach Numbers up to 1.2, together with Some Measurements of Lift-Curve Slope

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Summary.

Flight tests have been made to determine the drag of a Hawker *Hunter* F Mk. I aircraft. The results show that at low Mach number the drag coefficient at zero lift is 0.0125 and the effective induced-drag factor K is 1.09, both values being corrected to a constant Reynolds number of 34×10^6 . Above a certain C_L the drag due to lift increases rapidly, the C_L at which this occurs falling from 0.76 at $M = 0.3$ to 0.41 at $M = 0.7$. Some approximate measurements of K made at supersonic speeds suggest that virtually all the leading-edge suction on the wing is lost beyond $M = 1.0$.

At $C_L = 0.1$, the compressibility drag rise commences soon after $M = 0.8$, the drag rising rapidly beyond $M = 0.92$ and attaining a peak C_D of 0.0565 at $M = 1.15$. The compressibility drag rise obtained from high-speed wind-tunnel tests agrees well with that obtained in flight although this agreement may be largely fortuitous in view of the low tunnel Reynolds number.

Measurements of incidence show that the lift-curve slope at $M = 0.3$ is 3.5 rising to 4.6 at $M = 0.9$. The zero-lift angle remains constant with Mach number at about 0.4° . Agreement with wind-tunnel tests is reasonably good when allowance is made for differences in geometry and in Reynolds number.

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1. *Introduction.*

This report presents the results of drag measurements on a Hawker *Hunter* F Mk. I aircraft.

The drag has been measured in stabilised levels and also in partial glides and dives using the accelerometer technique¹. The results extend to a Mach number of 1.2 and to lift coefficients of about 0.9 at low speeds and 0.15 at $M = 0.94$. From $M = 0.94$ to $M = 1.2$ the results have been obtained mainly at $C_L = 0.1$, although a small C_L range was covered at supersonic speeds in dives and pull-outs.

Some brief accelerated and decelerated levels² have also been made to assess the accuracy and value of this method of drag measurement.

Incidence measurements made during the stabilised levels and partial glides have enabled the lift-curve slope to be obtained for Mach numbers up to 0.94.

Wherever possible, comparison has been made between the flight results and the results obtained from wind-tunnel tests. This in turn has led to some discussion of the effects of surface roughness and transition position on the measured flight characteristics.

2. *Details of Aircraft and Instrumentation.*

The aircraft used in these tests was a Hawker *Hunter* F Mk. I. A general arrangement drawing is shown in Fig. 1 and a photograph in Fig. 2. The aircraft was fitted with a nose-boom airspeed system but was otherwise a standard production machine. No fuselage airbrakes were fitted. Further details of the aircraft are given in Table 1.

The nose-boom airspeed system was used primarily for the auto-observer instruments, but the pilot was also provided with an altimeter and A.S.I. supplied from this same source. The standard wing-boom airspeed system was left unaltered, and was used by the pilot for his normal flying.

Instruments to measure the following quantities were fitted in an auto-observer mounted in the ammunition bay: altitude (from nose boom), I.A.S. (from nose boom), static-pressure lag, jet-pipe total head, jet-pipe total temperature, ambient air temperature, engine r.p.m., and fuel contents. The auto-observer was photographed by an Eclair camera running at 8 frames per second. Longitudinal acceleration, normal acceleration, and aircraft attitude were recorded on Hussenot A.22 recorders running at a paper speed of about one inch per second. The camera and recorders were synchronised by a common timing unit and also by feeding an electrical signal to each recorder every time the camera shutter operated.

The accelerometers used for measuring longitudinal and normal acceleration were of the Royal Aircraft Establishment electrically transmitting type employing the 'Barnes' type of damping, the damping being adjusted to about 0.7 critical. These accelerometers were mounted along and normal

to the fuselage datum, and in a position sufficiently close to the aircraft c.g. so that the effects of pitching velocity and pitching acceleration could be assumed negligible.

The inclination of the aircraft datum to the horizontal was measured with a Hussenot pendulum level, this instrument consisting of simply an undamped free pendulum with a number of mirrors attached to it. As such a pendulum is very sensitive to longitudinal acceleration, special care was necessary when using it to ensure that either the speed was constant or that the acceleration was known accurately enough for a correction to be applied. Measurements made with this instrument are clearly most accurate in stabilised levels.

3. Method of Test and Analysis of Results.

3.1. Drag Measurements.

The aircraft drag was determined by several different methods depending upon the combination of C_L and M under investigation. Techniques of stabilised levels, partial glides, and dives were all adopted at different times, and for purposes of comparison brief tests were also made using the accelerated and decelerated levels technique.

The following table summarises the techniques adopted and the range of Mach number and C_L covered by each.

Technique	M	C_L
Stabilised levels	0.3	0.5 to 0.7
	0.4	0.2 to 0.7
	0.5	0.15 to 0.6
	0.6	0.1 to 0.5
	0.7 to 0.9	0.1 to 0.3
	0.94	0.1 to 0.15
Partial glides	0.3	} 0.7 to 0.9
	0.4	
	0.5	0.7 to 0.8
Dives	0.65 to 0.7	0.5
	0.9 to 1.05	0.1
	1.05 to 1.23	0.05 to 0.2 (approx.)
Accelerated and decelerated levels	0.4 to 0.93	0.3 to 0.06
	0.55 to 0.93	0.5 to 0.18

It is shown in Ref. 1 that the drag, D , is given approximately by

$$\frac{D - F_N}{W} = R + Q\chi \quad (1)$$

where

F_N = nett thrust

W = aircraft weight

R = reading of longitudinal accelerometer in g units

Q = reading of normal accelerometer in g units

χ = angle between flight path and longitudinal accelerometer axis (radians).

In stabilised levels $D = F_N$, but under other conditions we must also measure R , Q and χ .

The nett thrust was measured using the jet-pipe pitot method. The theory behind this method is explained fully in Ref. 1. As is usual in applying this method, the following assumptions were made:

- (a) the jet-pipe 'effective area' obtained from the test-bed calibration remains constant at all values of jet-pipe pressure ratio beyond choking.
- (b) the air-mass-flow effective area is the same as the thrust effective area.
- (c) total air mass flow is the same as total gas mass flow (i.e. fuel flow is neglected).

3.1.1. *Stabilised levels.*—To facilitate fairing and cross plotting, the stabilised levels were made at specified Mach numbers and C_L 's in the manner of Ref. 3. For each Mach number and C_L the pilot was given a chart showing indicated airspeed and altitude plotted against fuel contents, so that he could select the speed and altitude appropriate to the fuel state. Great care was taken to stabilise speed and altitude accurately.

The drag of the aircraft was determined from the stabilised levels by equating the horizontal component of nett thrust to drag, in the usual manner.

Measurements of incidence were made during these stabilised levels, the incidence being obtained directly from the readings of the Hussenot pendulum level (Section 2).

3.1.2. *Dives and partial glides.*—The accelerometer technique¹ was used to measure drag from partial glides and dives. The results were obtained at given C_L 's and Mach numbers by giving the pilot charts similar to those used for the stabilised levels, but with additional lines appropriate to various dive or glide angles also plotted.

The drag from $M = 1.05$ to $M = 1.23$ was determined from continuous records of dives and pullouts.

As the accelerometer technique demanded a knowledge of the incidence of the aircraft {equation (i)}, it was necessary to either measure this quantity directly or estimate it. In the glides at low Mach number, the aircraft incidence was obtained from measurements of attitude (using the pendulum level) and rate of descent. It was found important to maintain a steady speed and rate of descent during these glides, as otherwise the error in incidence measurement could be appreciable. Estimated values of incidence were used for the high Mach number dives. The assumptions made in these estimates will be discussed in Section 4.2.

The Appendix gives a brief discussion on the effects of errors in incidence on the accuracy of drag measurements using the accelerometer technique.

3.1.3. *Accelerated and decelerated levels.*—Accelerated and decelerated levels were made at 15 000 ft and at 40 000 ft so that a direct comparison could be made between this method and the method of stabilised levels. The pilot performing the tests was given one flight to familiarise himself with the technique, all recorded runs then being made on his second flight.

For an accelerated level, the aircraft was flown at a given altitude and at some conveniently low speed. The throttle was then opened fully and the aircraft allowed to accelerate to its top speed, the pilot maintaining constant altitude throughout. A continuous auto-observer record was taken allowing a time history of true altitude, true airspeed, and nett thrust to be obtained. The results were analysed using the procedure of Ref. 2. Decelerated levels were obtained by reversing the above procedure, commencing at high speed and closing the throttle.

The pilot was instructed to maintain constant *indicated* altitude using the altimeter connected to the wing-boom pressure head. This resulted in an easier piloting technique than attempting to maintain constant *true* altitude but led to a progressive correction for dh/dt in the analysis of the results. However, this correction was relatively small as the position error of the wing-boom system was itself small up to $M = 0.94$.

3.2. Corrections to Flight Data.

The static- and pitot-pressure errors of the nose-boom system on this aircraft have already been measured and the results given in Ref. 4. These results have been used throughout the present tests to make corrections for position error.

Corrections for pressure lag in the static and pitot lines of the airspeed system and in the jet-pipe pitot system were applied to all flight measurements made in dives or glides. The lag in these systems was determined from ground tests in the usual manner¹⁴.

The impact air temperature bulb was calibrated for Mach number effects by the standard technique. Runs at various Mach numbers were made at constant-pressure altitudes of 15 000 ft and 35 000 ft. A temperature recovery factor of 0.96 was found at both altitudes. This value has been used throughout the present tests to obtain ambient air temperature and true airspeed.

4. Results and Discussion.

4.1. Transition and Surface Roughness.

As some reference will be made later to the effects of transition and of surface roughness, it is convenient to discuss these effects separately before proceeding with the discussion of the lift and drag results.

4.1.1. Transition.

Some brief flight tests to determine transition were made using the sublimation technique¹⁹. Tests were made at 4000 ft altitude at two speeds, 180 knots ($R = 18 \times 10^6$, $C_L = 0.39$) and 460 knots ($R = 45 \times 10^6$, $C_L = 0.06$). No laminar flow was found to be present on the wing at either speed. At 180 knots, transition on the upper surface of the tailplane was found to be at the skin joint at 15% chord. The records on the lower surface of the tailplane at this speed and on both surfaces of the tailplane at the higher speed were unfortunately insufficiently clear to enable any observations to be made.

The few results that were obtained are in general agreement with what would be expected from our knowledge of the destabilising effect of sweepback on a laminar boundary layer⁶. Calculations based on Refs. 7 and 8 show that, for the combinations of R and C_L achieved in level flight on the *Hunter*, transition would be expected to be always at or very near the leading edge of the wing on both the upper and lower surfaces. This was found to be the case in the two conditions tested.

Similar calculations for the tailplane show that conditions there are more favourable to the occurrence of regions of laminar flow, particularly at low speeds where the Reynolds numbers are low. However, in practice it is unlikely that laminar flow will extend beyond 15% chord on either surface because of a skin joint at that point. Variations in transition position over this limited chord-wise extent would be expected to have a negligible effect on the drag and lift of the complete aircraft.

Only small regions of laminar flow would be expected on the fin because of the various panels and joints near the leading edge. No data are available for the fuselage, but transition is expected to be near the nose as the surface finish immediately behind the nose boom was poor.

4.1.2. *Surface roughness.*—The surface condition of the aircraft was generally very good. The upper surfaces were finished in a glossy grey-green camouflage cellulose, whilst the lower surfaces were of matt silver. All surfaces were wax polished periodically. Rivets and skin joints (other than transport joints or inspection covers) were generally flush and well concealed. However, as flying progressed the condition began to deteriorate, and the paint began to flake in parts, notably along the leading edge of the wings and on the fairing at the rear of the nose boom.

The roughness of the paint finish was measured using a 'Talysurf' roughness machine. The roughness was found to vary appreciably from point to point but average values for the particle size were about 0.00005 in. for the camouflage paint and about 0.00015 in. for the silver paint. Ref. 5 shows that this degree of roughness is small enough for the *paint surface* to be considered as being aerodynamically smooth. It should be noted that the variation with Reynolds number of the drag of the complete aircraft will not be as great as if the aircraft had aerodynamically smooth surfaces, due to the effects of control-surface gaps, skin joints, and other surface irregularities. Unfortunately no means is available for estimating the extent to which these irregularities might influence the drag.

4.2. *Incidence and Lift-Curve Slope.*

The results obtained from the measurement of incidence are shown in Fig. 3 plotted in carpet form. Note that the C_L 's are trimmed values and that the incidence is measured from the wing datum.

The Reynolds number varies throughout the carpet of Fig. 3 decreasing from a mean value of about 30×10^6 at $C_L = 0.1$ to about 13×10^6 at $C_L = 0.5$. The specific values of R corresponding to the various C_L 's and Mach numbers can be obtained from Fig. 5. Estimates using Ref. 11 suggest that the effects of this Reynolds number variation are negligible. Estimates also show that the c.g. variation as fuel is consumed is insufficiently large to warrant any corrections to C_L to reduce these values to a constant c.g. position.

Fig. 3 shows that the incidence for zero lift is about 0.4° at all Mach numbers. This compares quite well with the values obtained from wind-tunnel tests^{9,10,12}. The lift-curve slopes derived from Fig. 3 are shown plotted in Fig. 4a. It is seen that $(\partial C_L / \partial \alpha)_M$ increases with Mach number up to $M = 0.9$ and then decreases slightly. In this respect it should be noted that at $M = 0.94$ the C_L range over which incidence measurements were made was small by comparison with experimental scatter. Thus, as the lift-curve slope obtained at this Mach number may not be very reliable, the fall in $(\partial C_L / \partial \alpha)_M$ at the higher Mach number cannot be regarded as being conclusively proved.

Also shown in Fig. 4a are the results of wind-tunnel tests on two *Hunter* models^{9,10}. To facilitate comparison with these, the flight results have been corrected to the tail-off condition, using the data of Ref. 9. The wind-tunnel results of Ref. 9 are seen to give a 5 to 10% lower lift-curve slope than the flight tests. Estimates based on Ref. 11 suggest that the geometrical differences between the wind-tunnel model and the full-scale aircraft would be sufficient to account for a 3% difference in $\partial C_L / \partial \alpha$, the remaining difference being possibly due to scale effect¹². The tests of Ref. 10 were on a more representative model at a higher Reynolds number, and are seen to give a value of $\partial C_L / \partial \alpha$ in fairly good agreement with that obtained by extrapolation of the flight results. The tunnel results quoted above were all with transition free.

Fig. 4b shows the flight results (corrected to tail-off condition) compared with estimates for the wing alone as derived from Refs. 11 and 13. In making these estimates transition on the wing was assumed to be at the leading edge (*see* Section 4.1). Comparison shows that the estimated lift-curve slopes are consistently lower than the flight results. Inclusion of the fuselage¹⁸ would only increase

the estimated lift-curve slope by about 4%, leaving a large discrepancy between estimates and flight tests still unaccounted for.

As it was not found possible to measure incidence directly in flight at transonic and supersonic speeds, some assumptions were necessary in this respect in order that drag measurements could be made using the accelerometer technique. In the absence of any directly applicable experimental data on lift-curve slope, the existing experimental curve (tail on) was faired smoothly into the supersonic curve estimated from Ref. 13. A further assumption made was that the zero-lift angle remained constant at 0.4° at all Mach numbers. Clearly, these extrapolations and assumptions are not completely satisfactory but they present the best that can be done under the circumstances. The errors in drag introduced by errors in these assumed values of incidence are discussed in the Appendix.

4.3. Drag.

4.3.1. *Drag due to lift.*—The drag results obtained from stabilised levels are presented in Fig. 5. It will be seen that at low C_L the compressibility drag rise commences soon after $M = 0.8$. As C_L increases, the drag rise commences progressively earlier until at $C_L = 0.5$ the drag starts to increase soon after $M = 0.45$.

The results of Fig. 5 are shown in Fig. 6a plotted as C_D versus C_L^2 for constant Mach numbers. The values plotted are those obtained from the faired lines drawn in Fig. 5, the low Mach number values being those below the drag rise. Straight lines have been drawn through the various sets of values on the assumption that drag obeys the law

$$C_{DT} = C_{DZ} + \frac{K}{\pi A} C_L^2$$

where

$$C_{DT} = \text{total aircraft drag coefficient}$$

$$C_{DZ} = \text{drag coefficient at zero lift}$$

$$K = \text{effective induced-drag factor.}$$

The values of K obtained from the slopes of the lines are 1.15 at low M , 1.37 at $M = 0.85$ and 1.52 at $M = 0.90$.

The experimental scatter present in Fig. 5 amounts to about $\pm 4\%$ in C_D . This scatter makes the value of K obtained very critical both to the weight that we give each experimental point in drawing the mean lines of Fig. 5 and also to the range of C_L covered. The value of K obtained at low Mach number is the mean over a larger C_L range than at $M = 0.85$ or 0.90 and might therefore be expected to be more accurate.

The flight technique whereby drag is measured at various Mach numbers at a series of fixed values of C_D results inevitably in a variation of Reynolds number. It so happens that the change in Reynolds number with Mach number at constant C_L is relatively small (Fig. 5), but with increasing C_L at constant M the reduction in Reynolds number is quite large (Fig. 6a). The values of K obtained from Fig. 6a thus include any effects on total drag arising from these Reynolds number variations. An attempt has been made to reduce the results to a constant Reynolds number of 34×10^6 by using R.Ae.S. Data Sheets and assuming that only the drag at zero lift is affected by Reynolds number¹⁵. In making this correction, transition was assumed to be at the leading edge of

the wings and tail and at the nose of the body, and the surfaces were assumed to be aerodynamically smooth (Section 4.1). The values of C_{DT} so corrected are shown plotted in Fig. 6b. The values of K obtained are as follows:

M	K	
	Uncorrected for R (Fig. 6a)	Corrected to $R = 34 \times 10^6$ (Fig. 6b)
Low M	1.15	1.09
0.85	1.37	1.19
0.90	1.52	1.23

The variation of the drag of the complete aircraft with Reynolds number will in practice be rather less than that for an aerodynamically clean aircraft due to the effects of control-surface gaps, skin joints and other surface irregularities (Section 4.1). The true values of K at constant Reynolds number will thus probably lie somewhere between the two extremes given above.

The value of 1.09 for K at low Mach number compares with 1.1 for the Supermarine 510, 1.25 for the DH.108, and 1.33 for the Hawker P.1052, all values being corrected to constant R (Ref. 15). The reason for this large variation of K from aircraft to aircraft is not readily apparent.

Fig. 7 presents a plot of C_D versus C_L^2 showing the results of Fig. 5 extended to higher C_L 's by additional stabilised levels and by partial glides. Note that no correction for Reynolds number has been applied, because of the uncertainty in applying this at high C_L 's. The C_D/C_L^2 curve is seen to be linear up to a certain C_L , above which the drag increases rapidly and departs more and more from the linear value. This drag increase results from the occurrence and subsequent spread of separated flow on various parts of the aircraft. The drag rise commences earlier as Mach number increases, confirming the well known result that separation also occurs at an earlier C_L . The values of C_L for the onset of buffet (as obtained from unpublished R.A.E. tests) are also shown plotted in Fig. 7. It is seen that the drag rise does not become apparent to the pilot as buffet until the drag has risen by a finite amount. A larger drag rise is necessary at low M than at high M , probably because of the lower E.A.S. and hence lower intensity of buffet.

At transonic and supersonic speeds a small range of C_L from about 0.05 to about 0.20 was covered in dives and pull-outs. This has enabled some approximate values of K to be obtained at supersonic speeds, and the results are given in Fig. 8. It is seen that the results are in fairly good agreement with the empirical data of Ref. 16. The measured values of K beyond $M = 1.0$ are of the same magnitude as those that would be expected for the wing alone with no leading-edge suction, $\{K = \pi A / (\partial C_L / \partial \alpha)_{\text{wing}}\}$. This suggests that if the drag due to lift on the fuselage and tail were negligible the high values of K on the *Hunter* could be explained by the loss of virtually all the leading-edge suction on the wing beyond $M = 1.0$, although this result would be rather surprising.

It should be emphasised that the actual values of K derived from these dives and pull-outs are dependent largely upon the values of α_0 and $\partial C_L / \partial \alpha$ that are assumed, errors in these two quantities

having an appreciable effect on K (Appendix). However, it is of interest to note that any errors in $\partial C_L/\partial\alpha$ alone would not be expected to influence the general result, noted above, that $K \approx \partial C_L/\partial\alpha$, although the picture could be altered by errors in the assumed values of α_0 .

4.3.2. *Drag at C_L 's of 0 and 0.1.*—The established level results at $C_L = 0.1$ (Fig. 5) are shown in Fig. 9 extended to transonic and supersonic speeds by dives using the accelerometer technique. As steady dives at $C_L = 0.1$ were not found possible beyond $M = 1.05$, the drag from $M = 1.05$ to 1.23 was obtained from dives and pull-outs, the results being reduced to $C_L = 0.1$ by assuming the values of K given in Fig. 8.

Fig. 9 shows that the drag obtained from stabilised levels agrees closely with that obtained from the dives. The drag coefficient at $C_L = 0.1$ is seen to commence to rise soon after $M = 0.8$, the drag increasing rapidly between $M = 0.92$ and 0.99 and attaining a peak value of 0.0565 at $M = 1.15$. Further increase of Mach number up to $M = 1.23$ causes a slight reduction in C_D .

Also shown in Fig. 9 is the zero-lift drag coefficient obtained by using the values of K given in Fig. 8 to extrapolate the results from $C_L = 0.1$. The low Mach number value of C_{DZ} is seen to be about 0.0125 (at $R = 34 \times 10^6$). This rises to a peak value of 0.0545 at $M = 1.15$.

4.3.3. *Accelerated and decelerated levels.*—The results obtained from an accelerated and a decelerated level at both 15 000 ft and 40 000 ft are given in Fig. 10. Also plotted, where appropriate, are the values derived from the results of stabilised levels (Fig. 5). The extent of the agreement with stabilised levels is illustrated more clearly in Fig. 11, where the results have been reduced to C_{DZ} by assuming the values of K given in Fig. 6a.

It is seen that, although the general agreement with stabilised levels is reasonable, the scatter is large. This large scatter arises mainly from the difficulty of fairing the readings of A.S.I. and altitude and of drawing tangents to these fairings. This difficulty is accentuated by the hysteresis lag of the standard altimeter making it impossible to detect rates of change of altitude within this hysteresis band. The skill of the pilot in maintaining altitude strictly constant plays a large part in obtaining good results from this method.

It is of interest to note that the four runs shown in Fig. 10 were accomplished in one flight. In the same amount of flying time only about four stabilised level points could have been produced. The argument for using accelerated levels therefore lies in the large amount of data (of admittedly limited accuracy) that can be produced in a small number of flying hours. Thus one flight or so consisting of a good accelerated level at, say 10 000, 20 000, 30 000 and 40 000 ft would enable us to deduce

- (a) the variation of C_{DZ} up to the maximum level-flight Mach number
- (b) the level-flight thrust boundaries of the aircraft for the engine settings and altitudes chosen.

In deriving this data a value for K would need to be assumed or estimated. A further assumption with regard to (b) would be that the intake efficiency did not vary appreciably with C_L . The accuracy with which the data could be obtained and the number of flights necessary would depend largely upon the skill of the pilot.

Decelerated levels are not in general of great value as the intakes are working under unrepresentative conditions, possibly leading in some cases to an appreciable increase in spillage drag. Further inspection of Figs. 10 and 11 suggests that the decelerated levels give in general a slightly higher drag for the *Hunter* than do the accelerated levels. This difference however may be due largely to experimental inaccuracies.

4.3.4. *Comparison of flight and wind-tunnel results.*—Fig. 12 compares the high Mach number drag rise obtained from flight tests with that obtained from high-speed wind-tunnel tests⁹. The model used in the wind-tunnel tests was without tail and, as the tests were made several years ago, was not completely representative of the full-scale aircraft. The main differences were that on the model the tip sections were 10% thick and the sweep 42.5° . The drag rise is seen to compare well at low C_L 's but to commence progressively earlier in flight than in the tunnel as C_L is increased. This is contrary to other comparisons¹⁷ between wind-tunnel data at low Reynolds number and flight data. It is felt that the relatively good agreement at low lift shown in Fig. 12 may be largely fortuitous in view of the large and unpredictable scale effects²⁰ to be expected on transition-free model tests at Reynolds numbers as low as 0.5×10^6 .

The values of effective induced-drag factor, K , obtained from various low Mach number wind-tunnel tests are shown in Fig. 13 plotted against Reynolds number. Except where otherwise stated, the tests are all with transition free. All the results shown are for configurations similar to, if not identical to, that of the *Hunter*. Also shown in Fig. 13 is the value of K obtained from the present flight tests. It is seen that apart from the isolated point at $R = 0.5 \times 10^6$, the tunnel results agree well amongst themselves, the mean value of K decreasing from 1.30 to about 1.08 as Reynolds number is increased from 1.4×10^6 to 10×10^6 . At the highest Reynolds number attained in the tunnel tests the value of K is of the same order as that obtained from the flight tests.

The high values of K at low Reynolds numbers are probably the result of changes in profile drag due to forward movement of transition as C_L is increased. The considerably reduced value when transition is fixed at a forward position tends to confirm this.

4.4. *Level-Flight Performance.*

Fig. 14 shows the level-flight performance of the *Hunter* Mk. I plotted in non-dimensional form. The experimental points shown are derived from further analysis of the flight data which was obtained for determination of the stabilised level results shown in Fig. 5. The performance carpet has been plotted with C_L as one of the variables instead of the more usual W/P , but it is a simple matter to convert one into the other as $W/P \propto C_L M^2$.

5. *Conclusions.*

Flight tests made to measure the drag of a Hawker *Hunter* F Mk. I aircraft give the following results:

- (i) C_{DZ} at low Mach number at $R = 34 \times 10^6$ is 0.0125.
- (ii) At $C_L = 0.1$, a gradual drag rise commences soon after $M = 0.8$, the drag increasing rapidly beyond $M = 0.92$ and attaining a peak value of C_D of 0.0565 at $M = 1.15$. Further increase of Mach number up to 1.23 causes a slight reduction in drag. Comparison of the compressibility drag rise obtained from wind-tunnel tests and from flight shows good agreement, although this may be largely fortuitous in view of the low tunnel Reynolds number.
- (iii) The C_D/C_L^2 curve becomes non-linear at the higher C_L 's, the C_L for divergence decreasing with increase in Mach number. At $M = 0.3$ the divergence C_L is 0.76 falling to 0.41 at $M = 0.70$. Over the low C_L range at low Mach number the effective induced-drag factor K corrected to constant Reynolds number is 1.09.

(iv) Some approximate values of K at supersonic speeds suggest that virtually all the leading-edge suction on the wing is lost beyond $M = 1.0$.

(v) The accelerated and decelerated levels technique gives values of C_{DZ} similar to those obtained from stabilised levels although the scatter is large.

(vi) The lift-curve slope of the complete aircraft increases from 3.5 at $M = 0.3$ to 4.6 at $M = 0.9$. The zero-lift angle is about 0.4° . Wind-tunnel and flight measurements of lift-curve slope are in reasonable agreement when allowance is made for differences in geometry and in Reynolds number.

NOTATION

p_a	Ambient air pressure (lb/sq. in.)
p_0	Sea-level air pressure (lb/sq. in.)
P	Ambient air pressure ratio = p_a/p_0
V_i	Equivalent airspeed (knots)
T_a	Ambient air temperature at pressure altitude ($^{\circ}$ abs.)
T_0	Sea-level air temperature (288 $^{\circ}$ abs.)
$\theta =$	T_a/T_0
M	Mach number
W	Weight of aircraft (lb)
S	Gross wing area (sq. ft)
A	Wing aspect ratio
$\lambda_{c/4}$	Sweepback of wing quarter-chord line
t/c	Thickness-chord ratio parallel to free stream
C_L	Overall aircraft lift coefficient
C_{DZ}	Drag coefficient at zero lift
C_{DT}	Total drag coefficient
	$= C_{DZ} + \frac{KC_L^2}{\pi A}$
K	Effective induced-drag factor
α	Wing incidence measured from wing datum
α_0	Wing incidence for zero lift
$\left(\frac{\partial C_L}{\partial \alpha}\right)_M$	$=$ Lift-curve slope at constant M
N	Engine r.p.m.
R	Reynolds number based on wing S.M.C. (unless otherwise stated)
$\frac{dh}{dt}$	Rate of change of true altitude.

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APPENDIX

Effects of Errors in Incidence on the Accuracy of Drag Measurements using the Accelerometer Technique

It can be shown from the equations of Ref. 1 that, to a first approximation

$$C_D = \frac{F_N + WR}{qS} + C_L\phi$$

where

F_N = Nett thrust

W = Weight of aircraft

R = Longitudinal accelerometer reading

ϕ = Incidence of fuselage datum to flight path (radians).

Thus an error $\Delta\phi$ in incidence gives rise to an error of $C_L \Delta\phi$ in C_D . The accuracy of drag measurements using the accelerometer technique is thus closely related to the accuracy of the values of incidence that are assumed.

In this report, the drag at transonic and supersonic speeds has been derived using estimated values of incidence. The following table gives some idea of the effects of errors in the estimated values used for lift-curve slope and no lift angle at supersonic speeds.

Error in estimated value of incidence	Resulting error in	
	C_D at $C_L = 0.1$	K
$\pm \frac{1}{2}^\circ$ in α_0	± 0.0009	± 0.5
+ 50% in $\partial C_L / \partial \alpha$	-0.0022	-2.3
- 50% in $\partial C_L / \partial \alpha$	$+0.0007$	$+0.8$

It can be seen that quite large errors in incidence can be tolerated without seriously impairing the accuracy of C_D at $C_L = 0.1$. This is particularly true when C_{DZ} is obtained from measurements of C_D at two or more C_L 's, as these errors in $\partial C_L / \partial \alpha$ can be shown to cancel.

The above table also shows that K is very critical to errors in α_0 and $\partial C_L / \partial \alpha$. It would appear that accurate values of K can only be obtained with the accelerometer technique if incidence is measured directly in flight or can be estimated from reliable experimental data.

TABLE 1

*Details of Hunter WT.571**Aircraft*

Wing area	340 sq. ft
Wing span	33 ft 8 in.
Aspect ratio	3.33
Taper ratio	0.41
Sweepback at quarter-chord	40°
Standard mean chord	10.1 ft
Wing setting to fuselage datum	1½°
Max. thickness/chord ratio (symmetrical)	8.5%
Position of max. <i>t/c</i>	37.5% chord
A.U.W. (Take-off)	15 520 lb
Fuel contents	334 gal
C.G. position at take-off	0.298 \bar{c}
C.G. position with rear tanks empty (274 gal left)	0.270 \bar{c}
C.G. position with rear and centre tanks empty (202 gal left)	0.267 \bar{c}
C.G. position no fuel	0.314 \bar{c}

Engine

Rolls Royce Avon 107 RA7

Nominal static thrust at sea level

7500 lb

The operational limitations of the engine are as follows:

	<i>r.p.m.</i>	<i>Max.</i> <i>J.P.T.</i>	<i>Time Limit</i>
Take-off and operational necessity	7950	680°C	10 min
Max. intermediate	7750	620°C	30 min
Max. continuous	7500	575°C	Unrestricted

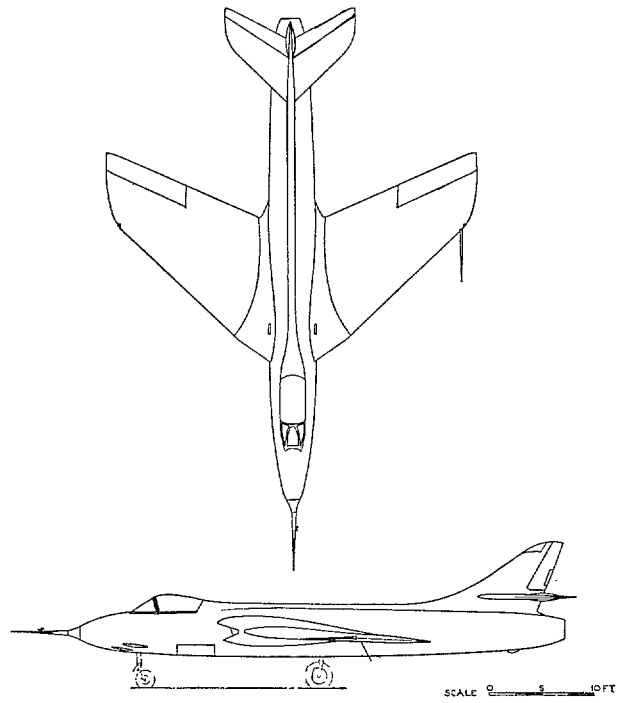


FIG. 1. General arrangement of Hawker *Hunter*
F. Mk. I (WT.571).



FIG. 2. General view of *Hunter* WT.571.

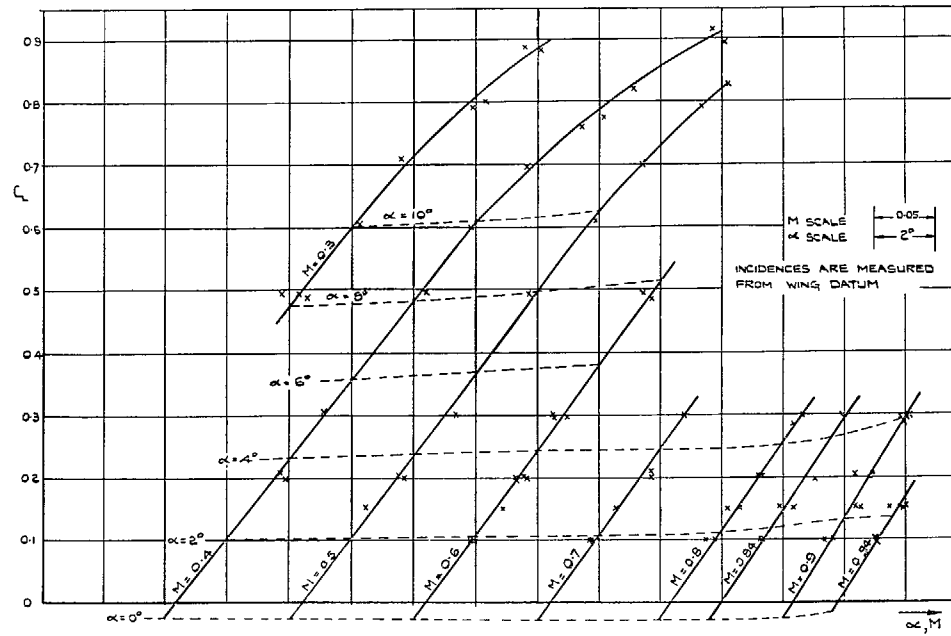


FIG. 3. Lift carpet for aircraft trimmed at $0.27\bar{c}$ mean c.g.

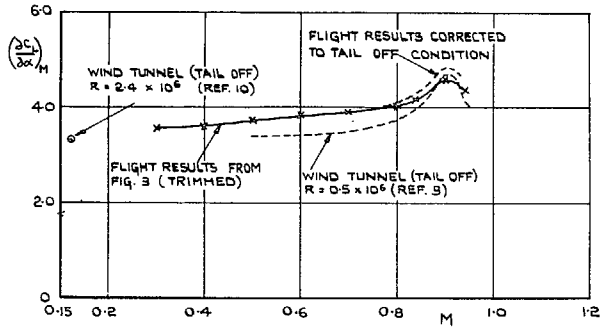


FIG. 4a. $(\partial C_L / \partial \alpha)_M$ vs. M —comparison of flight and tunnel results.

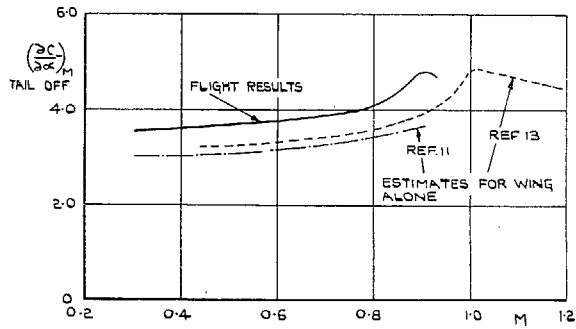


FIG. 4b. $(\partial C_L / \partial \alpha)_M$ vs. M —comparison of flight tests with estimates (tail off).

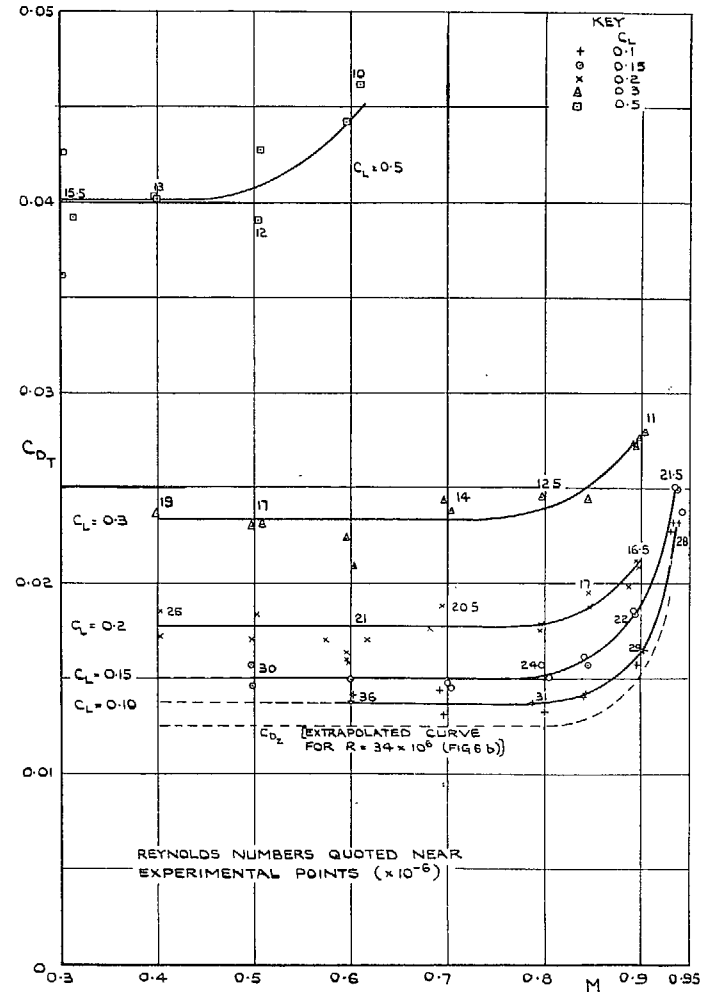


FIG. 5. Drag obtained from stabilised levels.

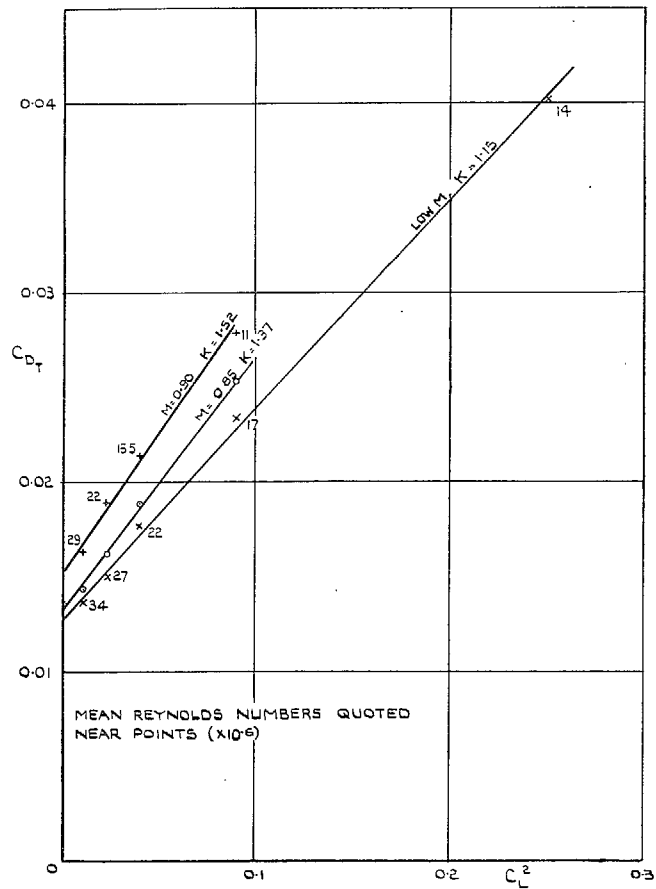


Fig. 6a. Drag coefficient vs. C_L^2 —results derived from FIG. 5.

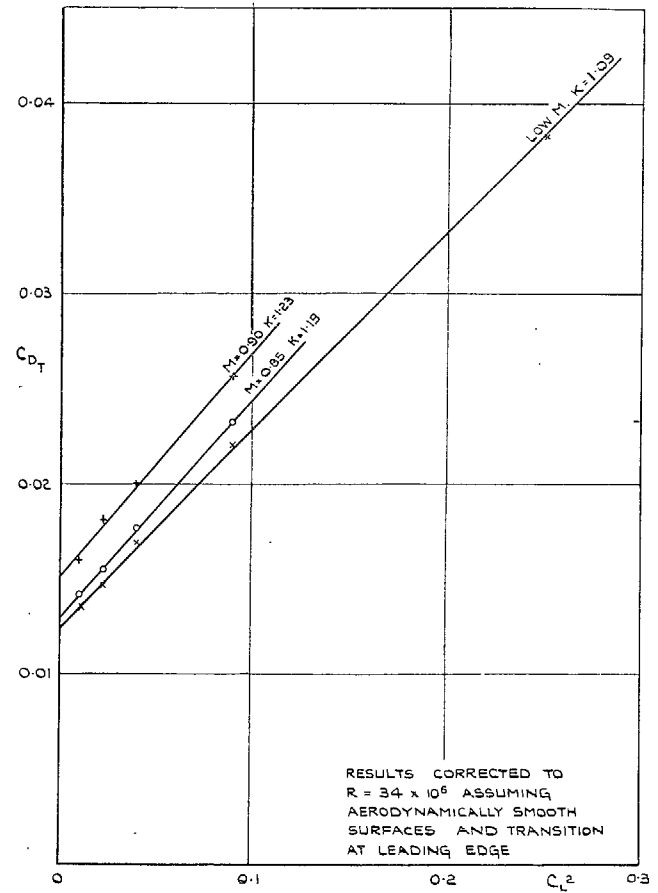


Fig. 6b. Drag coefficient vs. C_L^2 —results of FIG. 6a corrected to $R = 34 \times 10^6$.

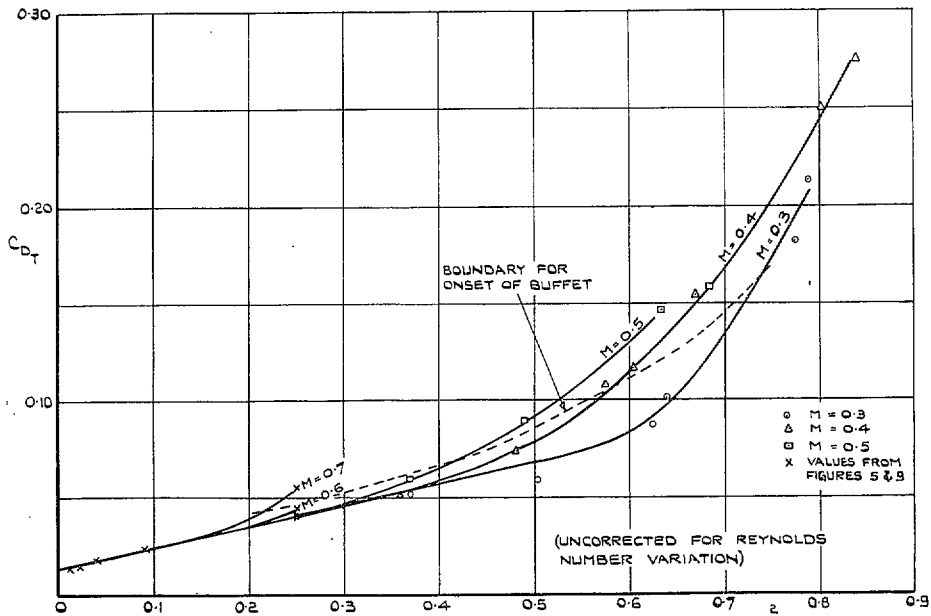


FIG. 7. Drag coefficient vs. C_L^2 at high C_L 's.

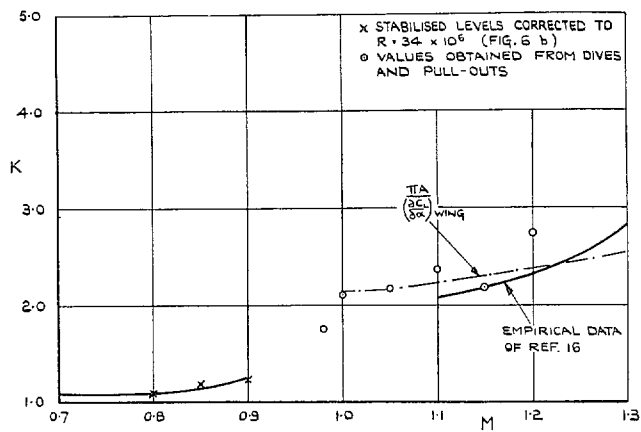


FIG. 8. Variation of effective induced-drag factor with Mach number.

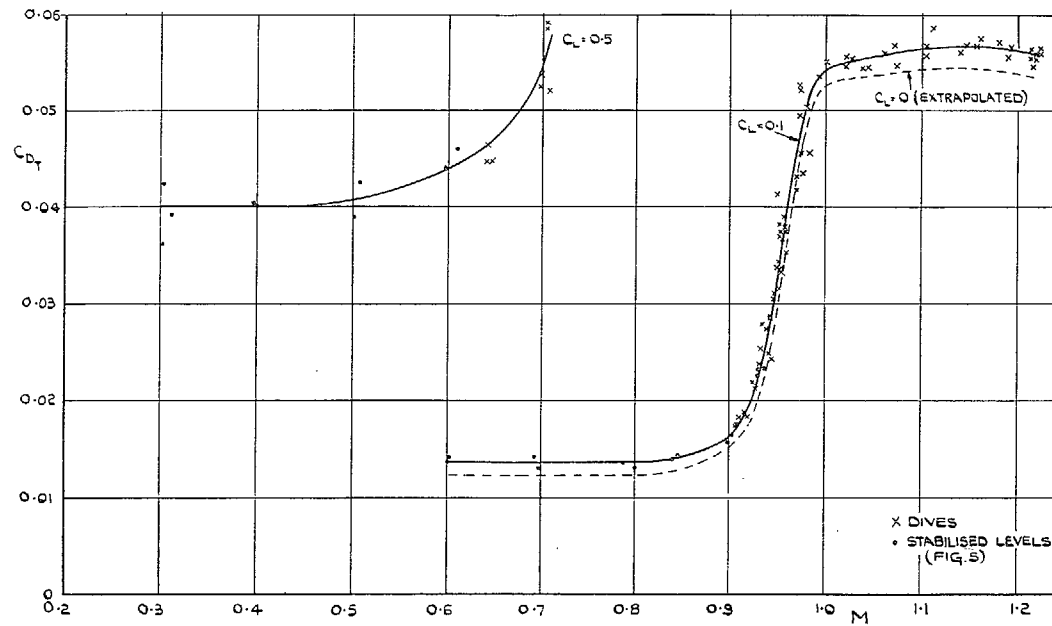


FIG. 9. Drag obtained from dives using accelerometer technique.

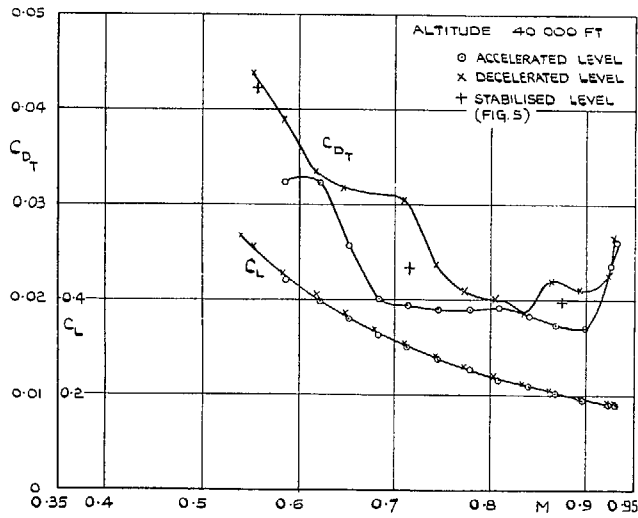
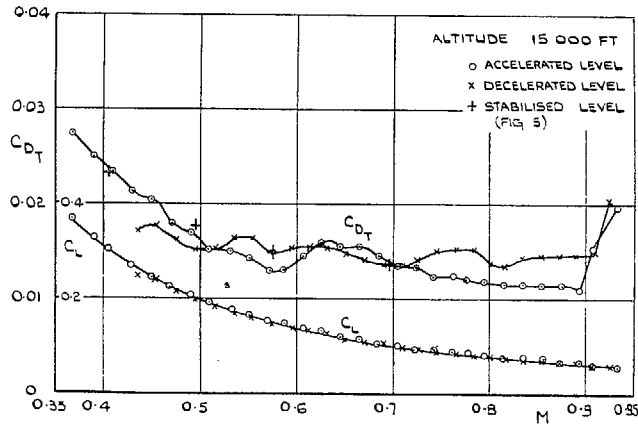


FIG. 10. Results obtained from accelerated and decelerated levels.

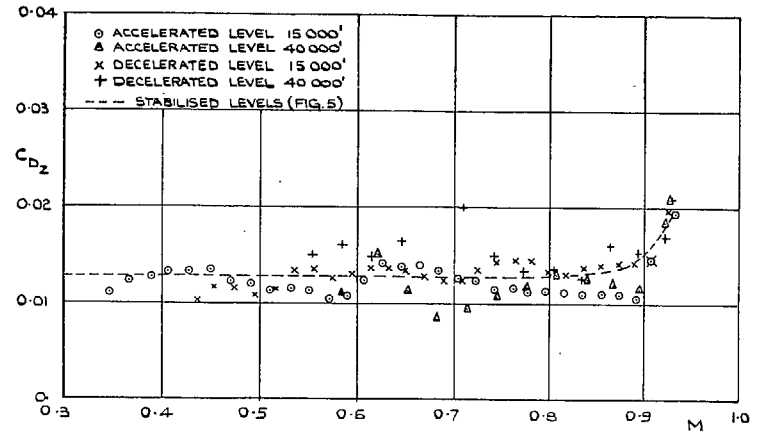


FIG. 11. C_{DZ} derived from accelerated and decelerated levels compared with that from stabilised levels.

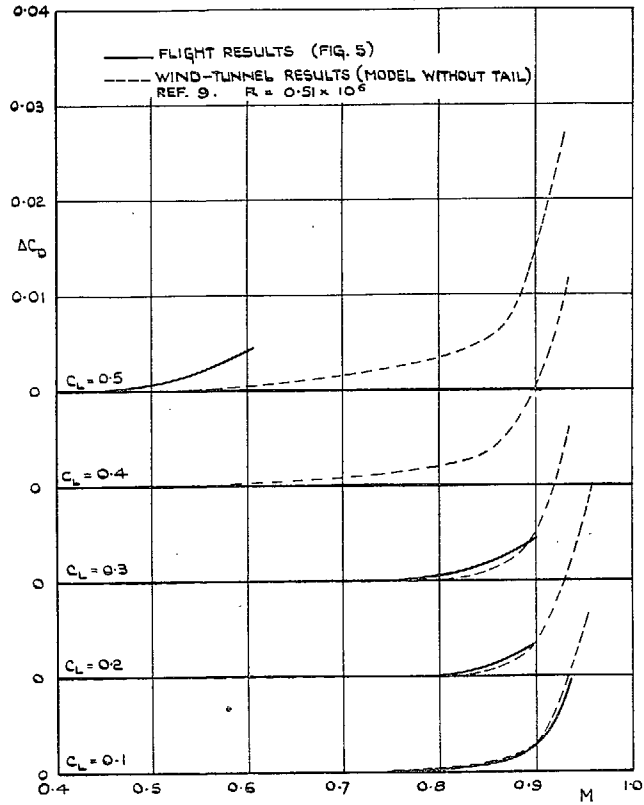


FIG. 12. Comparison of drag rise with Mach number from flight and wind-tunnel tests.

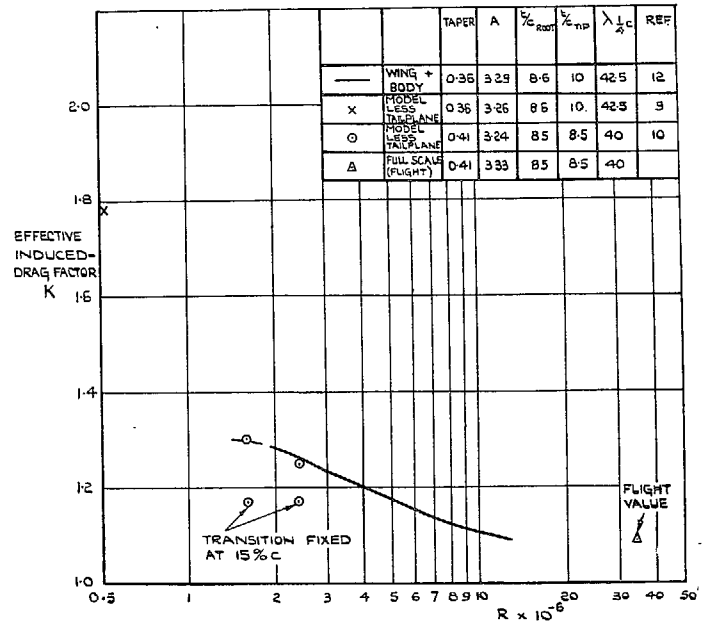


FIG. 13. Comparison of flight and wind-tunnel induced-drag data at low M .

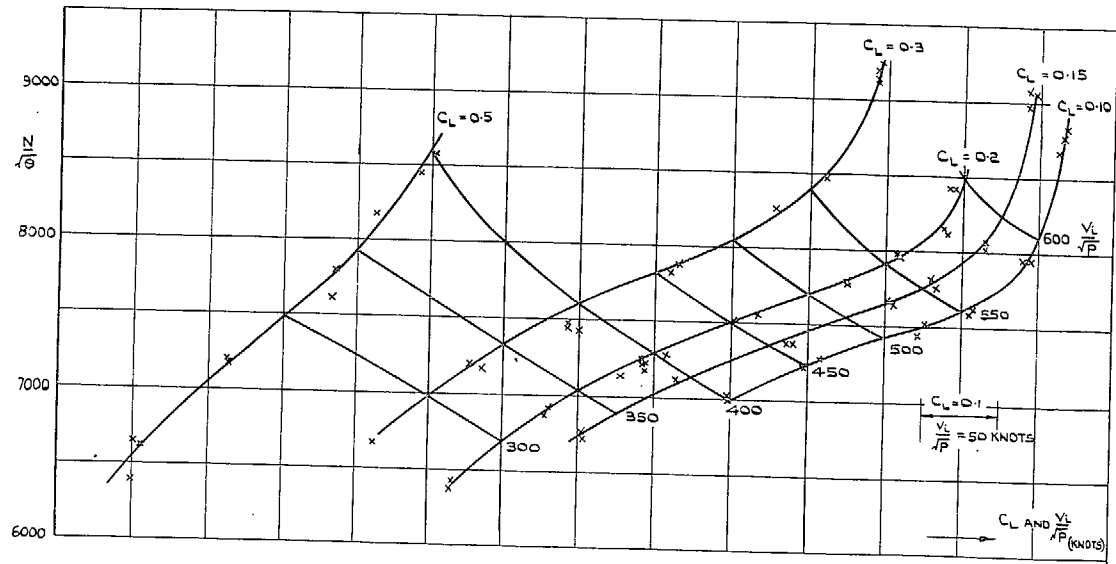


FIG. 14. Hunter F. Mk. I.—level-flight performance carpet.

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