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By

J. WILLIAMS, M.Sc., Ph.D.

Part I

A Comparison of the Stalling Properties of some Thin
Nose-Suction Aerofoils

Part II

A Theoretical Investigation on Thin High-lift Aerofoils
Specially Designed for Nose-Slot Suction

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Summary.—The stalling properties of some thin nose-suction aerofoils already tested have been examined, and further theoretical investigations have been carried out on thin aerofoils specially designed to give high lift with nose-slot suction.

In Part I, the experimental results from stalling tests on thin nose-suction aerofoils are compared and the design features of the tested aerofoils are analysed. The aerofoils include the 8 per cent thick Lighthill and Glauert sections specially designed for nose-slot suction, the 8 per cent thick H.S.A. V section with distributed suction through a porous nose, and some conventional sections of moderate thickness tested in Germany with slot suction at various positions on the nose. The Lighthill and Glauert aerofoils proved quite good without suction, but the increments in $C_{L\max}$ due to suction were rather disappointing. The H.S.A. V aerofoil with distributed suction promises to be more economical as regards suction quantities for delaying the stall at full-scale Reynolds numbers, but this needs further confirmation.

Part II describes a theoretical exploration of possible thin nose-slot aerofoils specially designed to have an abrupt fall in velocity where suction is to be applied on the upper surface of the nose. In an attempt to obtain better sections as regards a late stall at practical suction quantities, various symmetrical and cambered shapes were designed by a simple approximate method and the effect of sink action was also estimated. Low-speed stalling tests are to be made on one of the new cambered sections (D.2/4) in order to determine whether the considerable improvements expected are in fact achieved. The effect of the unusual nose shape on the high-speed performance of the section will also need to be examined.

The theoretical formulæ required for the calculation of the velocity distribution and lift of an aerofoil with a sink on its surface, and some detailed notes on the design of the Glauert nose-slot aerofoil, are given in the Appendices.

PART I

A Comparison of the Stalling Properties of some Thin Nose-Suction Aerofoils

1. *Introduction.*—Suction at the nose of a thin aerofoil may be employed to delay the stall to a higher incidence and increase the maximum lift. Three thin nose-suction aerofoils have been tested in a 4-ft (National Physical Laboratory) wind tunnel at low airspeeds^{1, 2, 3}, the Lighthill and Glauert aerofoils with slot suction, and the H.S.A. V aerofoil with distributed suction through a porous nose. The shapes of these aerofoils are shown in Fig. 1, and the results from the stalling tests are compared in Fig. 2. Some conventional aerofoils of moderate thickness, with slot suction at various positions on the nose, have been tested in Germany at low airspeeds⁴. In view of the German results (*see* Table 1), a theoretical examination has been carried out here of the effect of a sink located on the nose of a thin aerofoil (H.S.A. V) with a large nose radius.

$C_{L\max}$ and α_{\max} denote the values of the lift coefficient C_L and the incidence α at which C_L first ceases to increase with α ; the incidence is measured from the zero-lift attitude (without suction), except in the case of the German results. In the diagrams and tables, the velocity q on the aerofoil is given as a fraction of the velocity of the undisturbed stream, and the chordwise

distance x from the leading edge as a fraction of the chord. The curves given in the present report for the thin nose-suction aerofoils tested in the 4-ft wind tunnel are not corrected for wind-tunnel interference; the correction to $C_{L\max}$ is believed to be small.

2. *The Lighthill and Glauert Slot-Suction Aerofoils.*—The shapes of the Lighthill and the Glauert slot-suction aerofoils were calculated by an exact method^{5*}. At an upper design incidence, they were designed to have on the upper surface a large steep fall in velocity at the nose, followed by a low steady adverse gradient back to the trailing edge. To prevent separation at the steep velocity fall, the boundary layer is removed through a narrow slot; the adverse velocity gradient aft of the slot is assumed to be insufficient at the upper design incidence to cause separation of the boundary layer behind the slot. The suction quantity required to prevent stalling at and below the design incidence, therefore, should be small. The stall can be delayed to higher incidences by sink action at the slot sufficient to prevent an increase in the adverse gradient aft of the slot, but the suction quantities required are large. The steep velocity fall chosen for the Lighthill aerofoil was a discontinuous drop at the leading edge, from an infinite to a low velocity, and consequently the aerofoil has a sharp beaked nose. The effect of a narrow slot at the leading edge was not allowed for in the calculations. The Glauert aerofoil has a thin rounded nose with a narrow slot on its upper surface. To enable the slot to be included automatically in the aerofoil shape, the theoretical velocity distribution was assigned for a chosen sink strength.

Experimental and Theoretical Results.—Fig. 2 gives measured values of $C_{L\max}$ and α_{\max} plotted against C_q , and Fig. 3 shows some typical lift *vs.* incidence curves at various C_q values. The $C_{L\max}$ for both aerofoils without suction is about 1.12, and with suction $C_{L\max}$ increases to about 1.6 for $C_q = 0.012$. The values of α_{\max} without suction are about $13\frac{1}{2}$ deg and $12\frac{1}{2}$ deg for the Lighthill and Glauert respectively; with suction, these values each increase by about 4 deg for $C_q = 0.012$. Unfortunately, the results from the stalling tests are insufficient for a direct comparison of the two aerofoils at other C_q values. It seems probable that, for a low value of C_q (boundary-layer suction only), the $C_{L\max}$ of the Glauert aerofoil would be the higher in view of the improved nose shape. With $C_q > 0.012$, when sink action predominates, the values of $C_{L\max}$ for the two aerofoils should not differ markedly, as the adverse velocity gradients over the aerofoil upper surfaces at a high incidence are very similar (*see* Fig. 4). The theoretical velocity distribution over the upper surface of the Lighthill aerofoil at a high incidence is shown in Fig. 5 for various sink strengths at the leading edge. It is seen that large sink strengths are necessary to reduce appreciably the adverse velocity gradients.

Fig. 3 shows that the stall is in all cases reasonably gentle. The slope of the experimental lift curves at *low* incidence, when reduced by the factor of 6 per cent to allow for wind-tunnel interference, is about 5.7 per radian for both aerofoils, about 14 per cent lower than the theoretical value of 6.6. It is noticeable that at high incidences below the stall the lift slope is lower for the Lighthill aerofoil than for the Glauert. The flow over the Lighthill aerofoil at incidences just below the stall was investigated by experiments with surface streamers; these tests were not reported in R. & M. 2355¹. Without suction, the flow separated at the slot but became reattached further along the upper surface, and the position of reattachment moved rearwards as the incidence was increased. With $C_q \geq 0.010$, separation occurred first at the rear of the upper surface and the separation point moved forward as the incidence was increased; no reattachment was evident.

The theoretical values of M_{crit} for the Lighthill and Glauert aerofoils without suction are respectively 0.73 and 0.72 at zero lift, and 0.68, 0.70 respectively, at 2 deg incidence from zero-lift[†]. The velocity gradients over the aerofoils at low incidences remain favourable for only a short distance from the leading edge (*see* Fig. 6).

* The design of the Glauert slot-suction aerofoil has not previously been reported in detail, and is given in Appendix II of the present report.

† Deduced by means of the Kármán compressibility correction for results from incompressible flow; large theoretical velocities in the immediate neighbourhood of the slot are disregarded.

The theoretical and experimental velocity distributions without suction are compared in Fig. 7 for the Lighthill aerofoil and in Fig. 8 for the Glauert aerofoil.

3. *The H.S.A. V Aerofoil with Distributed Suction.*—Thwaites designed the H.S.A. V aerofoil by the approximate method⁶. The velocity distribution at low incidence (see Fig. 6) was chosen from novel low-drag considerations which have not yet been tested experimentally. The aerofoil has an extremely large nose radius, $0.03c$ and consequently the adverse velocity gradients over the nose at high incidence are much less severe than for a normal thin aerofoil. The boundary layer is kept thin and separation from the upper surface prevented, at high incidences, by distributed suction through a porous area (Porosint) over the nose. In early tests the porous area extended to $0.15c$ from the leading edge on both the upper and lower surfaces, but later the area was reduced to a half.

Experimental and Theoretical Results.—According to approximate theoretical arguments, the value of C_0 required to provide a given increment in C_L at a constant incidence varies with the Reynolds number as $R^{-1/2}$. This was roughly confirmed by the model tests, but experimental verification over a wider range of Reynolds numbers is needed before the results of the model tests can be safely extrapolated to full-scale Reynolds numbers.

Fig. 2 gives the largest values of C_L measured for $\alpha \leq 15$ deg, plotted against C_0 ; $C_{L \max}$ and α_{\max} are available only for low values of C_0 . Without suction, $C_{L \max} = 0.87$ and $\alpha_{\max} = 10$ deg when $R = 0.58 \times 10^6$. With suction through the full Porosint area and $C_0 = 0.0019$, $C_{L \max} = 1.10$ and $\alpha_{\max} = 14\frac{1}{2}$ deg at the same R . When $C_0 = 0.0047$, $R = 0.24 \times 10^6$, and $\alpha = 15$ deg, $C_L = 1.20$ for suction through the full Porosint area and $C_L = 1.39$ for suction through the reduced Porosint area; in both cases C_L was still increasing with incidence. An approximate calculation of the corresponding results at $\alpha = 15$ deg and $R = 0.58 \times 10^6$ gives $C_L = 1.14$ and 1.33 for $C_0 = 0.003$ [$\equiv 0.0047 \times \sqrt{(0.24/0.58)}$], with suction through the full and the reduced areas respectively*. The Porosint areas used in the experiments and the experimental C_0 values required are much larger than those estimated theoretically, but the velocity into the Porosint is in fair agreement with the theoretical estimate. Therefore, it seems likely that even lower values of C_0 would suffice if the porous area were reduced further.

The flow over the aerofoil was investigated at incidences just below the stall. Both without suction and with suction, the flow separated on the upper surface of the nose but became reattached some distance aft. The complete stall appeared to develop from rearward movement of the position of reattachment.

The slope of the experimental lift curves at low incidences, when reduced by the factor of 6 per cent to allow for wind-tunnel constraint (lift effect), is about 5.3 per radian, about 22 per cent lower than the theoretical value of 6.8.

The theoretical M_{crit} of the H.S.A. V aerofoil without suction has the values 0.68 and 0.52 for the incidences of 0 deg and 2 deg respectively. However, as the theoretical velocity distributions consist of a peak at the nose followed by an almost constant velocity back to mid-chord, the effect of shock waves on the drag may not be marked until Mach numbers much higher than the M_{crit} are reached (see R. & M. 2242⁶).

4. *Conventional Aerofoils with Slot Suction.*—The results from German tests on three moderately thick conventional aerofoils with slot suction are summarised in Table 1. The $C_{L \max}$ and α_{\max} , for a given aerofoil and constant value of C_0 , vary extensively with the location of the slot on the upper surface, and the slot position giving the highest $C_{L \max}$ differs from that for the highest α_{\max} †. The best position of the slot (either in respect of $C_{L \max}$ or α_{\max}) is different for each aerofoil,

* From the experimental results, it appears that the C_L without suction for $\alpha = 15$ deg decreases by 0.06 when R is increased from 0.24×10^6 to 0.58×10^6 ; the difference between the C_L with and without suction at a given incidence is assumed to be independent of R provided $C_0\sqrt{R}$ remains constant.

† It is relevant to note that, theoretically, the introduction of a sink on the upper surface increases the circulation (and hence lift) at a given incidence, by an amount which vanishes as the sink is placed closer to the leading edge.

being nearest the leading edge for the aerofoil with the smallest nose radius. It appears, from these tests, that a *large* nose radius is conducive to high $C_{L\max}$ and α_{\max} without suction, and to large increments by means of slot suction.

Fig. 9 shows the theoretical velocity distribution over the upper surface of H.S.A. V at a high incidence, when a sink of strength $C_q = 0.01$ is located at various positions on the upper surface of the nose. The velocity first rises from the stagnation point on the lower surface of the nose, but may fall again before ultimately rising to its infinite value at the sink. The magnitude of this velocity fall diminishes as the sink is placed closer to the leading edge and vanishes when the sink is very near to the leading edge. Immediately behind the sink there is a stagnation point. The velocity gradient is afterwards favourable for a short distance until a finite velocity maximum is reached, and then remains adverse right back to the trailing edge. The velocity fall, from the maximum to the value at the trailing edge, increases as the sink is placed nearer to the leading edge. Thus, in practice, a very careful choice of slot position is necessary so that the stall may be delayed to the highest possible incidence. The curves in Fig. 9 give a very rough idea of the gains feasible by slot suction on H.S.A. V. For example, the adverse velocity gradients over the upper surface at an incidence of 12.7 deg ($C_L = 1.5$) and a sink strength $C_q = 0.01$ at 0.006 of the chord from the leading edge are clearly less severe than those for an incidence of 8.7 deg ($C_L = 1.0$) and no sink action.

5. *Concluding Remarks.*—The Lighthill and the Glauert slot-suction aerofoils do not differ appreciably, either in their stalling characteristics (see Figs. 2 and 3) or in their velocity distributions at low incidences (see Fig. 6). The gains in $C_{L\max}$ and α_{\max} due to suction are poor, but the values of $C_{L\max}$ and α_{\max} without suction are quite high considering the steep fall in the theoretical velocity at the nose. The H.S.A. V aerofoil with distributed suction through the proper area of porous surface at the nose promises to be more economical than these slot-suction aerofoils as regards suction quantities for the postponement of the stall at full-scale Reynolds numbers. But this requires further confirmation by tests at high Reynolds numbers, and the respective power requirements also need investigation.

The thin slot-suction aerofoils already tested were specially designed to have, on the upper surface at high incidences, a large steep fall in velocity at the nose slot followed by a low steady adverse velocity gradient aft of the slot back to the trailing edge. For comparison, tests on a thin *conventional* aerofoil, with sink action at a nose slot to reduce the adverse velocity gradients at high incidences, would be very useful; the nose radius should be large and the slot position carefully chosen (see Section 4).

Some drag tests on thin nose-suction aerofoils at high speeds are also needed, as adverse effects on the drag due to the slot or to the porous surface may arise. Such effects may possibly be removed by a small amount of suction, in which case the economy of this procedure must be carefully considered.

For a fair assessment of the practical value of thin nose-suction aerofoils, their characteristics should be compared, in the first instance, with those of a thin conventional aerofoil incorporating a normal (non-suction) device at the nose to delay the stall to a higher incidence. Since nose devices usually have moveable parts and may lead to nose shapes which are poor from a low-drag standpoint, nose-suction aerofoils may be preferable for high speed aircraft. The use of nose-suction aerofoils, at the outboard sections of swept-back wings, is now being considered for the prevention of early tip-stalling. In this connection, tests under three-dimensional flow conditions (rather than two-dimensional) are of the utmost importance.

The maximum lift of thin nose-suction aerofoils may be further increased by the introduction of trailing-edge devices. It may be profitable, from this standpoint, for the air sucked in at the nose to be ejected downstream over a trailing-edge flap.

PART II

A Theoretical Investigation on Thin High-Lift Aerofoils Specially Designed for Nose-Slot Suction

6. *Introduction.*—A theoretical exploration of possible thin sections designed to have a large abrupt fall in velocity on the upper surface of the nose at high incidences has been carried out in an attempt to improve on the Lighthill and Glauert sections discussed in Part I.* Approximate theory has been employed to enable a comprehensive survey to be made fairly quickly. Various symmetrical 8 per cent thick shapes were first designed and the effect of camber was initially examined by adding a normal type centre-line. However, with such a centre-line, the aerofoil has an abrupt velocity fall on the lower surface, so new centre-lines were designed specially to eliminate this unnecessary and undesirable feature. The effect of a sink at the abrupt velocity fall was also investigated.

7. *Method of Design.*—The velocity q over an aerofoil (expressed as a fraction of the free-stream velocity) may, on the basis of Goldstein's Approximation I, be expressed in the form⁹

$$q = 1 + g_s \pm \left[g_i + \frac{1}{2} \left(\frac{1}{a_0} + \frac{1}{2\pi} \right) (C_L - C_{L \text{ opt}}) \cot \frac{1}{2}\theta - \frac{1}{2} \left(\frac{1}{a_0} - \frac{1}{2\pi} \right) C_L \tan \frac{1}{2}\theta \right],$$

where the upper (positive) sign refers to the upper surface ($y_c + y_s$) and the lower (negative) sign to the lower surface ($y_c - y_s$), and where the chordwise co-ordinate $x = \frac{1}{2}(1 - \cos \theta)$ is measured from the leading edge. The contribution $1 + g_s$ corresponds to the velocity distribution over the fairing $\pm y_s$ at zero incidence, and is specified here to have a discontinuous fall at the point $x = X_1$ near the leading edge. The centre-line y_c can be designed from a knowledge of g_i .

The velocity distributions chosen for the symmetrical sections at zero incidence, on the basis of Goldstein's Approximation I, are of the form shown in Fig. 10a. The velocity q changes linearly from a value $1 + g_s(0)$ at the leading edge ($x = 0$) to $1 + g_s(X_1)$ at $x = X_1$ where it drops discontinuously to $1 + g_s'(X_1)$; it then increases linearly to a value $1 + g_s(X_2)$ at $x = X_2$ and finally decreases to $1 + g_s(1)$ at the trailing edge. The formulae for calculating the section shape, and the functions arising in Goldstein's Approximations II and III for the velocity distributions, are derived in Appendix III.

Cambered shapes were in the first instance obtained by adding the simple centre-line¹⁰ given in Table 4, which has a continuous g_i , has no negative loading, and has a low value ($-\frac{1}{8}$) for $C_{m0}/C_{L \text{ opt}}$. However, with such a centre-line, the section has an abrupt velocity fall on the lower surface. Clearly, for a continuous velocity distribution over the lower surface, g_i must have a discontinuous fall at $x = X_1$ of the same magnitude as that for g_s . Four centre-lines for use with the most promising fairing shape (D.2) were later designed to have the required discontinuity in g_i at $x = X_1$ and with g_i linear in each of the two segments as illustrated in Fig. 10b. Formulae given in a comprehensive paper by Goldstein on the design of centre-lines¹² were employed to obtain their characteristics. Table 5 lists the basic-design data relating to these four centre-lines, together with the corresponding values obtained for C_{m0} .

8. *Aerofoil Section Characteristics.*—Various symmetrical shapes, of which the four shown in Fig. 11 are typical, were designed by the simple approximate method outlined in Section 7 and Appendix III. The parameter $g_s(X_2)$ controls primarily the maximum thickness; $g_s(1)$ is chosen to give a cusped trailing-edge, and $g_s(0)$, $g_s(X_1)$, $g_s'(X_1)$ determine primarily the shape

* It will be recalled that to prevent separation due to the abrupt velocity fall, the boundary layer is assumed to be removed through a narrow slot there; in addition, sink action at the slot may be used to reduce adverse velocity gradients in the vicinity of the nose.

of the forward part of the aerofoil. An increase in $g_s(0)$ or $g_s(X_1)$ increases ρ_L and the nose thickness, but has little effect on the maximum thickness t and its chordwise position ($x = x_i$) or on the trailing-edge shape. An increase in $g_s'(X_1)$ produces an overall thickening of the forward part of the aerofoil, so that $g_s(X_2)$ has to be decreased to keep t constant, and x_i is slightly reduced. Decrease of X_2 also leads to a reduction in x_i . Data relating to eleven symmetrical sections designed by this simple method are listed in Table 3. For the series A, $X_1 = 0.005$ and $X_2 = 0.35$; for the series B, X_1 remains unchanged but X_2 is decreased to 0.25 ; for the series C, D and E, X_1 takes the values 0.003 , 0.02 and 0.05 respectively, and $X_2 = 0.35$ as at first.

The type of velocity distribution obtained for these sections by means of Approximation III is illustrated in Fig. 10(c). The upper surface velocity distributions* for the symmetrical section A.2, as given by Approximations I, II, and III, are compared in Fig. 13, and it is seen that at high lifts Approximation II is insufficiently accurate over the nose. Table 6 lists the values of the maximum velocities q_{\max} and q'_{\max} in front of and behind the discontinuity, and the values q_1 and q'_1 of the velocity at the discontinuity, calculated by means of Approximation III, for the eleven symmetrical sections at various lift coefficients. Fig. 14 shows the velocity distributions for the four symmetrical sections A.2, A.5, D.2 and E.1 (see Fig. 11) at $C_L = 0$ and $C_L = 1.0$.

Table 7 gives the values of q_{\max} , q'_{\max} , q_1 , and q'_1 for the four cambered sections A.2/N, A.5/N, D.2/N, and E.1/N obtained by adding the normal-type centre-line of Table 4 to the fairing shapes A.2, A.5, D.2, and E.1 respectively, and for the four cambered sections D.2/1, D.2/2, D.2/3, and D.2/4 (see Fig. 12) obtained by adding the discontinuous-type centre-lines of Table 5 to the fairing shape D.2.

The effect of a sink, located at the upper surface velocity discontinuity, on the velocity distributions at high lifts is illustrated in Fig. 10d. The velocity first rises from a zero value at the stagnation point on the lower surface of the nose to a maximum value q_{\max} on the upper surface of the nose but may fall again to a minimum q_{\min} before ultimately rising to its infinite value at the sink. Immediately behind the sink there is a stagnation point, aft of which the velocity gradient is favourable for a short distance until a maximum value q'_{\max} is reached, and then remains adverse right back to the trailing-edge. Table 8 gives the values of q_{\max} , q_{\min} and q'_{\max} for the four symmetrical sections of Fig. 11, with a sink ($C_Q = 0.003\dagger$) at the discontinuity, and Table 9 gives the corresponding values for the cambered versions already mentioned.

9. *Analysis of Results.*—In a discussion of the stalling properties, it is important to observe that, at high incidences, adverse velocity gradients may appear on the upper surface ahead of the discontinuity as well as behind. Again, in relation to the high-speed performance at low incidences, it should be noted that the velocities ahead of the discontinuity may be very large.

Effect of Changes in Fairing Shape on the Upper Surface Velocity Distribution. (See Tables 3 and 6, Figs. 11 and 14). A larger q_L with a more marked concavity near the discontinuity (cf. sections A.2 and A.5) improves the velocity gradients at high incidences, both in front of and behind the discontinuity. At low incidences, the velocity gradients ahead of the maximum thickness become more favourable; the maximum velocity behind the discontinuity is little changed, but the value in front of the discontinuity is considerably increased.

Forward movement of the position of maximum thickness with a general fattening of the forward part of the section (cf. A.2, A.4 and A.6) improves the velocity gradients ahead of the discontinuity at high incidences, but has little effect on those behind the discontinuity. However, at low incidences, the maximum velocity behind the discontinuity is increased and is located further forward, so that the region of adverse velocity gradients becomes more extensive.

* Attention will be restricted here to the upper surface velocity distributions, as at high lifts the velocity gradients on the lower surface will be favourable everywhere except possibly at the lower surface velocity discontinuity.

† This is the practical value envisaged for wings of this thickness.

Rearward movement of the position of the discontinuity without marked alteration in the general section shape, improves the velocity gradients behind the discontinuity at high incidences, at the expense of those in front (*cf.* A.2 and D.1). These latter gradients can be restored to some extent by increasing e_L as already mentioned (*cf.* A.2 and A.5, D.1 and D.2).

Comparison of Maximum Lift Properties.—The maximum lifts of these sections are very difficult to estimate theoretically, especially since the boundary-layer separation may arise before or after the discontinuity, and a reattachment may also occur. For a rough but quick comparison of probable maximum lift properties, an upper limit $C_{L \text{ lim}}$ to the lift coefficient has been chosen, at which the maximum velocity q'_{max} behind the upper surface discontinuity does not exceed twice the free-stream velocity* and the velocity gradients in front of the discontinuity are still favourable. Table 10, derived with the aid of Fig. 15, gives the values of $C_{L \text{ lim}}$ for the four symmetrical shapes A.2, A.5, D.2 and E.1 shown in Fig. 11, for the four cambered versions of these sections with the normal-type centre-line, and for the Lighthill section, both without and with a sink ($C_o = 0.003$) at the discontinuity on the upper surface. It is evident from Fig. 15 that the values of $C_{L \text{ lim}}$ for the sections with the fairing shapes A.2 and A.5 and for the Lighthill are in fact limited by the first condition, $q'_{\text{max}} \leq 2$, while the values for the sections with the fairing shapes D.2 and E.1 are limited by the second condition which requires favourable gradients ahead of the discontinuity.

The values of $C_{L \text{ lim}}$ for the four cambered sections D.2/1, D.2/2, D.2/3, and D.2/4, with the fairing shape D.2 and discontinuous type centre-lines are 2.1, 1.9, 2.0, and 1.8, respectively, as compared with the value 1.3 for the Lighthill section. With these five sections the theoretical velocity gradients ahead of the discontinuity remain favourable for all the high-lift conditions considered, so that $C_{L \text{ lim}}$ is essentially limited by the condition $q'_{\text{max}} \leq 2$.† The increments of $C_{L \text{ lim}}$ obtained with a sink ($C_o = 0.003$) at the discontinuity are less than 0.1 for all five sections, *i.e.*, less than half the increment obtained with the sink on the fairing shape D.2 alone (*see* Table 10).

Drags at High Speeds.—A comparison of the drags of these sections at high speeds is not possible at present. The velocity in a very *small* region ahead of the discontinuity is considerably larger than the maximum velocity behind the discontinuity (*see* Figs. 14 and 16). The region increases in extent as the discontinuity is moved further rearward, and may be important from shock-wave considerations.

10. *Conclusions.*—The comparison of maximum lift properties made in section 9 indicates that the stalling incidences and maximum lifts for the cambered versions of the D.2 shape should be considerably larger than those for the Lighthill section, at practical suction quantities. The improvement has been obtained by moving the suction slot back to $0.02c$ from the leading edge and increasing e_L to $0.02c$. Of the four cambered sections with the velocity discontinuity on the lower surface removed, the section D.2/4 is probably the most acceptable from pitching moment and high speed considerations, although it is the least promising as far as maximum lift is concerned. Low-speed stalling tests are to be made on this section to determine whether the considerable improvements expected are in fact achieved. If the results are satisfactory the effect of the unusual nose shape on the high-speed performance of this type of section will need to be investigated experimentally.

* The maximum velocity q'_{max} provides a measure of the severity of the adverse velocity gradients behind the discontinuity.

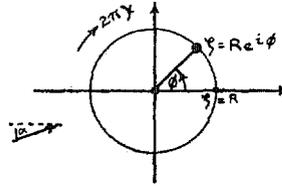
† This suggests that, for cambered sections with a velocity discontinuity on the upper surface only, the position of the discontinuity might with slight advantage be taken a little further back than $0.02c$ from the leading edge, since the velocity gradients behind the discontinuity would then be improved at the expense of those in front.

APPENDIX I

Theoretical Formulae for the Effect of a Sink on an Aerofoil

Theoretical formulæ are derived for the velocity distribution and lift of an aerofoil with a sink on its surface, when the aerofoil is designed by the exact and approximate methods respectively.

The region outside the aerofoil, in the $z(\equiv x + iy)$ plane, is obtained by a conformal transformation from the region outside a circle $\zeta = Re^{i\phi}$, so that $d\zeta/dz \rightarrow 1$ as $|\zeta| \rightarrow \infty$, and so that one particular point on the aerofoil corresponds to a chosen point on the circle. Consider the flow past the circle, with a stream of unit velocity at incidence α , with a sink of strength $2\pi m$ on the circle at $\phi = \beta$, and with circulation $2\pi\kappa$, as indicated in the diagram below.



If \hat{q}_{am} denotes the velocity at the circle boundary, it is readily shown that

$$\hat{q}_{am} = \left| 2 \sin(\phi - \alpha) + \frac{\kappa}{R} + \frac{m}{R} \cot \frac{1}{2}(\phi - \beta) \right| \dots \dots \dots \quad (\text{AI.1})$$

The corresponding velocity over the aerofoil surface will be denoted by q_{am} .

In the exact method of design^{7,8}, the radius R is chosen as unity, and the trailing edge of the aerofoil is taken to correspond to the point $\zeta = 1$ on the circle. When the circulation is adjusted so that $\zeta = 1$ is a stagnation point,

$$\kappa = 2 \sin \alpha + m \cot \frac{1}{2}\beta,$$

and

$$\hat{q}_{am} = \left| 4 \sin \frac{1}{2}\phi \cos \left(\frac{1}{2}\phi - \alpha \right) + m \operatorname{cosec} \frac{1}{2}\beta \sin \frac{1}{2}\phi \operatorname{cosec} \frac{1}{2}(\phi - \beta) \right|.$$

It follows that

$$q_{am}/q_{00} = \left| \frac{\cos \left(\frac{1}{2}\phi - \alpha \right)}{\cos \frac{1}{2}\phi} + \frac{m}{4} \operatorname{cosec} \frac{1}{2}\beta \operatorname{cosec} \frac{1}{2}(\phi - \beta) \sec \frac{1}{2}\phi \right| \dots \dots \quad (\text{AI.2})$$

and the lift coefficient of the aerofoil is

$$C_{Lm} = \frac{4\pi}{c_0} (2 \sin \alpha + m \cot \frac{1}{2}\beta), \quad \dots \dots \dots \quad (\text{AI.3})$$

where c_0 denotes the aerofoil chord corresponding to the unit circle; α represents the angle of incidence measured from the zero-lift attitude without suction. In the design calculations, q_{00} and the co-ordinates x, y are tabulated at convenient intervals of θ , and c_0 is also determined.

In Goldstein's approximate method of design⁹, the co-ordinates of the aerofoil are usually expressed as

$$x = \frac{1}{2}(1 - \cos \theta), \quad y = \frac{1}{2}\psi \sin \theta, \quad \dots \dots \dots \quad (\text{AI.4})$$

where the trailing edge corresponds to $\theta = \pi$. The angular co-ordinate ϕ on the circle is then $\pi - (\theta + \varepsilon)$, where ε is a function of θ ; the radius of the circle will be denoted as R_0 . If, when $\phi = \beta$, $\theta = \eta$ and $\varepsilon = \varepsilon_\eta$, then from equation (AI.1)

$$\hat{q}_{am} = \left| 2 \sin (\theta + \alpha + \varepsilon) + \frac{\kappa}{R_0} - \frac{m}{R_0} \cot \frac{1}{2}(\theta + \varepsilon - \eta - \varepsilon_\eta) \right|.$$

If the circulation is adjusted so that the point on the circle given by $\theta = \pi$ becomes a stagnation point, then

$$\frac{\kappa}{R_0} = 2 \sin (\alpha + \varepsilon_\pi) + \frac{m}{R_0} \cot \frac{1}{2}(\pi + \varepsilon_\pi - \eta - \varepsilon_\eta)$$

where ε_π is the value of ε for $\theta = \pi$. Thus, here, the incidence measured from the zero-lift attitude (without suction) is $\alpha + \varepsilon_\pi$.

It is customary, in the approximate method of design, to write $|d\zeta/dz| = \frac{1}{2}F(\theta)$ for points on the circle, and so

$$\begin{aligned} q_{am} &= |d\zeta/dz| \hat{q}_{am} \\ &= F(\theta) \left| \sin (\theta + \alpha + \varepsilon) + \sin (\alpha + \varepsilon_\pi) \right. \\ &\quad \left. - \frac{m}{2R_0} \left\{ \cot \frac{1}{2}(\theta + \varepsilon - \eta - \varepsilon_\eta) - \cot \frac{1}{2}(\pi + \varepsilon_\pi - \eta - \varepsilon_\eta) \right\} \right|. \end{aligned} \quad (\text{AI.5})$$

The lift coefficient of the aerofoil is

$$C_{Lm} = 4\pi R_0 \left[2 \sin (\alpha + \varepsilon_\pi) + \frac{m}{R_0} \cot \frac{1}{2}(\pi + \varepsilon_\pi - \eta - \varepsilon_\eta) \right]. \quad \dots \quad (\text{AI.6})$$

Now we may write $C_{L0}/a_0 = \sin (\alpha + \varepsilon_\pi)$ where C_{L0} represents the lift coefficient for zero m and where $a_0 = 8\pi R_0$. Furthermore,

$$\begin{aligned} \sin (\theta + \alpha + \varepsilon) &= \sin (\alpha + \varepsilon_\pi) \cos (\theta + \varepsilon - \varepsilon_\pi) + \cos (\alpha + \varepsilon_\pi) \sin (\theta + \varepsilon - \varepsilon_\pi) \\ &= \frac{C_{L0}}{a_0} \cos (\theta + \varepsilon - \varepsilon_\pi) + \left(1 - \frac{C_{L0}^2}{a_0^2} \right)^{1/2} \sin (\theta + \varepsilon - \varepsilon_\pi). \end{aligned}$$

The relations (AI.5) and (AI.6) then become

$$\begin{aligned} q_{am} &= F(\theta) \left| \left(1 - \frac{C_{L0}^2}{a_0^2} \right)^{1/2} \sin (\theta + \varepsilon - \varepsilon_\pi) + \frac{C_{L0}}{a_0} \cos (\theta + \varepsilon - \varepsilon_\pi) + \frac{C_{L0}}{a_0} \right. \\ &\quad \left. - \frac{m}{2R_0} \left\{ \cot \frac{1}{2}(\theta + \varepsilon - \eta - \varepsilon_\eta) - \cot \frac{1}{2}(\pi + \varepsilon_\pi - \eta - \varepsilon_\eta) \right\} \right| \quad \dots \quad (\text{AI.7}) \end{aligned}$$

and $C_{Lm} = C_{L0} + 4\pi m \cot \frac{1}{2}(\pi + \varepsilon_\pi - \eta - \varepsilon_\eta)$. $\dots \dots \dots$ (AI.8)

In the design calculations, ε and $F(\theta)$ are tabulated at convenient intervals of θ , and $a_0 = 8\pi R_0$ is determined. Actually, $4R_0 \simeq 1$, so that $m/2R_0 = 2\pi m/4\pi R_0 \simeq C_0/\pi$ in equation (AI.7)

APPENDIX II

The Glauert Nose-Slot Suction Aerofoil

The design of the Glauert nose-slot suction aerofoil has not previously been reported in detail, but will be presented here*. The exact method^{7,8}, extended to enable the slot shape to be incorporated automatically in the aerofoil, was used. In the following discussion, some of the formulae derived in Appendix I, for the exact method, will be required.

The formulae for the aerofoil co-ordinates (x, y) are

$$x = \int (2 \sin \phi / q_{00}) \cos \chi \, d\phi, \quad y = \int (2 \sin \phi / q_{00}) \sin \chi \, d\phi, \text{ where}$$

$$x(\phi) = (1/2\pi) P \int_{-\pi}^{\pi} \log q_{00}(t) \cot \frac{1}{2}(\phi - t) \, dt$$

is the function conjugate to $\log q_{00}(\phi)$. The function $\log q_{00}$ must satisfy the relations

$$\int_{-\pi}^{\pi} \log q_{00} \, d\phi = 0, \quad \int_{-\pi}^{\pi} \log q_{00} \cos \phi \, d\phi = 0, \quad \int_{-\pi}^{\pi} \log q_{00} \sin \phi \, d\phi = 0. \quad \dots \quad \dots \quad \dots \quad (\text{AII.1})$$

It is usually expressed in terms of the velocity over the upper surface at an upper design incidence α_1 , and over the lower surface at a lower design incidence α_2 ; the necessary relations are provided by the equation (AI.2), when a sink is assumed to lie at $\phi = \beta$. If the sink strength is such that, at incidence α , there is a stagnation point on the circle at $\phi = \beta - \gamma$, equation (AI.2) reduces to

$$\frac{q_{um}}{q_{00}} = \left| \frac{\sin \frac{1}{2}(\phi - \beta + \gamma) \cos \frac{1}{2}(\phi - \gamma - 2\alpha)}{\sin \frac{1}{2}(\phi - \beta) \cos \frac{1}{2}\phi} \right|. \quad \dots \quad \dots \quad \dots \quad \dots \quad (\text{AII.2})$$

Furthermore, if the strength is adjusted so that γ remains constant as α is varied, then

$$\frac{q_{um}}{q_{00}} = \left| \frac{\cos \frac{1}{2}(\phi - \gamma - 2\alpha)}{\cos \frac{1}{2}(\phi - \gamma)} \right|. \quad \dots \quad (\text{AII.3})$$

The velocity over the aerofoil may be specified to be finite and continuous everywhere. A shaped slot is then obtained on the aerofoil of width equal to the sink strength divided by the velocity on the aerofoil at $\phi = \beta^\dagger$.

The velocity distribution was chosen by Glauert to be of the form (with $\alpha_2 = 0$)

$$\left. \begin{aligned} \log q_{0m} = & \log \left| \cos \frac{1}{2}(\phi - \gamma) / \cos \frac{1}{2}(\phi - \gamma - 2\alpha_1) \right| & \dots & \gamma + \alpha_1 < \phi < \pi + \gamma + \alpha_1 \\ & + l + a(1 - \cos \phi) & \dots & \dots & \dots & \dots & 0 < \phi < \beta \\ & + l + b(1 - \cos \phi) & \dots & \dots & \dots & \dots & \beta < \phi < 2\pi \\ & + c(\sin \overline{\beta - \gamma} - \sin \phi) & \dots & \dots & \dots & \dots & \beta - \gamma < \phi < \beta \\ & + d(\sin \overline{\alpha_1 + \gamma} + \sin \phi) & \dots & \dots & \dots & \dots & \pi + \delta < \phi < \pi + \alpha_1 + \gamma \\ & + d(\sin \overline{\alpha_1 + \gamma} - \sin \delta) & \dots & \dots & \dots & \dots & \beta < \phi < \pi + \delta \\ & + g \cos 3\phi & \dots & \dots & \dots & \dots & \pi/2 < \phi < \beta \end{aligned} \right\} \quad (\text{AII.4})$$

From equation (AII.2), we have also

$$\log q_{00} = \log \left| \frac{\sin \frac{1}{2}(\phi - \beta) \cos \frac{1}{2}\phi}{\sin \frac{1}{2}(\phi - \beta - \gamma) \cos \frac{1}{2}(\phi - \gamma)} \right| + \log q_{0m} \quad \dots \quad \dots \quad \dots \quad (\text{AII.5})$$

* The writer gratefully acknowledges information and advice received from Mr. M. B. Glauert concerning the design of this aerofoil.

† In the integration to obtain the aerofoil shape, it is necessary to check, not that the contour closes up, but that there is a slot entry of the correct width; the sides of the slot approach asymptotically to the same direction at a constant width apart.

In view of the relation (AII.3), $\log q_{am}$ and $\log q_{om}$ are given over the ranges $\gamma + \alpha_1 < \phi < \pi + \gamma + \alpha_1$ and $\pi + \gamma + \alpha_1 < \phi < 2\pi + \gamma + \alpha_1$ respectively, by ignoring the log term in the expression (AII.4) for $\log q_{om}$. The purpose of the remaining terms is now briefly explained.

The terms involving the constants l , a and b provide steadily falling velocities over the upper surface at incidence α_1 , and over the lower surface at zero incidence. The c term gives a rising velocity from the slot lip (at $\phi = \beta - \gamma$) into the slot (at $\phi = \beta$), and c is chosen so that $\log q_{am}$ is continuous at $\phi = \beta$. The d terms give a high and non-decreasing velocity from the front stagnation point to the slot at incidence α_1 ; d is chosen to make $d/d\phi (\log q_{am})$ continuous at $\phi = \pi + \gamma + \alpha_1$ and δ is chosen to provide a velocity of suitable magnitude. Finally, the constant g may be arbitrarily assigned a negative constant value to increase M_{crit} at low incidence, but the adverse velocity gradients at high incidence are simultaneously worsened. When α_1 , β , γ , δ and g are assigned, the values of l , a , b , c and d may be obtained from the three conditions (AII.1) together with the two supplementary conditions given above.

Glauert eventually chose $\alpha = 12$ deg, $\beta = 174$ deg, $\gamma = 0$ deg 4 min, $\delta = 4$ deg and $g = -0.065$, which yielded the values $l = -0.0713061$, $a = 0.3693949$, $b = 0.1267340$, $c = 699.5190$, $d = 9.729334$. The aerofoil co-ordinates and the values of the design velocities q_{om} and q_{oo} are set out in Table 2. It is relevant to note that the sink strength chosen gave a slot width far too small for the suction quantities used in the experimental tests.

APPENDIX III

Design Formulae for the Symmetrical Sections

The velocity distribution for a symmetrical aerofoil at zero incidence to the airstream may be expressed, on the basis of Goldstein's Approximation I, in the form⁹

$$q = 1 + g_s$$

where the chordwise co-ordinate $x = \frac{1}{2}(1 - \cos \theta)$ is measured from the leading edge. In the following analysis, g_s is assumed to increase linearly with x in any segment $\theta_{r-1} < \theta < \theta_r$, from the value $g_s'(X_{r-1})$ at $\theta = \theta_{r-1}$ to the value $g_s(X_r)$ at $\theta = \theta_r$, where $g_s(X_r)$ and $g_s'(X_r)$ are not necessarily identical. Thus, for $\theta_{r-1} < \theta < \theta_r$,

$$g_s = \frac{\{-g_s'(X_{r-1}) \cos \theta_r + g_s(X_r) \cos \theta_r\}}{(\cos \theta_{r-1} - \cos \theta_r)} + \frac{\{g_s'(X_{r-1}) - g_s(X_r)\}}{(\cos \theta_{r-1} - \cos \theta_r)} \cos \theta \quad \dots \text{(AIII.1)}$$

Let M_{or} be a generic symbol to represent the contributions to the functions $2y_s, G(\theta) = \int_0^\theta g_s \sin \theta d\theta$, and to the constants $(2e_L)^{1/2}, (2e_T)^{1/2}, C_0$, when $g_s = 1$ for $\theta_{r-1} < \theta < \theta_r^*$. Similarly, let M_{1r} be the corresponding generic symbol when $g_s \equiv \cos \theta$ for $\theta_{r-1} < \theta < \theta_r$. The formulae giving the values of these contributions have already been derived in section 3 of Ref. 11. Summing over the several segments which constitute the whole range $0 < \theta < \pi, r = 1$ to n say, we have

$$2\pi y_s, \text{ etc.} = \sum_r \left\{ \frac{-\cos \theta_r M_{or} + M_{1r}}{\cos \theta_{r-1} - \cos \theta_r} g_s'(X_{r-1}) + \frac{\cos \theta_{r-1} M_{or} - M_{1r}}{\cos \theta_{r-1} - \cos \theta_r} g_s(X_r^*) \right\} \dots \text{(AIII.2)}$$

The remaining functions required for Approximation III then follow from the relations

$$e_s(\theta) = G(\theta) \operatorname{cosec} \theta - C_0 \tan \frac{1}{2}\theta, \quad \dots \dots \dots \dots \dots \dots \dots \text{(AIII.3)}$$

* Note that the contributions themselves are not restricted merely to the range $\theta_{r-1} < \theta < \theta_r$.

$$\left. \begin{aligned} \frac{d\varepsilon_s(\theta)}{d\theta} &= g_s - \frac{G(\theta) \cos \theta}{\sin^2 \theta} - \frac{C_0}{1 + \cos \theta} \\ d\varepsilon_s(\theta)/d\theta &= \frac{1}{2}\{g'_s(0) - C_0\}, \quad d\varepsilon_s(\pi)/d\theta = \frac{1}{2}\{g'_s(X_n) - C_0\} \end{aligned} \right\} \dots \dots \dots \text{(AIII.4)}$$

For the symmetrical sections considered in the main text, $n = 3$, and $g_s(X_r) = g'_s(X_r)$, except when $r = 1$.

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TABLE 1
Some Data from Tests on Aerofoils with Nose-Slot Suction

Data \ Aerofoil		NACA 23015	NACA 0015	Bis 2315	Lighthill	Glauert
Profile (unit chord)	Maximum Thickness	0.15	0.12	0.12	0.086	0.086
	Position of Max. Th.	0.30	0.30	0.50	0.29	0.30
	Nose Radius	0.0248	0.0158	0.003	Beaked Nose	small
	Camber	0.02	0	0.021	0.018	0.019
	Position of Max. Cam.	0.15	—	0.50	0.35	0.48
Max. Lift	$C_{L \max}$ for $C_q = 0$	1.23	1.02	0.68	1.12	1.13
	Optimum slot position	0.20	0.10	≈ 0.01	—	—
	$\Delta C_{L \max}, C_q = 0.0025$	0.40	0.25	0		0.19
	$\Delta C_{L \max}, C_q = 0.0075$	0.95	0.56	0.23	≈ 0.25	≈ 0.25
Max. Incidence	$\alpha_{\max}, C_q = 0$	13.6 deg	11.8 deg	10.0 deg	13.5 deg	12.5 deg
	Optimum slot position	0.17	0.03	0	—	—
	$\Delta \alpha_{\max}, C_q = 0.0025$	8.0 deg	1.8 deg	0.7 deg		≈ 1 deg
	$\Delta \alpha_{\max}, C_q = 0.0075$	12.5 deg	4.0 deg	2.5 deg	≈ 2 deg	≈ 2 deg

TABLE 2
Data for Glauert Nose-Slot Aerofoil

deg	ϕ min	Co-ordinates		Velocity (Zero Incidence)	
		x	y	q_{0m}	q_{00}
0		1.00000	0	0.93118	0.93121
10		0.99145	0.00050	0.93642	0.93645
20		0.96598	0.00226	0.93837	0.93840
30		0.92459	0.00582	0.94650	0.94653
40		0.86928	0.01172	0.96359	0.96362
50		0.80268	0.01982	0.98844	0.98848
60		0.72779	0.02962	1.02008	1.02012
70		0.64764	0.03997	1.05678	1.05683
80		0.56514	0.04959	1.09647	1.09653
90		0.48308	0.05668	1.13616	1.13623
100		0.40217	0.05978	1.13459	1.13468
110		0.32332	0.05976	1.13362	1.13373
120		0.24939	0.05722	1.13516	1.13531
130		0.18282	0.05210	1.13455	1.13477
140		0.12537	0.04427	1.11781	1.11815
150		0.07806	0.03368	1.05874	1.05935
160		0.04104	0.02104	0.91459	0.91592
162		0.03484	0.01839	0.87009	0.87173
164		0.02902	0.01574	0.81877	0.82085
166		0.02355	0.01314	0.75975	0.76251
168		0.01842	0.01063	0.69197	0.69589
170		0.01359	0.00830	0.61420	0.62048
172		0.00900	0.00633	0.52490	0.53852
172	20	0.00825	0.00607	0.50877	0.52540
172	40	0.00751	0.00584	0.49226	0.51351
173		0.00678	0.00565	0.47536	0.50451
173	20	0.00606	0.00552	0.45805	0.50390
173	40	0.00538	0.00549	0.44033	0.54469
173	44	0.00526	0.00550	0.43674	0.57620
173	48	0.00515	0.00551	0.43313	0.64275
173	52	0.00506	0.00553	0.42950	0.84977
173	56	0.00502	0.00555	0.42585	∞
174				0.94850	0

TABLE 2—continued
Data for Glauert Nose-slot Aerofoil

deg	ϕ min	Co-ordinates		Velocity (Zero Incidence)	
		x	y	q_{0m}	q_{00}
174	4	0.00472	0.00535	0.94013	0.46485
174	8	0.00461	0.00537	0.93173	0.61422
174	12	0.00451	0.00538	0.92330	0.68460
174	16	0.00442	0.00538	0.91482	0.72345
174	20	0.00434	0.00538	0.90631	0.74648
174	40	0.00396	0.00533	0.86318	0.77502
175		0.00361	0.00522	0.81908	0.75779
175	20	0.00329	0.00509	0.77396	0.72673
175	40	0.00299	0.00493	0.72779	0.68920
176		0.00270	0.00475	0.68054	0.64780
178		0.00133	0.00339	0.37202	0.35412
180		0.00042	0.00195	0.01298	0
182		0.00001	+0.00035	0.41009	0.42073
184		0.00009	-0.00104	0.91615	0.92552
186		0.00039	-0.00245	1.09265	1.09883
188		0.00226	-0.00379	1.17068	1.17493
190		0.00415	-0.00529	1.19485	1.19789
200		0.02210	-0.01308	1.19067	1.19161
210		0.05388	-0.01964	1.17961	1.18006
220		0.09849	-0.02451	1.16476	1.16503
230		0.15507	-0.02751	1.14670	1.14688
240		0.22156	-0.02829	1.12614	1.12627
250		0.29679	-0.02711	1.10382	1.10392
260		0.37862	-0.02427	1.08051	1.08059
270		0.46482	-0.02020	1.05699	1.05705
280		0.55291	-0.01547	1.03399	1.03404
290		0.64019	-0.01067	1.01216	1.01220
300		0.72381	-0.00634	0.99209	0.99213
310		0.80086	-0.00292	0.97430	0.97434
320		0.86854	-0.00066	0.95920	0.95923
330		0.92424	+0.00044	0.94712	0.94715
340		0.96574	0.00060	0.93832	0.93835
350		0.99135	0.00026	0.93297	0.93300
360		1.00000	0	0.93118	0.93121

TABLE 3
Design and Shape Data of Symmetrical Sections

Section No.	Design data							Max. thickness	Position of max. thickness	Position of slot	q_z	Thickness at $x = X_1$
	X_1	X_2	$g_s'(0)$	$g_s(X_1)$	$g_s'(X_1)$	$g_s(X_2)$	$g_s(1)$					
A.1	0.005	0.35	0.3	0.3	0.1	0.13	-0.075	0.083	0.3	0.005	0.0062	0.0145
A.2	0.005	0.35	0.5	0.5	0.1	0.13	-0.075	0.083	0.3	0.005	0.0084	0.0157
A.3	0.005	0.35	0.5	0.3	0.1	0.13	-0.075	0.083	0.3	0.005	0.0076	0.0149
A.4	0.005	0.35	0.5	0.5	0.3	0.045	-0.04	0.080	0.2	0.005	0.0160	0.0238
A.5	0.005	0.35	1.3	1.3	0.1	0.125	-0.07	0.081	0.3	0.005	0.0200	0.0206
A.6	0.005	0.35	0.5	0.5	0.15	0.113	-0.065	0.082	0.25	0.005	0.0103	0.0180
B.1	0.005	0.25	0.5	0.5	0.1	0.14	-0.065	0.082	0.3	0.005	0.0086	0.0159
C.1	0.003	0.35	0.5	0.5	0.1	0.13	-0.07	0.084	0.3	0.003	0.0074	0.0118
D.1	0.02	0.35	0.25	0.25	0.1	0.125	-0.07	0.081	0.3	0.02	0.0070	0.0294
D.2	0.02	0.35	0.7	0.7	0.1	0.125	-0.07	0.083	0.3	0.02	0.020	0.0408
E.1	0.05	0.35	0.5	0.5	0.1	0.12	-0.07	0.083	0.3	0.05	0.0204	0.0637

TABLE 4
Design and Shape Data for Simple Normal-Type Centre-line
 ($C_{L \text{ opt}} = 0.2$)

x	y _c	ψ _c	ε _c	dε _c /dθ
0	0	0	-0.04244	0
0.001	0.0001060	0.003354	-0.04229	0.00469
0.002	0.0002114	0.004733	-0.04214	0.00662
0.003	0.0003167	0.005788	-0.04200	0.00812
0.004	0.0004216	0.006676	-0.04185	0.00933
0.005	0.0005260	0.007454	-0.04170	0.01042
0.006	0.0006300	0.008155	-0.04155	0.01139
0.0075	0.0007851	0.009099	-0.04133	0.01271
0.0125	0.0012966	0.011670	-0.04060	0.01627
0.02	0.0020464	0.014617	-0.03950	0.02032
0.03	0.0030135	0.017666	-0.03806	0.02447
0.05	0.0048383	0.022200	-0.03523	0.03052
0.1	0.0087854	0.029285	-0.02844	0.03947
0.2	0.0142603	0.035651	-0.01613	0.04586
0.3	0.0169341	0.036953	-0.00552	0.04473
0.4	0.0173161	0.035346	+0.00342	0.03950
0.5	0.0159155	0.031831	0.01061	0.03185
0.6	0.0132417	0.027029	0.01613	0.02287
0.7	0.0098039	0.021394	0.01995	0.01361
0.8	0.0061115	0.015279	0.02207	0.00509
0.9	0.0026738	0.008913	0.02251	-0.00127
1.0	0	0	0.02122	0

Note.—The centre-line is derived from the simple centre-line loading formula

$$s_i = \frac{C_{L \text{ opt}}}{2\pi} (2 \sin \theta + \sin 2\theta),$$

and is designed¹⁰ to give no negative loading and a value for $C_{m0}/C_{L \text{ opt}} (= -\frac{1}{3})$ which is a minimum consistent with this. It follows, in the usual notation⁹, that

$$y = \frac{C_{L \text{ opt}}}{24\pi} (3 + \cos \theta - 3 \cos 2\theta - \cos 3\theta),$$

$$\varepsilon = -\frac{C_{L \text{ opt}}}{6\pi} (3 \cos \theta + \cos 2\theta), \quad d\varepsilon_c/d\theta = \frac{C_{L \text{ opt}}}{6\pi} (3 \sin \theta + 2 \sin 2\theta).$$

TABLE 5
Design and Shape Data for Discontinuous-Type Centre-Lines

Section No.	X ₁	g _i (0)	g _i (X ₁)	g _i '(X ₁)	g _i (1)	C _{m0}
D.2/1	0.02	0.68	0.68	0.08	0.08	-0.068
D.2/2	0.02	0	0.68	0.08	0.08	-0.075
D.2/3	0.02	0.6	0.6	0	0	0.012
D.2/4	0.02	0	0.6	0	0	0.006

Note.—The centre-lines were designed for use with the fairing shape D.2. The significance of the centre-line design data, X₁, g_i(0), g_i(X₁), g_i'(X₁) and g_i(1) is shown in Fig. 10b.

TABLE 6
Velocity Distributions for Symmetrical Sections

Section No.	Velocity Distribution $C_L = 0$			Velocity Distribution $C_L = 0.8$				Velocity Distribution $C_L = 1.0$				Velocity Distribution $C_L = 1.5$			
	q_1	q_1'	q'_{\max} (pos.)	q_{\max}	q_1	q_1'	q'_{\max}	q_{\max}	q_1	q_1'	q'_{\max}	q_{\max}	q_1	q_1'	q'_{\max}
A.1	1.08	0.89		2.86	2.70	2.22	—	3.36	3.10	2.55	—				
A.2	1.24	0.83	1.11 ($x=0.35$)	—	2.95	1.98	2.04	3.44	3.37	2.27	2.31	4.70	4.43	2.98	3.02
A.3	1.06	0.87	1.11 ($x=0.35$)	2.91	2.59	2.11	2.12	3.41	2.97	2.42	2.43				
A.4	1.01	0.85	1.22 ($x=0.05$)	—	2.41	2.01	2.07	—	2.76	2.30	2.34				
A.5	1.93	0.50	1.12 ($x=0.35$)	—	3.93	1.02	1.72	—	4.42	1.15	1.92	—	5.65	1.47	2.40
A.6	1.17	0.84	1.13 ($x=0.15$)	—	2.78	1.99	2.05	3.19	3.18	2.27	2.32				
B.1	1.23	0.83		—	2.93	1.97	2.03	3.42	3.35	2.25	2.31				
C.1	1.12	0.76	1.2 ($x=0.35$)	—	3.13	2.10	2.19	3.63	3.63	2.44	2.52				
D.1	1.19	1.03	1.12 ($x=0.35$)	2.49	2.09	1.81	—	2.94	2.32	2.00					
D.2	1.64	0.90	1.12 ($x=0.35$)	—	2.66	1.45	1.55	—	2.91	1.59	1.68	3.71	3.53	1.93	2.02
E.1	1.50	1.01	1.12 ($x=0.3$)					2.48	2.26	1.52	1.54	3.26	2.64	1.77	1.78

Note.—See Fig. 10c for meaning of q_1 , q_1' , q_{\max} , q'_{\max} .

TABLE 7a
Velocity Distributions for Cambered Sections with Normal-Type Centre-Line
 (Camber = 1.7 per cent, $C_{L\text{ opt}} = 0.2$)

Section No.	Velocity Distribution $C_L = 0.2$			Velocity Distribution $C_L = 1.0$				Velocity Distribution $C_L = 1.5$			
	q_1	q_1'	q'_{max} (POS.)	q_{max}	q_1	q_1'	q'_{max}	q_{max}	q_1	q_1'	q'_{max}
A.2/N	1.20	0.81	1.17 ($x=0.35$)	—	2.89	1.95	2.02	4.10	3.93	2.66	2.71
A.5/N	1.87	0.50	1.20 ($x=0.35$)	—	3.84	1.02	1.72	—	5.06	1.34	2.21
D.2/N	1.63	0.90	1.20 ($x=0.3$)	—	2.65	1.47	1.58	3.31	3.28	1.81	1.92
E.1/N	1.53	1.04	1.20 ($x=0.3$)	2.19	2.16	1.47	1.50	2.90	2.54	1.73	1.74

TABLE 7b
Velocity Distributions for Cambered Sections with Discontinuous-Type Centre-Lines

Section No.	Velocity Distribution $C_L = 0.2$			Velocity Distribution $C_L = 1.0$			Velocity Distribution $C_L = 1.5$			Velocity Distribution $C_L = 2.0$		
	q_1	q_1'	q'_{max}									
D.2/1	2.21	0.61	1.16	3.45	0.96	1.43	4.21	1.17	1.69	4.96	1.38	1.95
D.2/2	2.16	0.74	1.17	3.50	1.21	1.49	4.33	1.49	1.77	5.15	1.77	2.05
D.2/3	2.67	0.70	1.16	3.89	1.02	1.52	4.64	1.22	1.76	5.37	1.41	2.01
D.2/4	2.68	0.87	1.17	4.00	1.29	1.58	4.80	1.55	1.85	5.59	1.81	2.11

Note.—See Fig. 10c for meaning of $q_1, q_1', q_{\text{max}}, q'_{\text{max}}$.

TABLE 8
Velocity Distributions for Symmetrical Sections with Sink ($C_0 = 0.003$) at upper surface velocity discontinuity

Section No.	X_1	Velocity Distribution $C_L = 0.8$			Velocity Distribution $C_L = 1.0$			Velocity Distribution $C_L = 1.5$		
		q_{max}	q_{min}	q'_{max}	q_{max}	q_{min}	q'_{max}	q_{max}	q_{min}	q'_{max}
A.2	0.005	—	—	1.86	—	—	2.10	—	—	2.69
A.5	0.005	—	—	1.60	—	—	1.79	—	—	2.27
D.2	0.02	—	—	1.50	—	—	1.62	3.78	3.74	1.92
E.1	0.05	—	—	—	2.51	2.41	1.48	3.29	2.82	1.71

TABLE 9

Velocity Distributions for Cambered Sections with Normal-Type Centre-Line, with Sink ($C_0 = 0.003$) at upper surface velocity discontinuity

(Camber = 1.7 per cent, $C_{L \text{ opt}} = 0.2$)

Section No.	X_1	Velocity Distribution $C_L = 1.0$			Velocity Distribution $C_L = 1.5$		
		q_{\max}	q_{\min}	q'_{\max}	q_{\max}	q_{\min}	q'_{\max}
A.2/N	0.005	—	—	1.86	—	—	2.46
A.5/N	0.005	—	—	1.62	—	—	2.09
D.2/N	0.02	—	—	1.55	—	—	1.85
E.1/N	0.05	—	—	1.47	2.92	2.68	1.69

Note.—See Fig. 10c for meaning of q_{\max} , q'_{\max} , q_{\min} .

TABLE 10

Values of $C_{L \text{ lim}}$ for Symmetrical Sections and for Cambered Versions with Normal-Type Centre-Line

Type of Fairing	q^L	X_1	Symmetrical	Cambered	Symmetrical with sink	Cambered with sink
A.2	0.008	0.005	0.78	1.0	0.92	1.12
A.5	0.02	0.005	1.08	1.28	1.20	1.48
D.2	0.02	0.02	1.14	1.44	1.40	1.68
E.1	0.02	0.05	0.72	0.94	0.86	1.06
Lighthill section with discontinuity at a beaked leading edge.	—	1.3	—	1.4

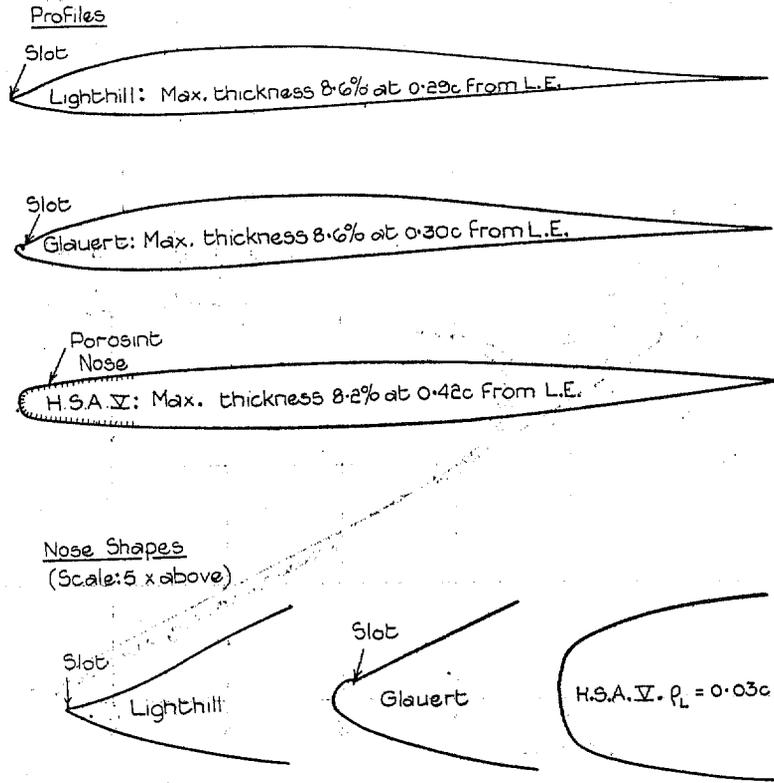


FIG. 1. Theoretical shapes of thin nose-suction aerofoils tested in N.P.L. 4-ft wind tunnel.

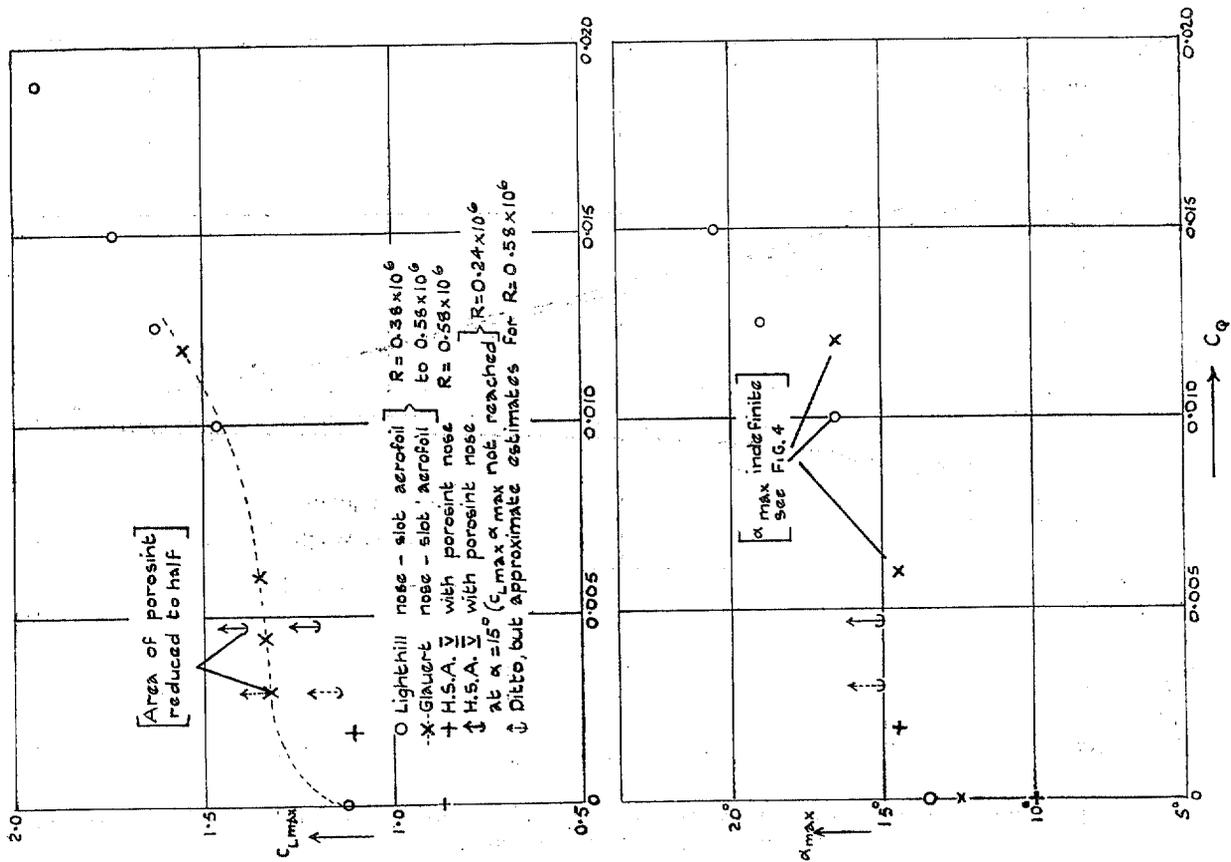


FIG. 2. Results from tests in N.P.L. 4-ft wind tunnel.

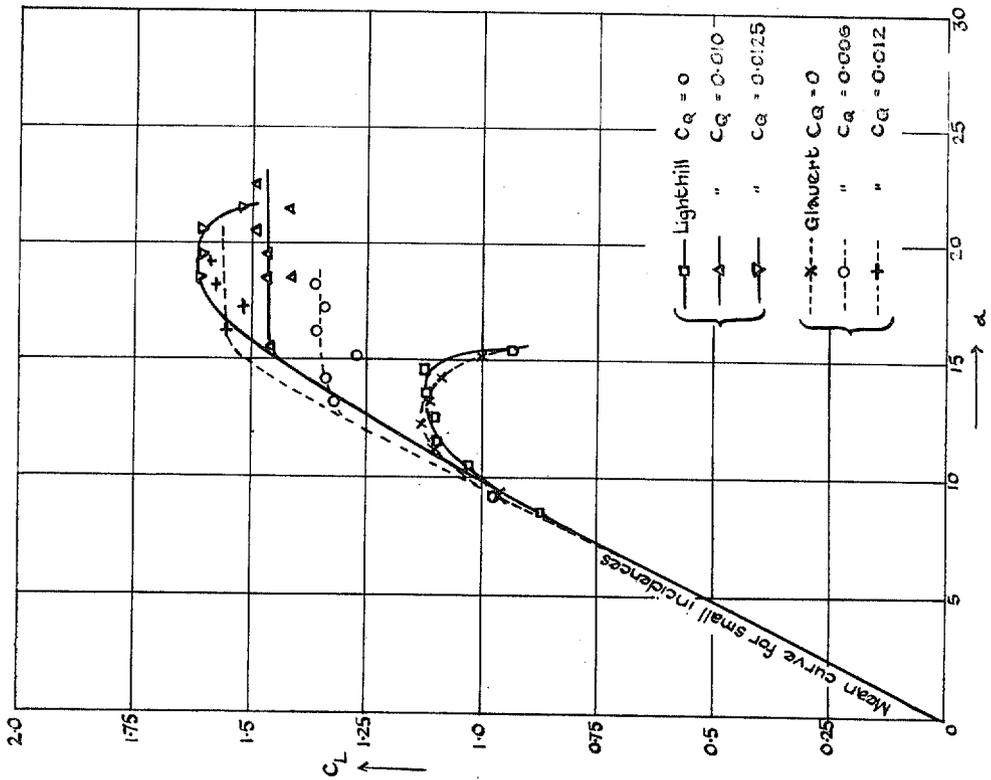


Fig. 3. Some typical experimental lift curves for Lighthill and Glauert nose-slot aerofoils ($R = 0.38 \times 10^6$ to 0.58×10^6).

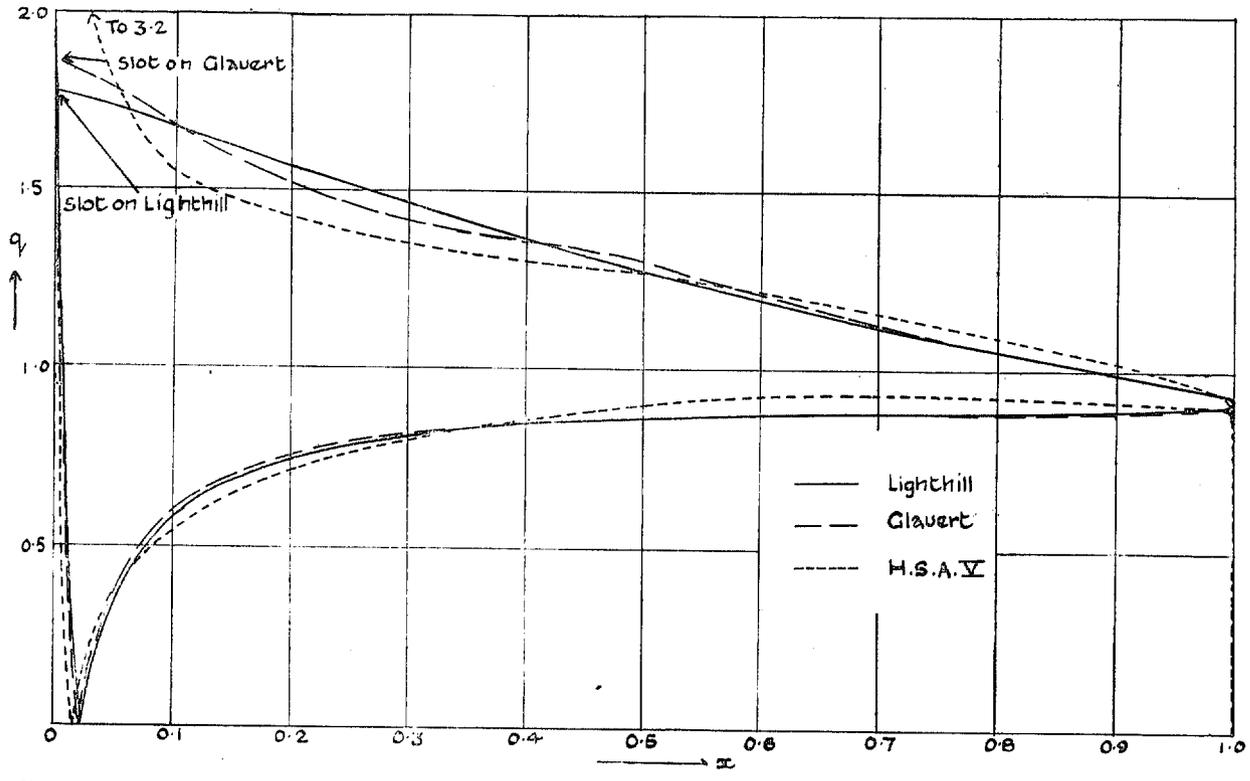


Fig. 4. Comparison of theoretical velocity distributions at 10 deg incidence for the Lighthill, Glauert and H.S.A. V aerofoils, without sink.

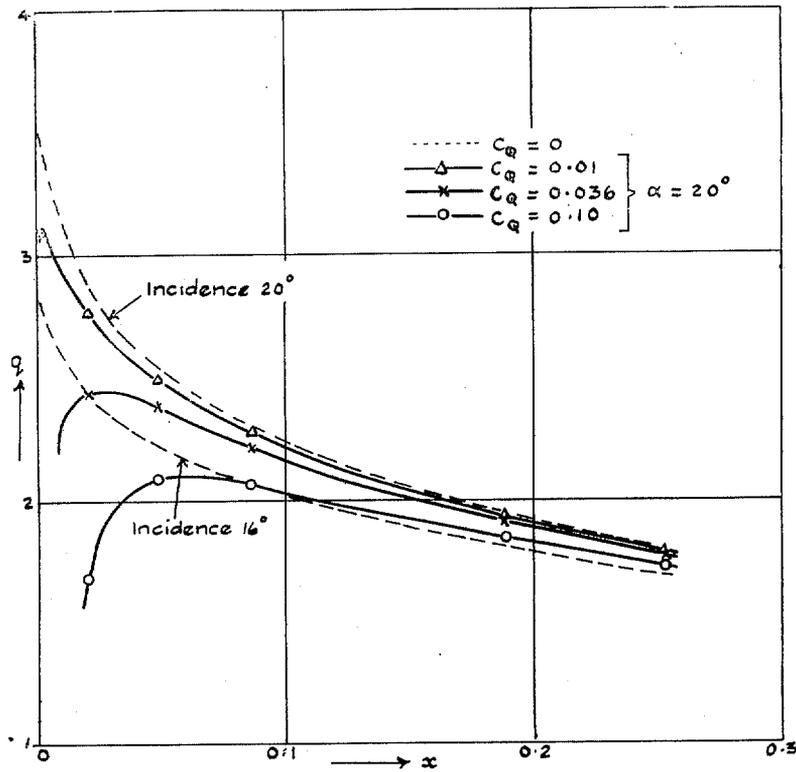


FIG. 5. Theoretical velocity distributions for Lighthill aerofoil at high incidence with sink at leading edge.

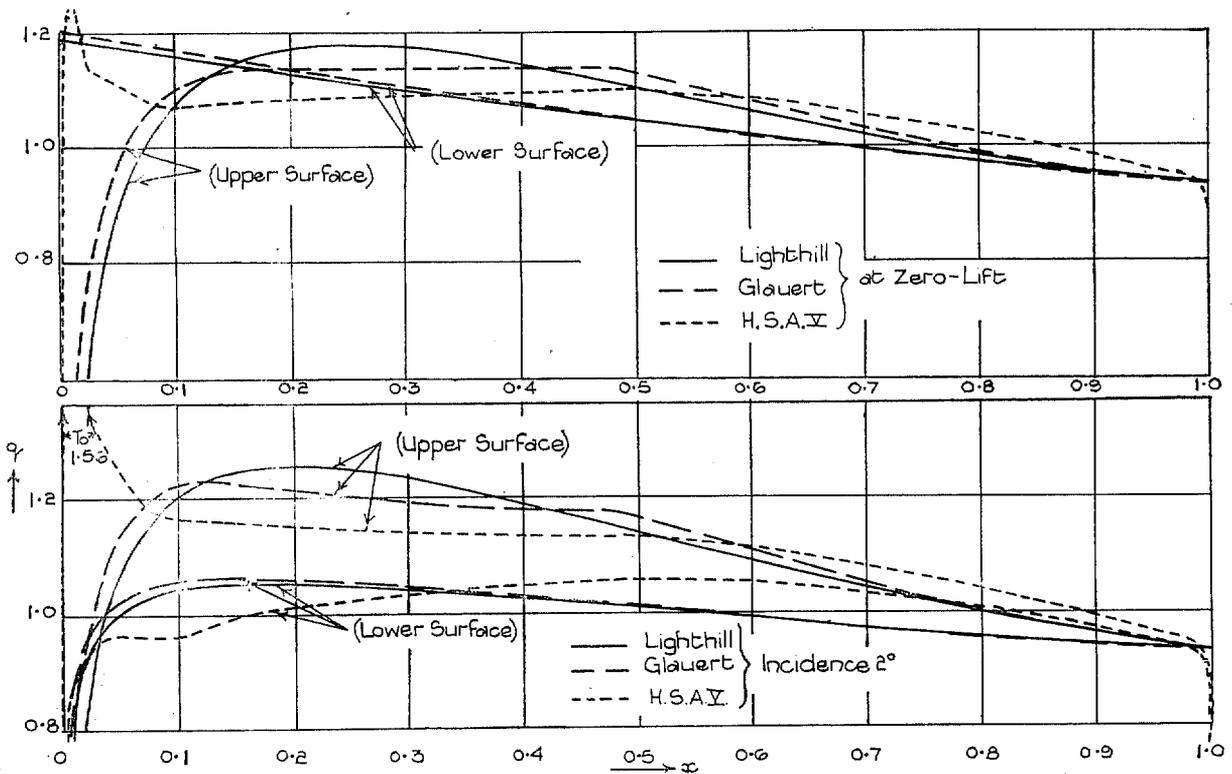


FIG. 6. Comparison of theoretical velocity distributions for the Lighthill, Glauert and H.S.A. V aerofoils at zero-lift and at 2 deg incidence, without sink.

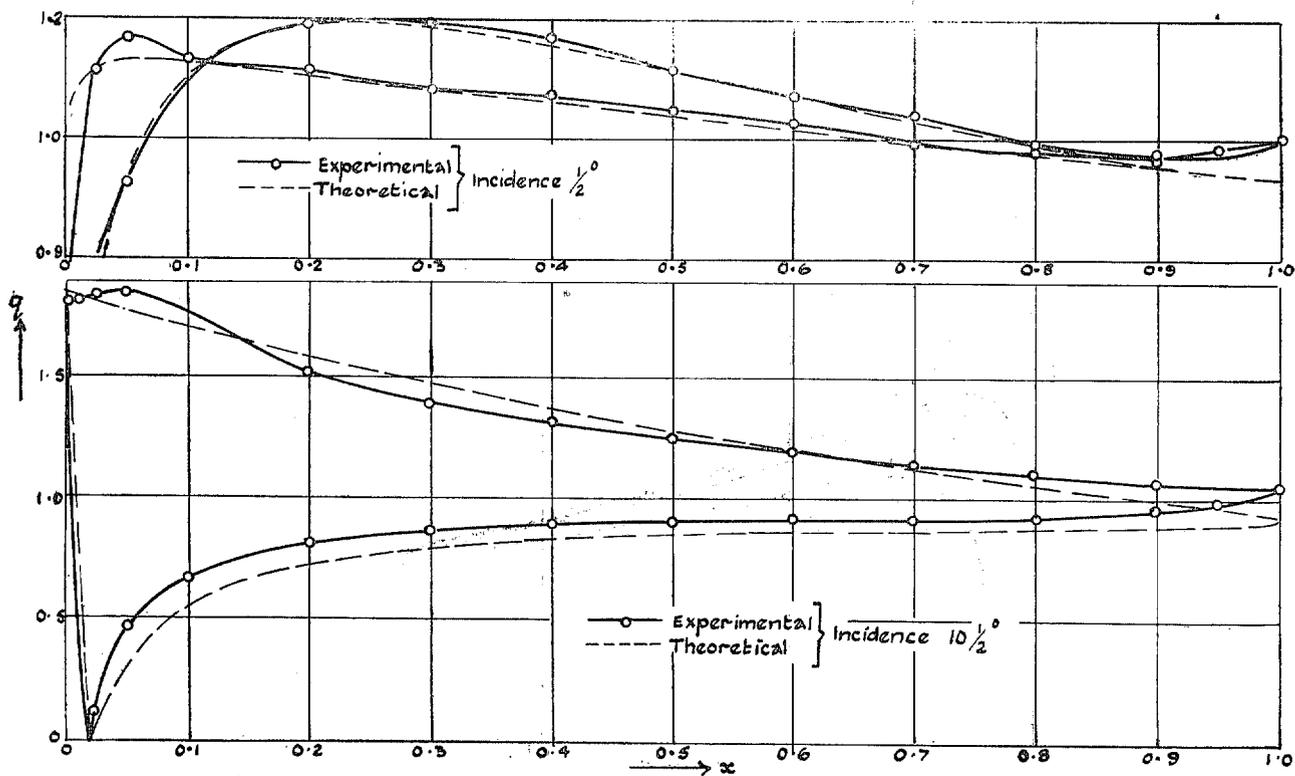


FIG. 7. Comparison of experimental and theoretical velocity distributions for Lighthill nose-slot aerofoil, without suction

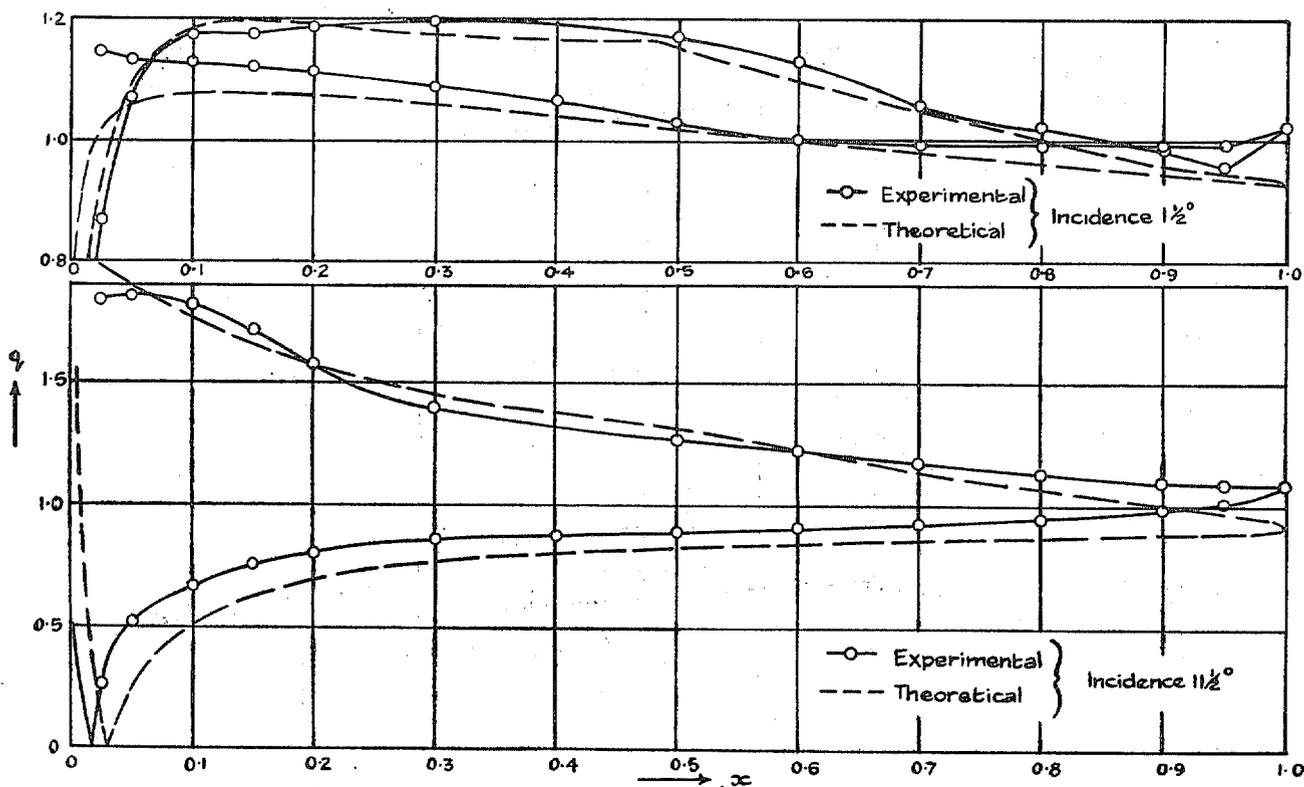


FIG. 8. Comparison of experimental and theoretical velocity distributions for Glauert nose-slot aerofoil, without suction.

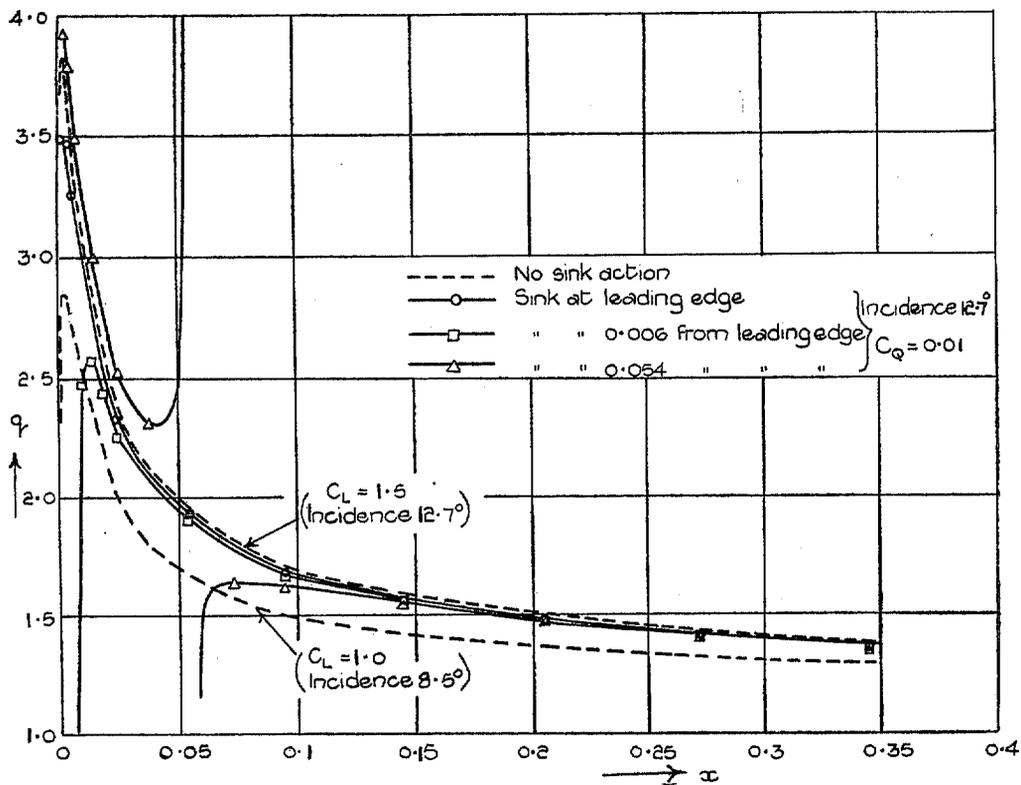


FIG. 9. Theoretical velocity distribution for H.S.A. V aerofoil at high incidences with and without sink on nose.

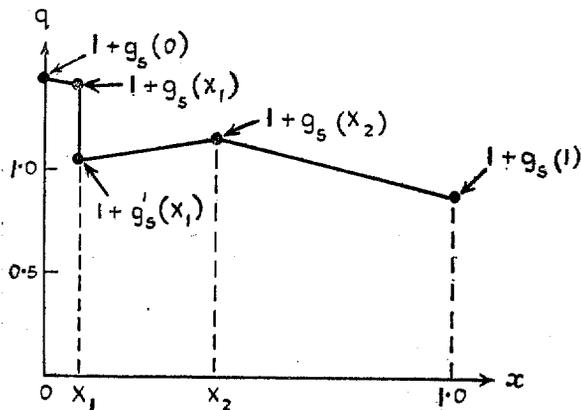


FIG. 10a. Approximation I velocity distribution $q \equiv 1 + g_s$ for symmetrical section at zero incidence.

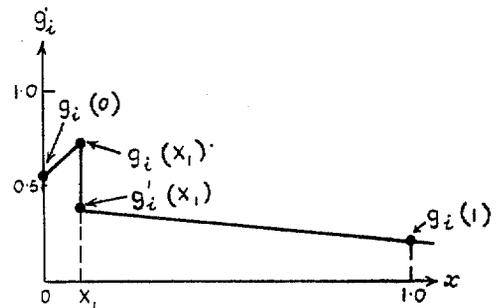


FIG. 10b. Distribution of g_s for centre-line eliminating velocity discontinuity on aerofoil lower surface.

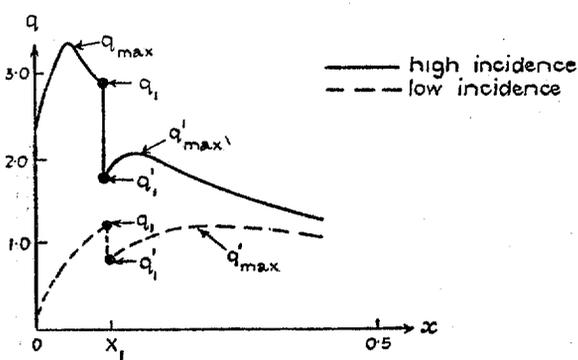


FIG. 10c. General form of Approximation III velocity distribution on upper surface.

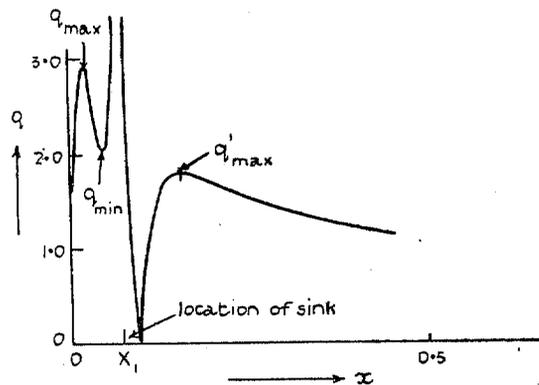
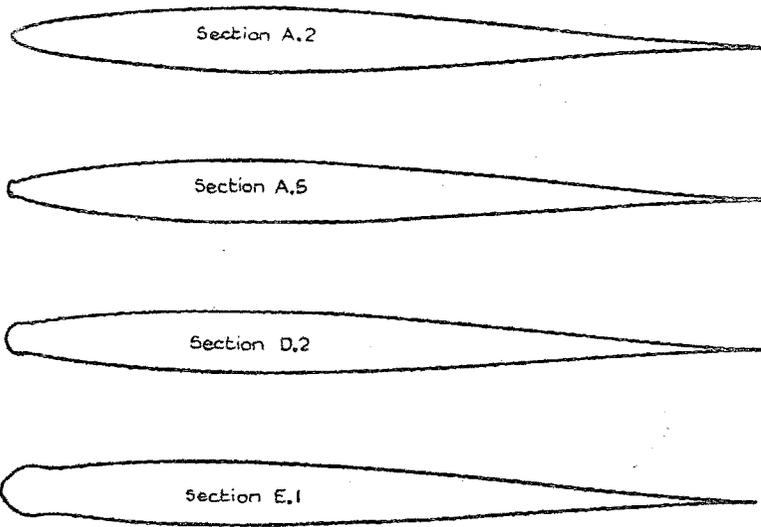


FIG. 10d. General form of Approximation III velocity distribution on upper surface, at high lift, with sink at discontinuity.



Nose Shapes
(Scale: 5 x above)

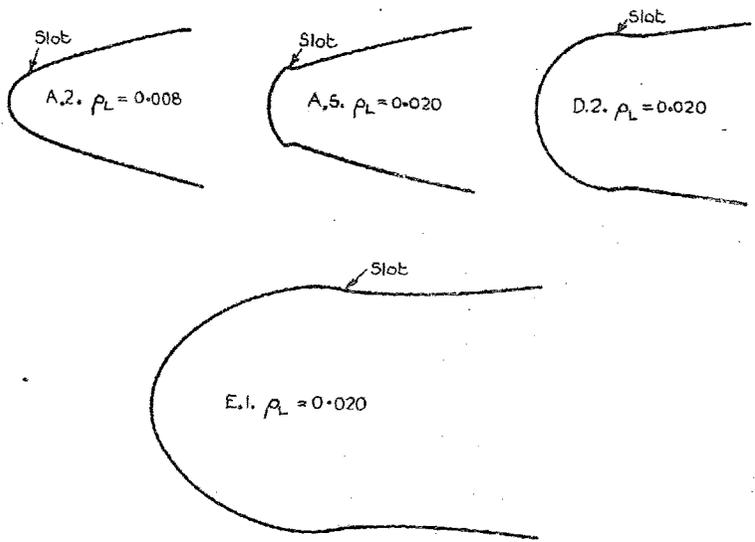
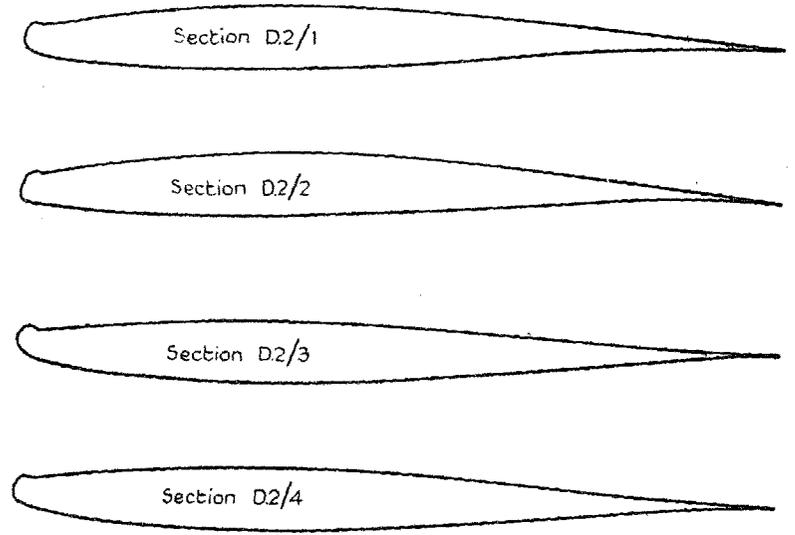


FIG. 11. Theoretical shapes of four typical symmetrical sections for nose-slot suction.



Nose Shapes
(Scale: 5 x above)

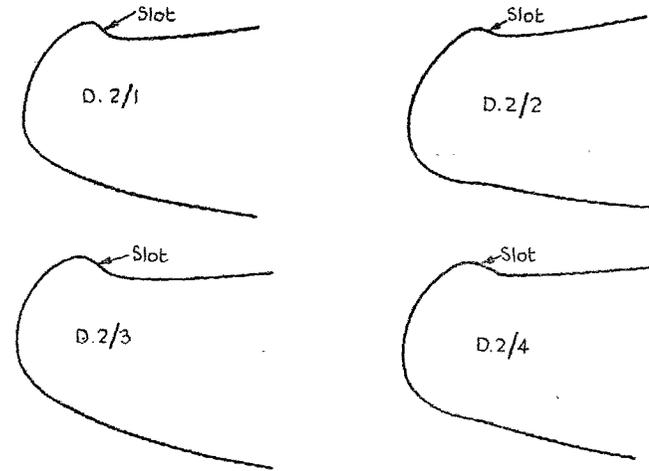


FIG. 12. Theoretical shapes of four cambered sections for nose-slot suction with fairing shape D.2 and discontinuous-type centre-lines.

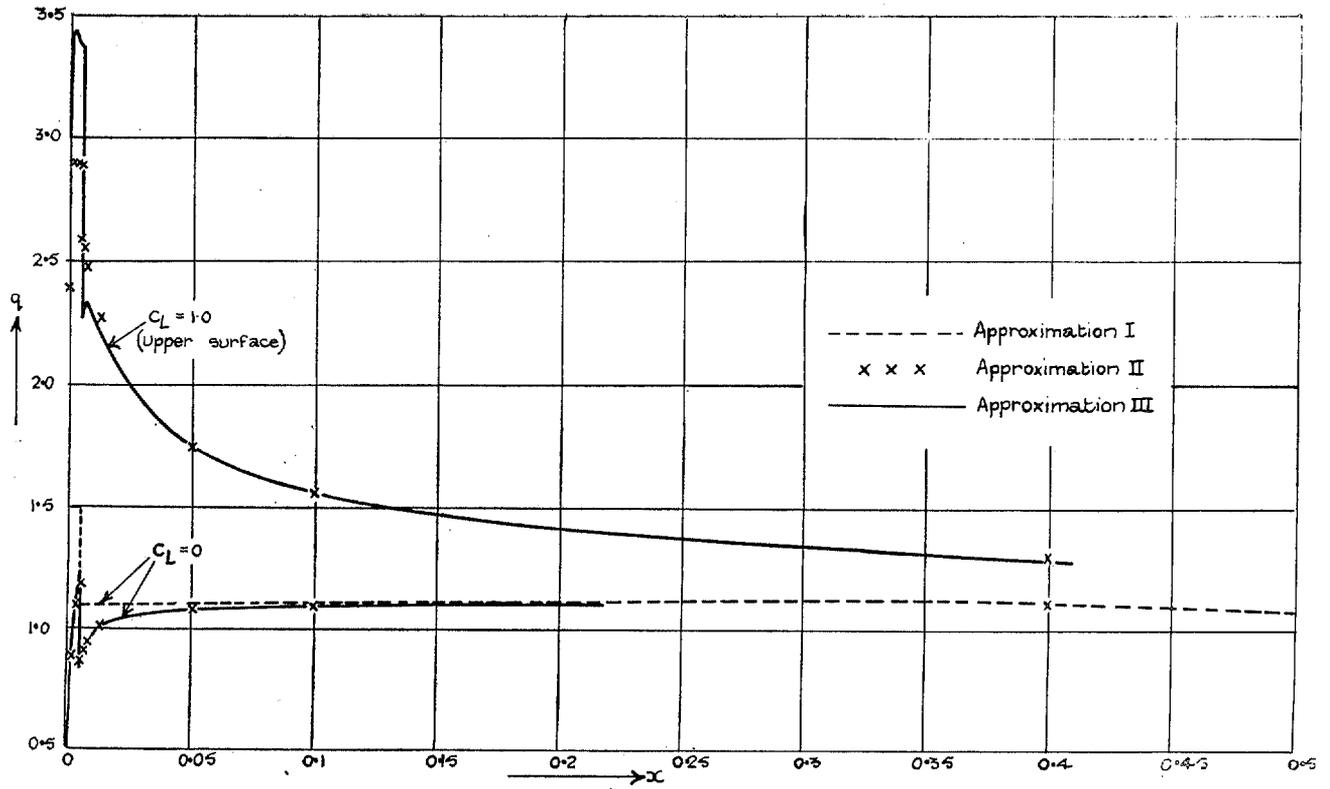


FIG. 13. Comparison of theoretical velocity distributions for symmetrical section A.2 as given by Approximations I, II and III.

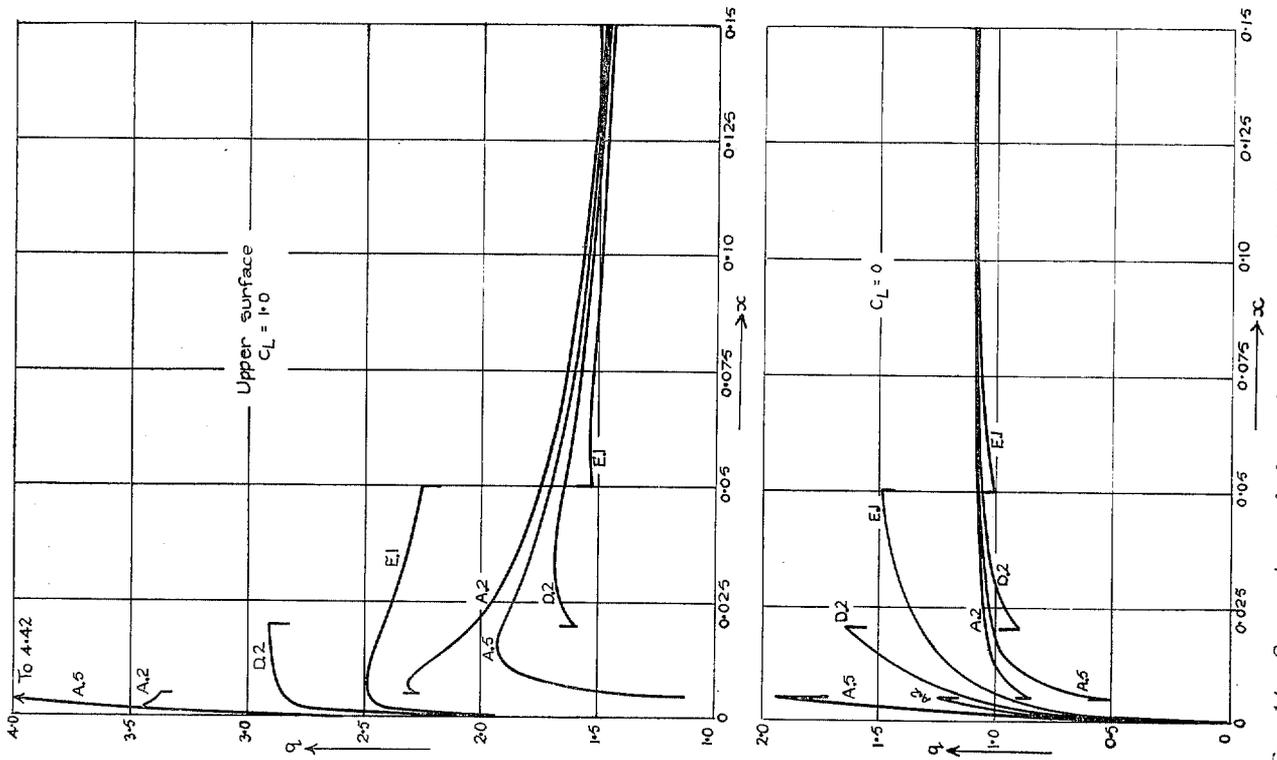


FIG. 14. Comparison of theoretical velocity distributions (without sink) for four typical symmetrical sections.

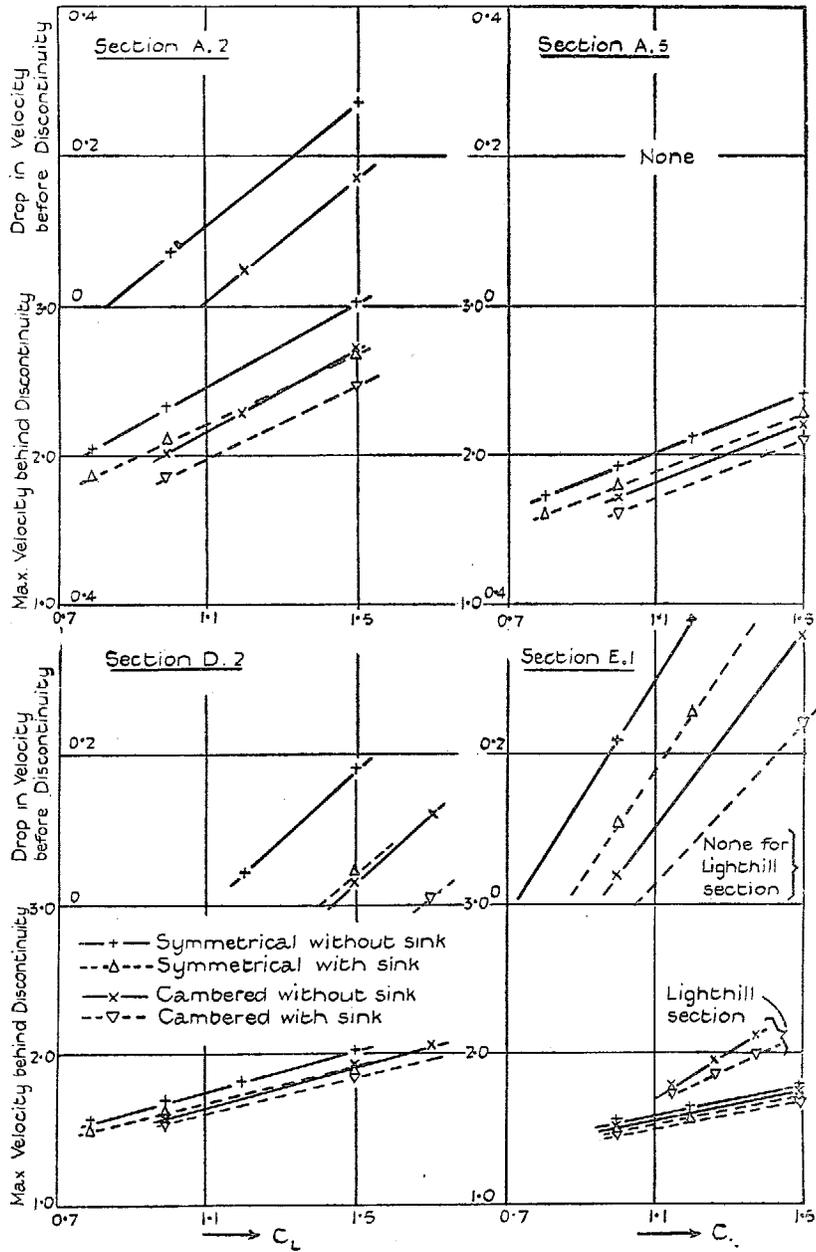


FIG. 15. Comparisons of drop in velocity before discontinuity, and of maximum velocity behind discontinuity, for symmetrical sections and for cambered versions with normal-type centre-line.

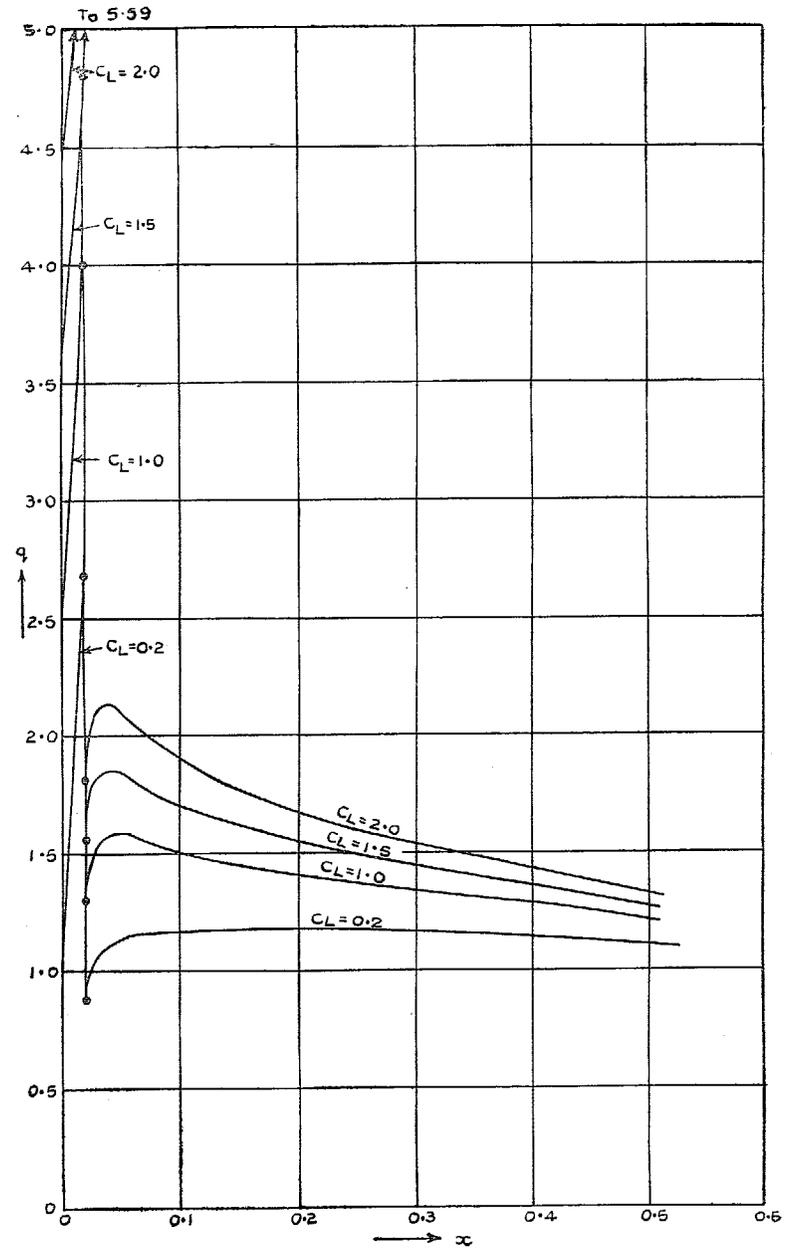


FIG. 16. Theoretical velocity distributions for cambered D.2/4 section as given by Approximation III.

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